

Programowanie współbieżne

LABORATORIUM - PROGRAMY, FORTRAN

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Programy I

circle.f90 - Prosty program.

```
! Circle

MODULE Circle_Operations
IMPLICIT NONE
CONTAINS
FUNCTION Area(radius)
REAL :: Area
REAL, INTENT(IN) :: Radius
Area = Radius**2 * 3.14159
END FUNCTION Area
FUNCTION Circumference(radius)
REAL :: Circumference
REAL, INTENT(IN) :: Radius
Circumference = Radius * 2 * 3.14159
END FUNCTION Circumference
END MODULE Circle_Operations

PROGRAM Circle
USE Circle_Operations
IMPLICIT NONE
REAL :: r=5.0
```

Programy II

```
PRINT *, "Area=",Area(r)
PRINT *, "Circumference=",Circumference(r)
END PROGRAM Circle
```

Programy III

oporniki.f90 - *Moduły. Interfejsy. Przykład dodawania oporów.*

```
!oporniki

MODULE oporniki
! dodawanie oporow
! a.rowno.b    - rownolegle
! a.szereg.b   - szeregowo
! Zadanie. DOPISAC czesc zwiiazana z zamiana jednostek.

TYPE opornik
    REAL wartosc
    CHARACTER*4 miano
END TYPE opornik

INTERFACE OPERATOR (.SZEREG.)
    MODULE PROCEDURE SZ
END INTERFACE
INTERFACE OPERATOR (.ROWNO.)
    MODULE PROCEDURE RO
END INTERFACE
```

Programy IV

CONTAINS

```
FUNCTION SZ(a, b) RESULT(res)
    TYPE(opornik), INTENT(IN) :: a, b
    TYPE(opornik) res
    res%wartosc=a%wartosc+b%wartosc
    IF (a%miano==b%miano) THEN
        res%miano=a%miano
    ELSE
        res%miano="?"
    END IF
END FUNCTION SZ
FUNCTION RO(a, b) RESULT(res)
    TYPE(opornik), INTENT(IN) :: a, b
    TYPE(opornik) res
    REAL r
    r=1.0/a%wartosc+1.0/b%wartosc
    res%wartosc=1.0/r
    IF (a%miano==b%miano) THEN
        res%miano=a%miano
    ELSE
        res%miano="?"
    END IF
END FUNCTION RO
```

Programy V

```
END MODULE OPORNIKI

program d
use oporniki
TYPE(opornik) a, b, c

a%wartosc=21.0; a%miano="om"
b%wartosc=87.0; b%miano="om"

c = a.ROWNO.b
write(*,*) 'rowno : ', c%wartosc, c%miano

c = a.SZEREG.b
write(*,*) 'szereg: ', c%wartosc, c%miano

end program d
```

Programy VI

quaternions.f90 - Kwaterniony.

```
module Quaternions

    type, public :: quaternion
        real :: a, b, c, d
    end type quaternion

    intrinsic :: conjg

    private quat_mul_real, real_mul_quat, quat_mul_int, &
        int_mul_quat, quat_mul, quat_sub, quat_div, &
        quat_div_real, quat_div_int, quat_conjg

    interface operator (+)
        module procedure quat_add
    end interface

    interface operator (*)
        module procedure quat_mul_real
        module procedure real_mul_quat
    end interface
```

Programy VII

```
module procedure quat_mul_int
module procedure int_mul_quat
module procedure quat_mul
end interface

interface operator (-)
    module procedure quat_sub
end interface

interface operator (/)
    module procedure quat_div
!     module procedure quat_div_real
!     module procedure quat_div_int
end interface

interface conjg
    module procedure quat_conjg
end interface

contains

function quat_add(x,y) result (res)
    type(quaternion), intent(in) :: x, y
    type(quaternion) :: res
```

Programy VIII

```
res % a = x % a + y % a
res % b = x % b + y % b
res % c = x % c + y % c
res % d = x % d + y % d
end function quat_add

function quat_sub(x,y) result (res)
    type(quaternion), intent(in) :: x, y
    type(quaternion) :: res
    res % a = x % a - y % a
    res % b = x % b - y % b
    res % c = x % c - y % c
    res % d = x % d - y % d
end function quat_sub

function quat_conjg(x) result (res)
    type(quaternion), intent(in) :: x
    type(quaternion) :: res
    res % a = x % a
    res % b = -(x % b)
    res % c = -(x % c)
    res % d = -(x % d)
end function quat_conjg
```

Programm IX

```
function quat_mul_real(x,r) result (res)
    ! quat * real
    type(quaternion), intent(in) :: x
    real, intent(in) :: r
    type(quaternion) :: res
    res % a = x % a *r
    res % b = x % b *r
    res % c = x % c *r
    res % d = x % d *r
end function quat_mul_real

function real_mul_quat(r,x) result (res)
    ! real * quat
    type(quaternion), intent(in) :: x
    real, intent(in) :: r
    type(quaternion) :: res
    res = quat_mul_real(x,r)
end function real_mul_quat

function int_mul_quat(i,x) result (res)
    ! integer * quat
    type(quaternion), intent(in) :: x
    integer, intent(in) :: i
    type(quaternion) :: res
```

