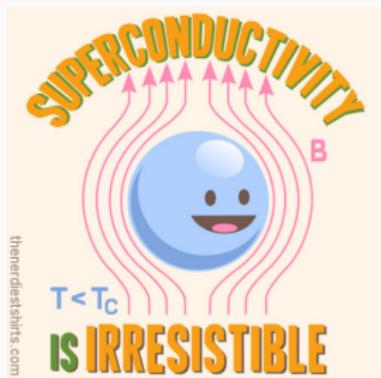


DELOCALISATION OF MAJORANA MODES IN LOW-DIMENSIONAL HYBRIDS

Tadeusz DOMAŃSKI

M. Curie-Skłodowska University, Lublin (Poland)



theredeastshifts.com

"New³SC – 12"

Oxford (UK), 31 March - 5 April 2019

OUTLINE

Superconductivity in low dim systems:

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- dim=0
bound states (Yu-Shiba-Rusinov & Andreev)

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- dim=0
bound states (Yu-Shiba-Rusinov & Andreev)
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topological phase (Majorana qps)
- hybrid structures: 1 + 2 dim
delocalized Majorana qps (itinerant modes?)

BASIC IDEA

Nanoscopic (finite-size) objects, like:

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- ⇒ magnetic atoms (for instance Fe, Co)
 - ⇒ correlated quantum dots (Anderson-type impurities)
 - ⇒ molecules (multi-level or vibrating)
 - ⇒ magnetic islands (Shiba glasses and/or lattices)
 - ⇒ nanowires (carbon nanotubes, Fe-chains)
- etc.

existing in bulk or on surface of superconducting materials

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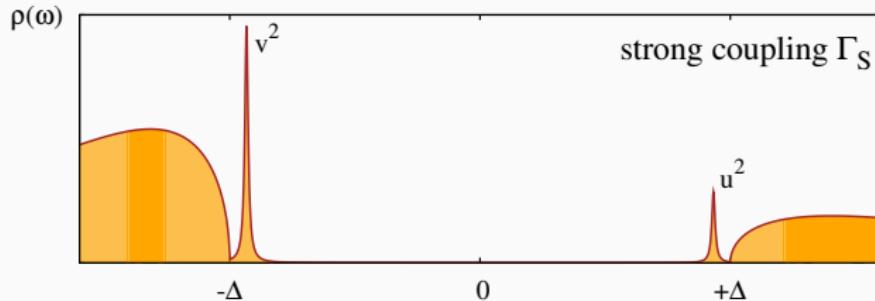
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acquire the electron pairing via *proximity effect*.

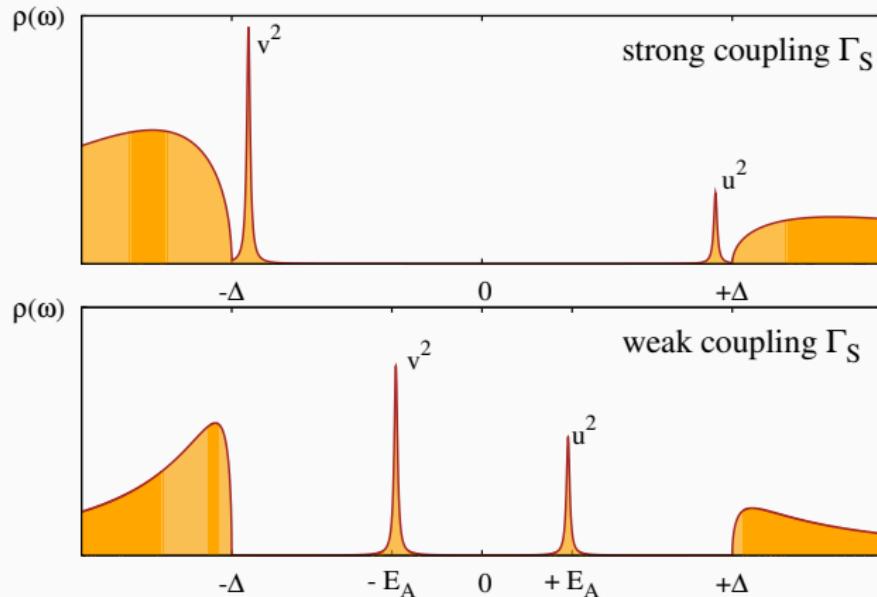
IN-GAP STATES

Spectrum of an uncorrelated impurity coupled to superconductor:



IN-GAP STATES

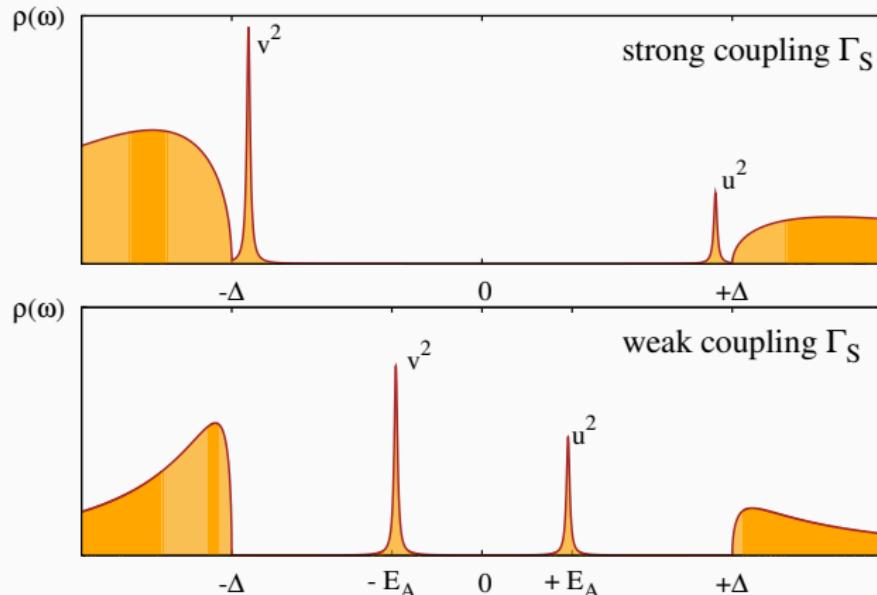
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Bound states appearing in the subgap region $E \in \langle -\Delta, \Delta \rangle$

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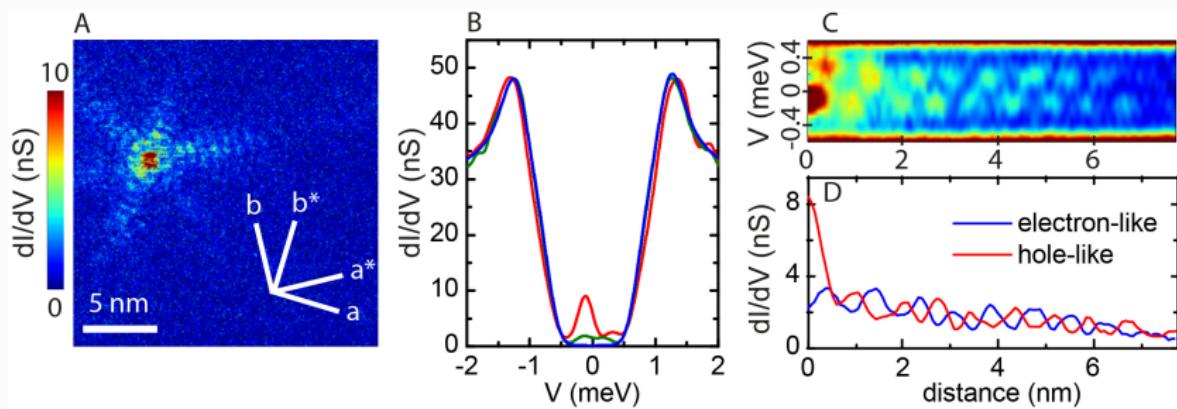
Spectrum of an uncorrelated impurity coupled to superconductor:



Bound states appearing in the subgap region $E \in (-\Delta, \Delta)$
are dubbed **Yu-Shiba-Rusinov (or Andreev) quasiparticles**.