Programy X

```
res = quat_mul_real(x,real(i))
end function int_mul_quat

function quat_mul_int(x,i) result (res)
    ! quat * integer
    type(quaternion), intent(in) :: x
    integer, intent(in) :: i
    type(quaternion) :: res
    res = int_mul_quat(i,x)
end function quat_mul_int

function quat_norm(q) result(res)
    type(quaternion), intent(in) :: q
    real res
    real :: ap, bp, cp, dp
    ap = q % a
    bp = q % b
    cp = q % c
    dp = q % d
    res = sqrt(ap*ap+bp*bp+cp*cp+dp*dp)
end function quat_norm

function quat_div(x,y) result (res)
    type(quaternion), intent(in) :: x, y
```

Programy XI

```
type(quaternion) :: res
real r
r = 1.0/quat_norm(y)**2
res = quat_mul_real(x,r)
end function quat_div

! MULTIPLICATION
function quat_mul(x,y) result (res)
type(quaternion), intent(in) :: x, y
type(quaternion) :: res
real r
res%a=0.; res%b=0.; res%c=0.; res%d=0.
end function quat_mul

subroutine quaternion_print(q)
type(quaternion), intent(in) :: q
real :: ap, bp, cp, dp
ap = q % a
bp = q % b
cp = q % c
dp = q % d
print "(a1,4f12.6,a1)", "(",ap,bp,cp,dp,")"
end subroutine quaternion_print
```

Program XII

```
end module Quaternions
!
!-----
! TEST
Program Quater
    use Quaternions
    type(quaternion) :: u, v, w
    u=quaternion(1,2,2,1)
    v=quaternion(4,3,2,1)
    w=u+v
    call quaternion_print(w)
    call quaternion_print(conjg(w))
    call quaternion_print(w/w)
    call quaternion_print(2.*w)
    call quaternion_print(w*2.)
    u = quaternion(1,0,0,0)
    print *, quat_norm(u)
end program Quater
```

Programy XIII

derivatives.f90 - Pierwsze i drugie pochodne.

```
!  
! Derivatives 1, 2 in 1-dim  
!  
module derivatives  
  
CONTAINS  
  
subroutine FirstDeriv_1d(npts, dx, u, u_x)  
    implicit none  
    integer, intent(in) :: npts  
    real, intent(in) :: dx  
    real, dimension(:), intent(in) :: u  
    real, dimension(:), intent(out) :: u_x  
    real two_invdx  
    integer i  
    two_invdx = 1d0/(2d0*dx)  
    ! central...  
    do i=2,npts-1  
        u_x(i)=(u(i+1)-u(i-1))*two_invdx  
    end do
```

Program XIV

```
! forward...
u_x(1)=(-3.*u(1)+4.*u(2)-u(3))*two_invdx
! backward
u_x(npts)=(3.*u(npts)-4.*u(npts-1)+u(npts-2))*two_invdx
end subroutine FirstDeriv_1d

subroutine SecondDeriv_1d(npts, dx, u, u_xx)
implicit none
integer, intent(in) :: npts
real, intent(in) :: dx
real, dimension(:), intent(in) :: u
real, dimension(:), intent(out) :: u_xx
real inv_dx2
integer i
inv_dx2=1d0/(dx*dx)
! forward...
u_xx(1)=(2.*u(1)-5.*u(2)+4.*u(3)-u(4))*inv_dx2
! central...
do i=2,npts-1
    u_xx(i)=(u(i+1)-2.*u(i)+u(i-1))*inv_dx2
end do
! backward
u_xx(npts)=(2.*u(npts)-5.*u(npts-1)+4.*u(npts-2)-u(npts-3))*inv_dx2
end subroutine SecondDeriv_1d
```

Programy XV

```
end module derivatives
```

Programy XVI

TestDerivs.f90 - Pochodne. Test.

```
!      Test of Derivatives routines

program TestDerivs
use derivatives
implicit none
real func, func_x, func_xx
integer, parameter :: levels=10      ! liczba poziomow do testowania
real, parameter :: a=0d0              ! dolna granica przedzialu
real, parameter :: b=1d0              ! gorna granica przedzialu
real, dimension(:), allocatable :: u, u_x, u_xx
integer i, j, npts, iall
real dx, ux_error, ux_xx_error

write(*,'(a)') "      npts      Error(1_Der)      Error(2_Der)"
do i=2,levels+1,1
    npts = 2**i                      ! liczba punktow rowna jest 2^level
    dx = 1d0/(npts-1)                 ! ustaw dx na podstawie liczby punkow

    ! rezerwuj pamiec, dynamicznie
    allocate(u      (npts), stat=iall)
```

Programy XVII

```
allocate(u_x (npts), stat=iall)
allocate(u_xx(npts), stat=iall)

! function
do j=1,npts
    u(j) = func((j-1)*dx)
end do

call FirstDeriv_1d(npts, dx, u, u_x)
call SecondDeriv_1d(npts, dx, u, u_xx)

! error
ux_error = 0d0
uxx_error = 0d0
do j=1,npts
    ux_error = ux_error + dx*(u_x (j)-func_x ((j-1)*dx))**2
    uxx_error = uxx_error + dx*(u_xx(j)-func_xx((j-1)*dx))**2
end do

write(*,'(i8, 2e20.9)') npts, sqrt(ux_error), sqrt(uxx_error)

! zwolnij pamiec
deallocate(u, u_x, u_xx)
```

Programy XVIII

```
end do ! i

end program TestDerivs

real function func(x)
    func = x*x*x*x
end function func

real function func_x(x)
    func_x = 4d0*x*x*x
end function func_x

real function func_xx(x)
    func_xx = 12d0*x*x
end function func_xx

! wyniki obliczeń:
!
!      npts      Error(1_Der)      Error(2_Der)
!        4        0.448540793E+00   0.200411100E+01
!        8        0.696229028E-01   0.242946550E+00
!       16        0.130890098E-01   0.367216199E-01
!       32        0.276197408E-02   0.616467539E-02
!       64        0.627306127E-03   0.110691791E-02
```

Programy XIX

!	128	0.148910393E-03	0.211078793E-03
!	256	0.362347450E-04	0.428963548E-04
!	512	0.893428971E-05	0.929152239E-05
!	1024	0.221800198E-05	0.212429174E-05
!	2048	0.552552792E-06	0.504635577E-06

Programy XX

hello.f90 - Program demonstracyjny hello (Burkardt).

```
program main

! ****
!
!! MAIN is the main program for HELLO.
!
! Discussion:
!
! HELLO is a simple MPI test program.
!
! Each process prints out a "Hello, world!" message.
!
! The master process also prints out a short message.
!
! Licensing:
!
! This code is distributed under the GNU LGPL license.
!
! Modified:
```

Programmy XXI

```
!      30 October 2008
!
! Author:
!
!      John Burkardt
!
! Reference:
!
!      William Gropp, Ewing Lusk, Anthony Skjellum,
!      Using MPI: Portable Parallel Programming with the
!      Message-Passing Interface,
!      Second Edition,
!      MIT Press, 1999,
!      ISBN: 0262571323,
!      LC: QA76.642.G76.
!
!      use mpi
!
! implicit none
!
integer error
integer id
integer p
real ( kind = 8 ) wtime
```

Programy XXII

```
!
! Initialize MPI.
!
call MPI_Init ( error )
!
! Get the number of processes.
!
call MPI_Comm_size ( MPI_COMM_WORLD, p, error )
!
! Get the individual process ID.
!
call MPI_Comm_rank ( MPI_COMM_WORLD, id, error )
!
! Print a message.
!
if ( id == 0 ) then
    wtime = MPI_Wtime ( )
    write ( *, '(a)' ) ''
    write ( *, '(a)' ) 'HELLO_WORLD - Master process:'
    write ( *, '(a)' ) '  FORTRAN90 version'
    write ( *, '(a)' ) ''
    write ( *, '(a)' ) '  An MPI test program.'
```

Programy XXIII

```
write ( *, '(a)' ), '  
write ( *, '(a,i8)' ),  The number of processes is ', p  
write ( *, '(a)' ), '  
  
end if  
  
write ( *, '(a)' ), '  
write ( *, '(a,i8,a)' ),  Process ', id, ' says "Hello, world!"'  
  
if ( id == 0 ) then  
  
    write ( *, '(a)' ), '  
    write ( *, '(a)' ), 'HELLO_WORLD - Master process:  
    write ( *, '(a)' ), ' Normal end of execution: "Goodbye, world!".'  
  
    wtime = MPI_Wtime ( ) - wtime  
    write ( *, '(a)' ), '  
    write ( *, '(a,g14.6,a)' ),  Elapsed wall clock time = ', wtime, ' seconds  
  
end if  
!  
! Shut down MPI.  
!  
call MPI_Finalize ( error )
```

Programy XXIV

```
stop  
end
```

Programy XXV

FirstDeriv1dp.f90 - Pochodne. Wersja równoległa

```
!  
! Derivative 1, MPI  
!  
subroutine FirstDeriv1dp(npts, dx, u, u_x, mynode, totalnodes)  
    implicit none  
    integer, intent(in) :: npts, mynode, totalnodes  
    real*8, intent(in) :: dx  
    real*8, dimension(:), intent(in) :: u  
    real*8, dimension(:), intent(out) :: u_x  
    real*8 two_invdx  
    MPI_STATUS status  
    two_invdx = 1d0/(2d0*dx)  
  
    if(mynode == 0) then  
        ! forward...  
        u_x(1) = (-3.*u(1)+4.*u(2)-u(3))*two_invdx  
    end if  
  
    if(mynode == totalnodes) then  
        ! backward
```

Programy XXVI

```
    u_x(npts) = (3.*u(npts)-4.*u(npts-1)+u(npts-2))*two_invdx
end if

do i=2,npts-1
    ! central...
    u_x(i) = (u(i+1)-u(i-1))*two_invdx
end do

if (mynode == 0) then
    mpitemp = u(npts)
    call MPI_SEND(mpitemp, 1, MPI_DOUBLE, 1, 1, MPI_COMM_WORLD)
    call MPI_RECV(mpitemp, 1, MPI_DOUBLE, 1, 1, MPI_COMM_WORLD, status)
    u_x(npts) = (mpitemp-u(npts-1))*two_invdx
else if (mynode == totalnodes) then
    call MPI_RECV(mpitemp, 1, MPI_DOUBLE, mynode, 1, MPI_COMM_WORLD, status)
    u_x(1) = (u(2)-mpitemp)*two_invdx
    mpitemp = u(1)
    call MPI_SEND(mpitemp, 1, MPI_DOUBLE, mynode, 1, MPI_COMM_WORLD)
else
    call MPI_RECV(mpitemp, 1, MPI_DOUBLE, mynode, 1, MPI_COMM_WORLD, status)
    u_x(1) = (u(2)-mpitemp)*two_invdx
    mpitemp = u(1)
    call MPI_SEND(mpitemp, 1, MPI_DOUBLE, mynode-1, 1, MPI_COMM_WORLD)
    mpitemp = u(npts)
```