TOPOGRAPHY AND SPATIAL EXTENT

Empirical data obtained from STM measurements for NbSe₂

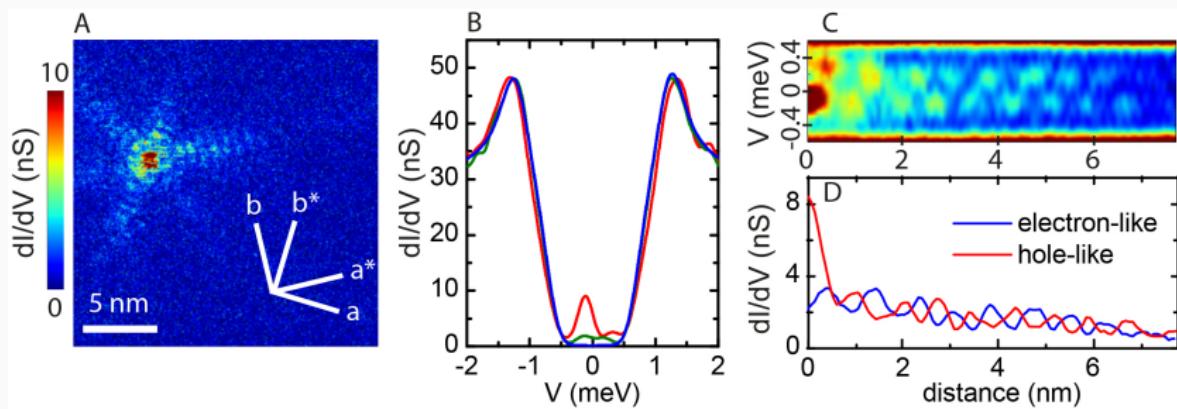


- a) bound states extending to 10 nm
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G.C. Menard et al., Nature Phys. 11, 1013 (2015).

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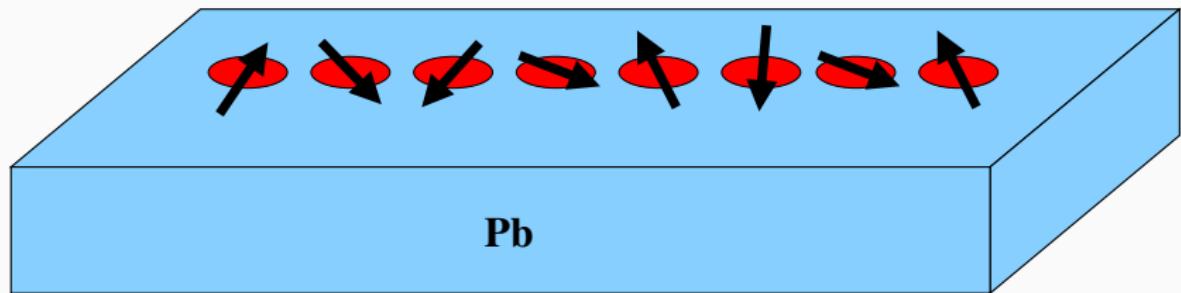
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G.C. Menard et al., Nature Phys. 11, 1013 (2015).

A. Ptok, Sz. Głodzik and T. Domański, Phys. Rev. B 96, 184425 (2017).

MAGNETIC CHAINS IN SUPERCONDUCTORS

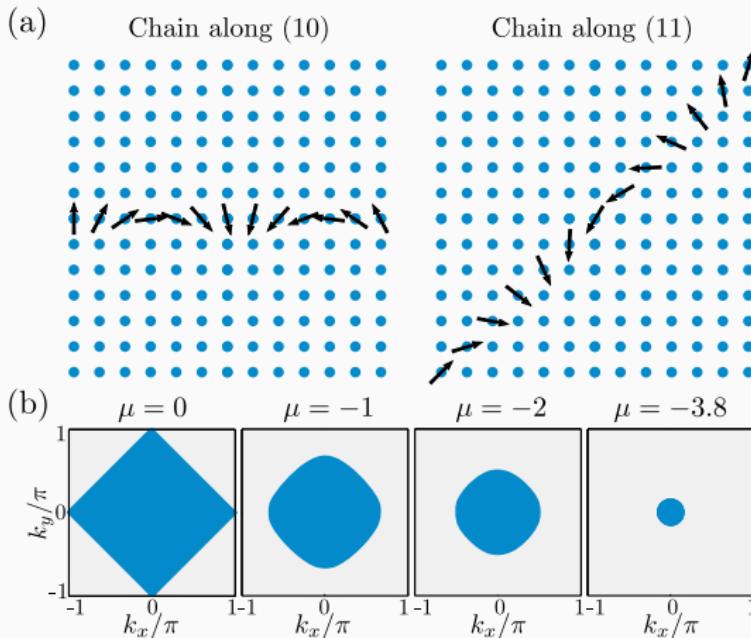
Nanochain of magnetic impurities embedded in superconductor:



T.-P. Choy, J.M. Edge, A.R. Akhmerov, and C.W.J. Beenakker,
Phys. Rev. B 84, 195442 (2011).