Programy XXVII

```
call MPI_SEND(mpitemp, 1, MPI_DOUBLE, mynode+1, 1, MPI_COMM_WORLD)
call MPI_RECV(mpitemp, 1, MPI_DOUBLE, mynode+1, 1, MPI_COMM_WORLD, status)
u_x(npts) = (mpitemp-u(npts-1))*two_invdx
end if
end subroutine FirstDeriv1dp
```

Programy XXVIII

FirstDeriv1dpTest.f90 - Pochodne. Test.

```
! przykład użycia procedur SENDRECV i SEND-NDRECV_REPLACE
!
integer mynode, totalnodes, mpierr
integer datasize ! liczba jednostek danych send/recv
integer process1, process2 ! rangi procesów wymieniających dane
integer tag1, tag2 ! znacznik komunikatu
real*8, dimension(:), allocatable :: buff, sendbuff, recvbuff
MPI_Status status ! zmienna przechowujaca informacje o stanie

call MPI_INIT( ierr )
call MPI_COMM_SIZE(MPI_COMM_WORLD, totalnodes, mpierr)
call MPI_COMM_RANK(MPI_COMM_WORLD, mynode, mpierr)

! rezerwacja buforow danych, process1, process2
allocate(sendbuff(datasize))
allocate(recvbuff(datasize))
allocate(buff(datasize))

if (mynode == process1) then
    ! dane w sendbuff są wysylane do process2, odbierane od process2
```

Programy XXIX

```
! dane trafiają do bufora recvbuff
call MPI_SENDRECV(sendbuff, datasize, MPI_DOUBLE, process2, &
    tag1, recvbuff, datasize, MPI_DOUBLE, process2, &
    tag2, MPI_COMM_WORLD, status)
! wywolanie powoduje wymiane (swap) zawartosci bufora buff
! z process2
call MPI_SENDRECV_REPLACE(buff, datasize, MPI_DOUBLE, process2, &
    tag1, process2, tag2, MPI_COMM_WORLD, status)
end if

if (mynode == process2) then
    ! zawartosc sendbuff jest przekazana do procesu process1, a dane
    ! trzymane od procesu process1 sa umieszczone w buforze recvbuff
    call MPI_SENDRECV(sendbuff, datasize, MPI_DOUBLE, process1, &
        tag2, recvbuff, datasize, MPI_DOUBLE, process1, &
        tag1, MPI_COMM_WORLD, status)
    ! wymiana danych buff z procesem process1
    !
    call MPI_SENDRECV_REPLACE(buff, datasize, MPI_DOUBLE, process1, &
        tag2, process1, tag1, MPI_COMM_WORLD, status)
end if

! process1 ma w swoim buforze recvbuff zawartosc bufora sendbuff
! procesu process1; process2 w swoim buforze recvbuff ma zawartosc
```

Programy XXX

! buforu sendbuff procesu process1; zawartosc buforow buff obu
! procesów zostala zamieniona

Programy XXXI

primes.f90 - Poszukiwanie liczb pierwszych

```
program primes
!
! Program zlicza liczby pierwsze w przedziale
! (kmin, kmax); podaje ich ilosc i czas zliczania
!
implicit none
integer, parameter :: kmin=1, kmax=1000
integer number0fPrimes, countPrimes
real*4 startTime, elapsedTime

! pomiar czasu
startTime=secnds(0.0)

number0fPrimes = countPrimes(kmin, kmax)
print *, number0fPrimes

! czas wykonania
elapsedTime=secnds(startTime) ! elapsed time
print *, "Time = ", elapsedTime
```

Programy XXXII

```
end program primes

function countPrimes(kmin, kmax) result(count)
!
! procedura zlicza liczby pierwsze w przedziale
! (kmin, kmax) i zwraca ich liczbe
!
implicit none
integer, intent(in) :: kmin, kmax
integer number, count
logical isPrime
count = 0
do number=kmin, kmax
    if (isPrime(number)) count = count + 1
end do
end function countPrimes

function isPrime(number)
!
! funkcja sprawdza, czy liczba jest pierwsza
! i zwraca .true. jesli jest lub .false.
!
```

Programy XXXIII

```
logical isPrime
integer, intent(in) :: number
integer k, limit

limit = int(sqrt(float(number)))+1
isPrime = .true.
do k=2, limit
    if (mod(number,k) == 0) then
        isPrime = .false.
        return
    end if
end do
end function isPrime
```

Programy XXXIV

matvec.f90 - Mnożenie macierzy przez wektor

```
! MPI Tutorial
! Dr. Andrew C. Pineda, HPCERC/AHPCC
! Dr. Brian Smith, HPCERC/AHPCC
! The University of New Mexico
! November 17, 1997
! Last Revised: September 18, 1998

program matvec2
  ! Perform matrix vector product -- Y = AX
  ! This is method two -- distribute A by block columns
  ! and X in blocks (of rows) and the partial vector sum of Y is on
  ! each processor.
  include 'mpif.h'
  integer, parameter :: dim1 = 80, dim2 = 10, dim3 = dim1*dim2
  integer ierr, rank, size, root, i, j
  integer sec_start, nano_start
  integer sec_curr, nano_curr
  integer sec_startup, nano_startup
  integer sec_comp, nano_comp
  integer sec_cleanup, nano_cleanup
```

Programm XXXV

```
real, dimension(dim1,dim1) :: a
real, dimension(dim1,dim2) :: apart
real, dimension(dim1) :: x, y, ypart
real, dimension(dim2) :: xpart
interface
    subroutine posix_timer(job_sec, job_nanosec)
        integer job_sec, job_nanosec
    end subroutine posix_timer
end interface
root = 0
call MPI_INIT( ierr )
call MPI_COMM_RANK( MPI_COMM_WORLD, rank, ierr )
call MPI_COMM_SIZE( MPI_COMM_WORLD, size, ierr )
print *, 'START process on processor ', rank
if( rank == root ) then
    call posix_timer(sec_start, nano_start)
    do i = 1, dim1
        x(i) = 1.0
        do j = 1, dim1
            a(j,i) = i + j
        enddo
    enddo
endif
! Distribute the 80x80 array A by columns as
```

Programm XXXVI

```
! 80x10 blocks stored in APART.  
! Distribute the 80 dimensional  
! array x in blocks of length 10  
call MPI_SCATTER( a, dim3, MPI_REAL, apart, dim3, MPI_REAL, root,&  
    & MPI_COMM_WORLD, ierr )  
call MPI_SCATTER( x, dim2, MPI_REAL, xpart, dim2, MPI_REAL, root,&  
    & MPI_COMM_WORLD, ierr )  
if( rank == root ) then  
    call posix_timer(sec_curr, nano_curr)  
    sec_startup = sec_curr - sec_start  
    nano_startup = nano_curr - nano_start  
    sec_start = sec_curr  
    nano_start = nano_curr  
endif  
do j = 1, dim1  
    ypart(j) = 0.0  
enddo  
do i = 1, dim2  
    do j = 1, dim1  
        ypart(j) = ypart(j) + xpart(i)*apart(j,i)  
    enddo  
enddo  
if( rank == root ) then  
    call posix_timer(sec_curr, nano_curr)
```

Programy XXXVII

```
sec_comp = sec_curr - sec_start
nano_comp = nano_curr - nano_start
sec_start = sec_curr
nano_start = nano_curr
endif
call MPI_REDUCE( ypart, y, dim1, MPI_REAL, MPI_SUM, root, &
    MPI_COMM_WORLD, ierr )
if( rank == root ) then
    call posix_timer(sec_curr, nano_curr)
    sec_cleanup = sec_curr - sec_start
    nano_cleanup = nano_curr - nano_start
endif
print *, 'Finish processor ', rank
if( rank == root ) then
    print *, 'Matrix vector product, elements 10 and 60, are: ',&
        & y(10), y(60)
    print *, 'Startup execution times (sec, nano): ',&
        & sec_startup, nano_startup
    print *, 'Computation execution times (sec, nano): ',&
        & sec_comp, nano_comp
    print *, 'Cleanup execution times (sec, nano): ',&
        & sec_cleanup, nano_cleanup
endif
call MPI_FINALIZE( ierr )
```

Programy XXXVIII

```
end program matvec2
```

Programy XXXIX

gausselim.f90 - Metoda Gaussa eliminacjii

```
! MPI Tutorial
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! The University of New Mexico
! November 17, 1997
! Last Revised: September 18, 1998

module GaussianSolver
    implicit none

    ! The default value for the smallest pivot that will be accepted
    ! using the GaussianSolver subroutines. Pivots smaller than this
    ! threshold will cause premature termination of the linear equation
    ! solver and return false as the return value of the function.
    real, parameter :: DEFAULT_SMALLEST_PIVOT = 1.0e-6

contains

    ! Use Gaussian elimination to calculate the solution to the linear
    ! system, A x = b. No partial pivoting is done. If the threshold
```

Programm XL

```
! argument is present, it is used as the smallest allowable pivot
! encountered in the computation; otherwise, DEFAULT_SMALLEST_PIVOT,
! defined in this module, is used as the default threshold. The status
! of the computation is a logical returned by the function indicating
! the existence of a unique solution (.true.), or the nonexistence of
! a unique solution or threshold passed (.false.).
! Note that this is an inappropriate method for some linear systems.
! In particular, the linear system, M x = b, where M = 10e-12 I, will
! cause this routine to fail due to the presence of small pivots.
! However, this system is perfectly conditioned, with solution x = b.
function gaussianElimination( A, b, x, threshold )
    implicit none
    logical gaussianElimination
    real, dimension( :, : ), intent( in ) :: A ! Assume the shape of A.
    real, dimension( : ), intent( in ) :: b ! Assume the shape of b.
    real, dimension( : ), intent( out ) :: x ! Assume the shape of x.
    ! The optional attribute specifies that the indicated argument 40
    ! is not required to be present in a call to the function. The
    ! presence of optional arguments, such as threshold, may be checked
    ! using the intrinsic logical function, present (see below).
    real, optional, intent( in ) :: threshold
    integer i, j ! Local index variables.
    integer N ! Order of the linear system.
    real m ! Multiplier.
```