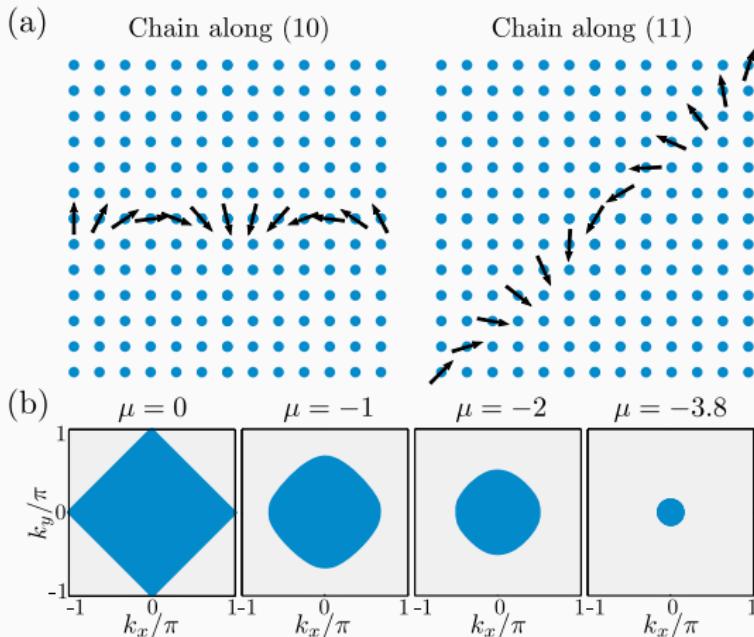
MAGNETIC CHAINS IN SUPERCONDUCTORS

Nanochain of magnetic impurities embedded in superconductor:



MAGNETIC CHAINS IN SUPERCONDUCTORS

Nanochain of magnetic impurities embedded in superconductor:



arrange the in-gap bound states into Shiba-band(s).

M.H. Christensen ... J. Paaske, Phys. Rev. B 94, 144509 (2016).

KITAEV CHAIN: PARADIGM FOR MAJORANA QPS

Itinerant 1D fermions with intersite (*p*-wave) pairing

$$\hat{H} = t \sum_i \left(\hat{c}_i^\dagger \hat{c}_{i+1} + \text{h.c.} \right) - \mu \sum_i \hat{c}_i^\dagger \hat{c}_i + \Delta \sum_i \left(\hat{c}_i^\dagger \hat{c}_{i+1}^\dagger + \text{h.c.} \right)$$

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This toy-model can be **recast** in the Majorana basis

$$\begin{aligned}\hat{\gamma}_{j,1} &\equiv \frac{1}{\sqrt{2}} \left(\hat{c}_j + \hat{c}_j^\dagger \right) \\ \hat{\gamma}_{j,2} &\equiv \frac{1}{i\sqrt{2}} \left(\hat{c}_j - \hat{c}_j^\dagger \right)\end{aligned}$$