Program XLI

```
real :: smallestPivot = DEFAULT_SMALLEST_PIVOT
! Pointers to the appropriate rows of the matrix during the elmination.
real, dimension( : ), pointer :: pivotRow
real, dimension( : ), pointer :: currentRow
! Copies of the input arguments. These copies are modified during
! the computation. The target attribute is used to indicate that
! the specified variable may be the target of a pointer. Rows of
! ACopy are targets of pivotRow and currentRow, defined above.
real, dimension( size( A, 1 ), size( A, 2 ) ), target :: ACopy
real, dimension( size( b ) ) :: bCopy
!
! Status of the computation. The return value of the function.
!
logical successful

!
! Change the smallestPivot if the threshold argument was included.
!
if ( present( threshold ) ) smallestPivot = abs( threshold )
!
! Setup the order of the system by using the intrinsic function size.
! size returns the number of elements in the specified dimension of
! an array or the total number of elements if the dimension is not
! specified. Also assume that a unique solution exists initially.
```

Program XLII

```
!  
N = size( b )  
ACopy = A  
bCopy = b  
successful = .true.  
!  
! Begin the Gaussian elimination algorithm. Note the use of array  
! sections in the following loops. These eliminate the need for  
! many do loops that are common in Fortran 77 code. Pointers are  
! also used below and enhance the readability of the elimination  
! process. Begin with the first row.  
!  
i = 1  
! Reduce the system to upper triangular.  
do while ( ( successful ) .and. ( i < N ) )  
!  
! The following statement is called pointer assignment and uses  
! the pointer assignment operator '=>'. This causes pivotRow  
! to be an alias for the ith row of ACopy. Note that this does  
! not cause any movement of data.  
! Assign the pivot row.  
!  
pivotRow => ACopy( i, : )  
!
```

Programm XLIII

```
! Verify that the current pivot is not smaller than smallestPivot.  
!  
successful = abs( pivotRow( i ) ) >= smallestPivot  
if ( successful ) then  
!  
    ! Eliminate the entries in the pivot column below the pivot row.  
!  
    do j = i+1, N  
        ! Assign the current row.  
        currentRow => ACopy( j, : )  
        ! Calculate the multiplier.  
        m = currentRow( i ) / pivotRow( i )  
        ! Perform the elimination step on currentRow and right  
        ! hand side, bCopy.  
        currentRow = currentRow - m * pivotRow  
        bCopy( j ) = bCopy( j ) - m * bCopy( i )  
    enddo  
endif  
! Move to the next row.  
i = i + 1  
end do  
! Check the last pivot.  
pivotRow => ACopy( N, : )  
if ( successful ) successful = abs( pivotRow( N ) ) >= smallestPivot
```

Programm XLIV

```
if ( successful ) then
    do i = N, 2, -1 ! Backward substitution.
        ! Determine the ith unknown, x( i ).
        x( i ) = bCopy( i ) / ACopy( i, i )
        ! Substitute the now known value of x( i ), reducing the order of
        ! the system by 1.
        bCopy = bCopy - x( i ) * ACopy( :, i )
    enddo
endif
! Determine the value of x( 1 ) as a special case.
if ( successful ) x( 1 ) = bCopy( 1 ) / ACopy( 1, 1 )
! Prepare the return value of the function.
gaussianElimination = successful
end function gaussianElimination
```

```
! Output A in Matlab format, using name in the Matlab assignment statement.
subroutine printMatrix( A, name )
    implicit none
    real, dimension( :, : ) :: A ! Assume the shape of A.
    character name ! Name for use in assignment, ie, name =
    ! .....
    integer n, m, i, j
    n = size( A, 1 )
    m = size( A, 2 )
```

Programy XLV

```
write( *, fmt="(a1,a5)", advance = "no" ) name, ' = [ ,
! Output the matrix, except for the last row, which needs no ';'.
do i = 1, n-1
    ! Output current row.
    do j = 1, m-1
        write( *, fmt="(f10.6,a2)", advance = "no" ) A( i, j ), ', '
    enddo
    ! Output last element in row and end current row.
    write( *, fmt="(f10.6,a1)" ) A( i, m ), ';'
enddo
! Output the last row.
do j = 1, m-1
    write( *, fmt="(f10.6,a2)", advance = "no" ) A( i, j ), ', '
enddo
! Output last element in row and end.
write( *, fmt="(f10.6,a1)" ) A( i, m ), ']'
end subroutine printMatrix

! Output b in Matlab format, using name in the Matlab assignment statement.
subroutine printVector( b, name )
implicit none
real, dimension( : ) :: b ! Assume the shape of b.
character name ! Name for use in assignment, ie, name = .....
integer n, i
```

Programy XLVI

```
n = size( b )
write( *, fmt="(a1,a5)", advance = "no" ) name, ' = [ ,
do i = 1, n-1
    write( *, fmt = "(f10.6,a2)", advance = "no" ) b( i ), ', '
enddo
write( *, fmt = "(f10.6,a2)" ) b( n ), ']',
end subroutine printVector
end module GaussianSolver
```

```
! A program to solve linear systems using the GaussianSolver module.
program SolveLinearSystem
    ! Include the module for the various linear solvers.
    use GaussianSolver
    implicit none
    integer, parameter :: N = 5 ! Order of the linear system.
    real, parameter :: TOO_SMALL = 1.0e-7 ! Threshold for pivots.
    ! Declare the necessary arrays and vectors to solve the linear system
    ! A x = b.
    real, dimension( N, N ) :: A ! Coefficient matrix.
    real, dimension( N ) :: x, b ! Vector of unknowns, and right hand side.
    real, dimension( N, N ) :: LU ! Matrix for LU factorization of A.
    logical successful ! Status of computations.
```

Program XLVII

```
! The intrinsic subroutine, random_number, fills a real array or scalar,
! with uniformly distributed random variates in the interval [0,1).
call random_number( A ) ! Initialize the coefficient matrix.
call random_number( b ) ! Initialize the right-hand side.

! Output the matrix in Matlab format for ease of checking the solution.
call printMatrix( A, 'A' )
call printVector( b, 'b' )

! Use Gaussian elimination to calculate the solution of the linear system.
! The call below uses the default threshold specified in the
! GaussianSolver module by omitting the optional argument.
successful = gaussianElimination( A, b, x )
print *, '=====',
print *, 'Gaussian Elimination:',
print *, '-----',
if ( successful ) then
    call printVector( x, 'x' )
    print *, 'Infinity Norm of Difference = ', &
              maxval( abs( matmul( A, x ) - b ) )
else
    print *, 'No unique solution or threshold passed.'
endif
```

Programy XLVIII

```
end program SolveLinearSystem
```

Programy XLIX

m-w.f90 - Model master-slave

```
PROGRAM MASTER_WORKER
USE MPI
INTEGER istatus(MPI_STATUS_SIZE)
PARAMETER (njobmx=124)
!
CALL MPI_INIT(ierr)
CALL MPI_COMM_SIZE(MPI_COMM_WORLD,nprocs,ierr)
CALL MPI_COMM_RANK(MPI_COMM_WORLD,myrank,ierr)

!=====  MASTER
!
! The master receives the messages from workers and if some worker
! is idle it sends to it a job number. the worker realizes this
! job and sends the message again to the master. If all jobs are
! processed then if the worker has finished the master sends the
! term signal (job=-1) to the worker and the worker exits.
!
IF (myrank == 0) THEN
```

Programy L

```
itag=1
DO njob=1,njobmx
    CALL MPI_RECV(iwk, 1, MPI_INTEGER, MPI_ANY_SOURCE,  &
                  itag, MPI_COMM_WORLD, istatus, ierr)
    idest=istatus(MPI_SOURCE)
    CALL MPI_SEND(njob, 1, MPI_INTEGER, idest,  &
                  itag, MPI_COMM_WORLD, ierr)
END DO

DO i=1,nprocs-1
    CALL MPI_RECV(iwk, 1, MPI_INTEGER, MPI_ANY_SOURCE,  &
                  itag, MPI_COMM_WORLD, istatus, ierr)
    idest=istatus(MPI_SOURCE)
    CALL MPI_SEND(-1, 1, MPI_INTEGER, idest,  &
                  itag, MPI_COMM_WORLD, ierr)
END DO

ELSE

!===== WORKER
!
! The worker sends the signal to the master that it is idle.
! if there are jobs to process then the master sends to the
! worker the job number (njob) and the worker processes the job.
```

Programm LI

```
! If there are no other jobs the number njob sent to the worker
! is equal to -1 and after receiving it the worker exits.
```

```
itag=1
iwk=0

DO
    CALL MPI_SEND(iwk, 1, MPI_INTEGER, 0,  &
                  itag, MPI_COMM_WORLD, ierr)
    CALL MPI_RECV(njob, 1, MPI_INTEGER, 0,  &
                  itag, MPI_COMM_WORLD, istatus, ierr)
    IF (njob == -1) EXIT

    CALL DOSOMETHING(njob)

END DO
!
CALL MPI_FINALIZE(ierr)

END IF

END PROGRAM MASTER
```

Programy LII

```
SUBROUTINE DOSOMETHING(JOB)
```

```
!
```

```
! MAIN JOB
```

```
!
```

```
END SUBROUTINE DOSOMETHING
```

Programy LIII

rwalk.f90 - Random walk, Monte Carlo method; wersja sekwencyjna

```
! RS6000 SP: Practical MPI programming
PROGRAM randomwalk
PARAMETER (n = 10000)
INTEGER itotal(0:9)
REAL seed
pi = 3.1415926
DO i = 0, 9
    itotal(i) = 0
END DO

! Uwaga: zalezy od kompilatora
! tutaj: gfortran
iseed = 5
CALL srand(iseed)
DO i = 1, n
    x = 0.0
    y = 0.0
    DO istep = 1, 10
        angle = 2.0 * pi * rand()
        x = x + cos(angle)
```

Programy LIV

```
y = y + sin(angle)
END DO
itemp = sqrt(x*x + y*y)
itotal(itemp) = itotal(itemp) + 1
END DO
PRINT *, "total =", itotal
END PROGRAM randomwalk
```