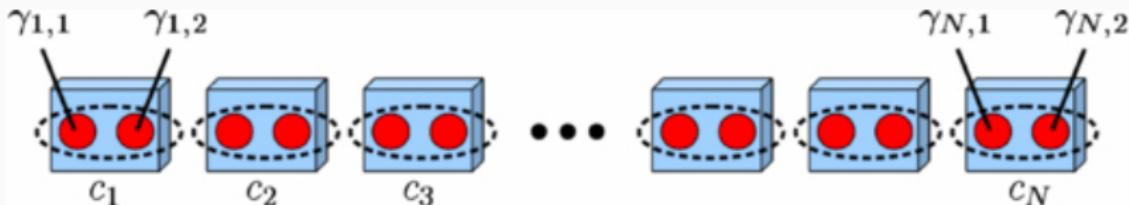
KITAEV CHAIN: PARADIGM FOR MAJORANA QPS

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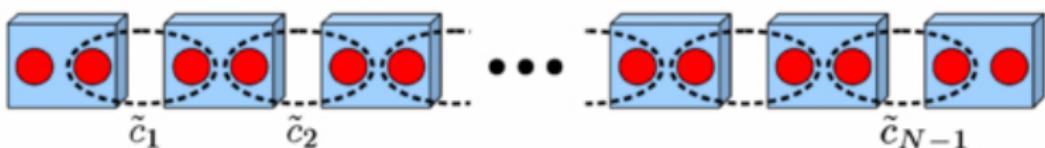
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Yu. Kitaev, Phys. Usp. 44, 131 (2001).

KITAEV CHAIN: PARADIGM FOR MAJORANA QPS

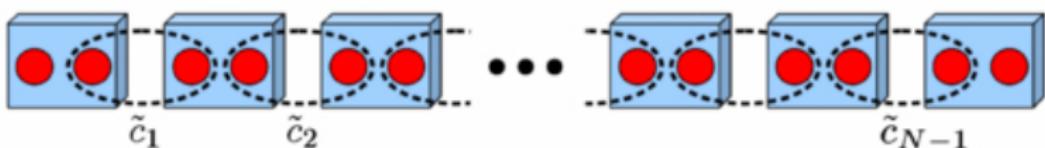
In particular, for $\Delta = t$ and when $|\mu|$ is inside the band
two operators $\hat{\gamma}_{1,1}$ and $\hat{\gamma}_{2,N}$ *decouple* from all the rest



inducing the zero-energy modes at the chain edges.

KITAEV CHAIN: PARADIGM FOR MAJORANA QPS

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They can be regarded as *fractions* of non-local fermion

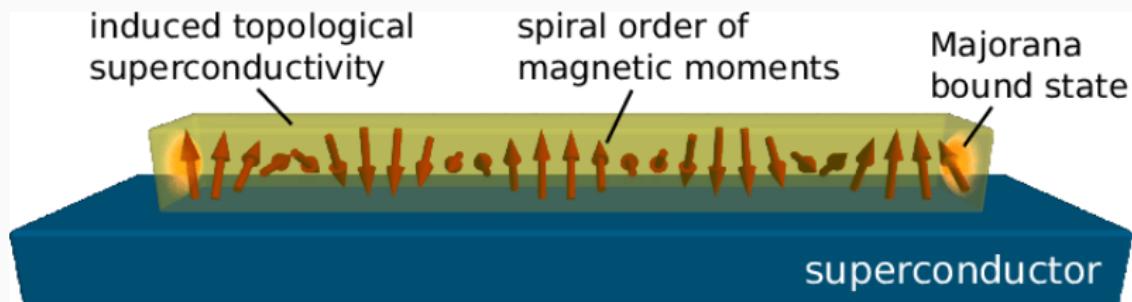
$$\hat{c}_{nonlocal} \equiv (\hat{\gamma}_{1,1} + i\hat{\gamma}_{N,2}) / \sqrt{2}$$

$$\hat{c}_{nonlocal}^\dagger \equiv (\hat{\gamma}_{1,1} - i\hat{\gamma}_{N,2}) / \sqrt{2}$$

as manifested by a number of unique phenomena.

MAGNETIC CHAINS IN SUPERCONDUCTORS

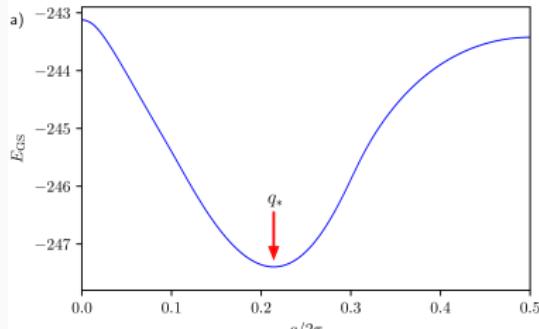
Topological superconductivity can be driven e.g. by the spin-orbit Rashba interaction combined with the external magnetic field.