Programy LV

rwalk-p.f90 - Random walk, Monte Carlo method; w. równoległa

```
! RS6000 SP: Practical MPI programming
PROGRAM randomwalk_p
INCLUDE "mpif.h"

PARAMETER (n = 100000)
INTEGER itotal(0:9), iitotal(0:9)
REAL seed

CALL MPI_INIT(ierr)
CALL MPI_COMM_SIZE(MPI_COMM_WORLD, nprocs, ierr)
CALL MPI_COMM_RANK(MPI_COMM_WORLD, myrank, ierr)

CALL para_range(1, n, nprocs, myrank, ista, iend)
pi = 3.1415926

DO i = 0, 9
    itotal(i) = 0
END DO

! Uwaga: zalezy od kompilatora
```

Programy LVI

```
! tutaj: gfortran
seed = 5 + myrank
CALL srand(seed)
DO i = ista, iend
    x = 0.0
    y = 0.0
    DO istep = 1, 10
        angle = 2.0 * pi * rand()
        x = x + cos(angle)
        y = y + sin(angle)
    END DO
    itemp = sqrt(x**2 + y**2)
    itotal(itemp) = itotal(itemp) + 1
END DO

CALL MPI_REDUCE(itotal, iitotal, 10, MPI_INTEGER, MPI_SUM, 0, &
MPI_COMM_WORLD, ierr)

PRINT *, "total =", iitotal

CALL MPI_FINALIZE(ierr)
END
```

Programy LVII

```
SUBROUTINE para_range(n1, n2, nprocs, irank, ista, iend)
    iwork1 = (n2 - n1 + 1) / nprocs
    iwork2 = MOD(n2 - n1 + 1, nprocs)
    ista = irank * iwork1 + n1 + MIN(irank, iwork2)
    iend = ista + iwork1 - 1
    IF (iwork2 > irank) iend = iend + 1
END SUBROUTINE para_range
```

Programy LVIII

BlasEx.f - Przykłady użycia biblioteki BLAS

Example

```
implicit real*8 (a-h,o-z)
parameter(maxn=200,m=80,k=maxn+1)
parameter(zero=0.0d0,one=1.0d0)
real*8 a(k,maxn),aa(k,maxn),x(k,m),b(k,m)
integer ip(maxn)
```

C =====

C Define the matrix

C =====

```
n=maxn
call inita(a,k,n)
do i=1,n
    do j=1,n
        aa(j,i)=a(j,i)
    end do
end do
```

C =====

C LU decomposition

C =====

```
c all dgetrf(n,n,a,k,ip,info)
```

Programy LIX

```
C =====
C Define the vectors
C =====
do jm=1,m
    do jn=1,n
        x(jn,jm)=jn+jm
    end do
end do
call dgemm('N','N',n,m,n,one,aa,k,x,k,zero,b,k)
C =====
C Solution
C =====
call dgetrs('N',n,m,a,k,ip,b,k,info)
if(info.ne.0) then
    write(6,*) 'error in dgetrs info = ',info
    stop
end if
C =====
C Check result
C =====
call check(a, b, k, n, m)

end
```

Programy LX

wsad1 - ...

```
#!/bin/sh
# plik wsad1
# praca w srodowisku Xeon, gondor; plik PBS
# obliczenia sekwencyjne
#PBS -S /bin/sh
#PBS -N nazwa
#PBS -l walltime=10:00:00
#PBS -l mem=4GB
#PBS -l ncpus=1
#
export OMP_NUM_THREADS=1
cd /home/uzytkownik/katalog
./prog < input > output
```

Programy LXI

wsad2 - ...

```
#!/bin/sh
# plik wsad2
# OpenMP lub BLAS3 z MKL - xeony
#
#PBS -S /bin/sh
#PBS -N ichox
#PBS -l walltime=10:00:00
#PBS -l mem=4GB
#PBS -l ncpus=X
#PBS -l nodes=1:ppn=X
#
export OMP_NUM_THREADS=X
cd /home/uzytkownik/katalog
./prog < input > output
```

Programy LXII

wsad3 - ...

```
#!/bin/sh
# plik wsad3
# MPI - xeony
#
#PBS -S /bin/sh
#PBS -N ntrs
#PBS -l walltime=10:00:00
#PBS -l mem=10GB
#PBS -l nodes=2:ppn=8
#
cd /home/uzytkownik/katalog
source /opt/bin/intel64
export OMP_NUM_THREADS=1
mpirun -env I_MPI_DEVICE ssm -ppn 8 -n 16 ./ntrs < input > output
```

Programy LXIII

wsad4 - ...

```
#!/bin/sh
# plik wsad4
# wezel ROHAN, rohan
#
#PBS -S /bin/sh
#PBS -N testowe
#PBS -l mem=1GB
#PBS -l nodes=x:itanium:ppn=2
source /opt/bin/ia64
```

Programy LXIV

Makefile.ex - Przykładowy plik Makefile

```
PROG2    = ntrs
FILES2   = blt.f loca.f
LDLIBS   = -L/opt/intel/mkl/10.2.2.025/lib/em64t -lmkl_scalapack_lp64 \
           -lmkl_blacs_intelmpi_lp64 -lmkl_intel_thread -lmkl_intel_lp64 \
           -lmkl_core -liomp5 -lpthread
OPTFLG   = -O3 -xT -openmp -parallel
all:
    mpiifort $(OPTFLG) -o $(PROG2) $(FILES2) $(LDLIBS)
clean:
    rm -f core *.o
```

Programy LXV