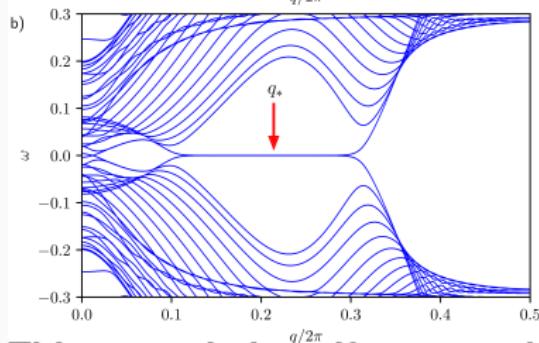
R. Lutchyn, J. Sau, S. Das Sarma, Phys. Rev. Lett. 105, 077001 (2010).

Y. Oreg, G. Refael, F. von Oppen, Phys. Rev. Lett. 105, 177002 (2010).

MAGNETIC CHAINS IN SUPERCONDUCTORS



Ground state energy
vs the pitch vector q

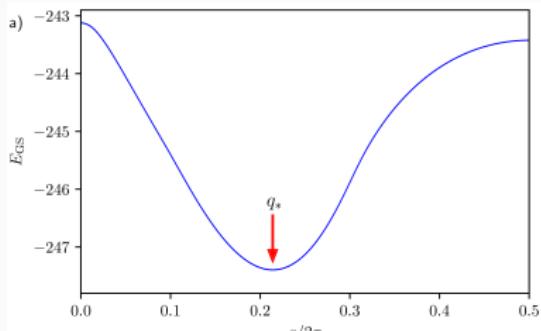


In-gap Shiba states

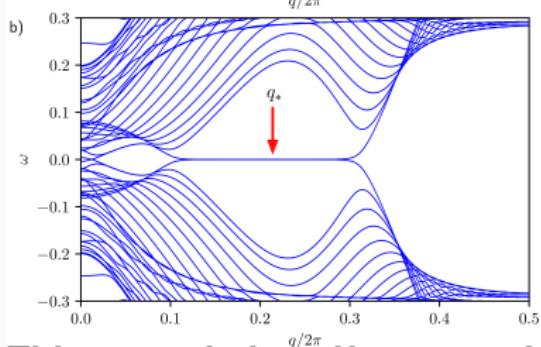
This nanochain self-tunes to its *topological phase (topofilia)*

A. Gorczyca-Goraj, T. Domański & M.M. Maśka, arXiv:1902.1902.06750.

MAGNETIC CHAINS IN SUPERCONDUCTORS



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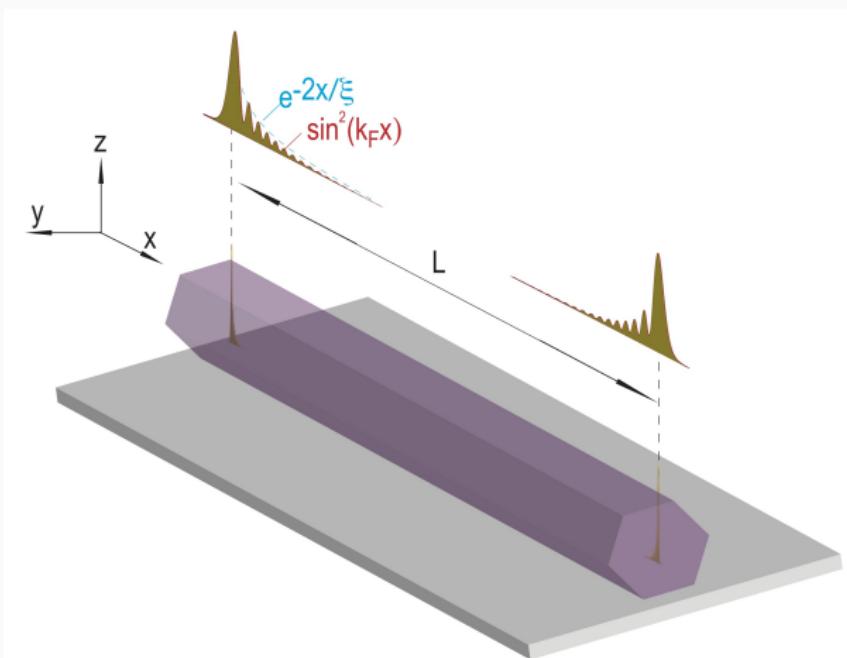
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/ details provided in the lecture by Maciek Maśka /

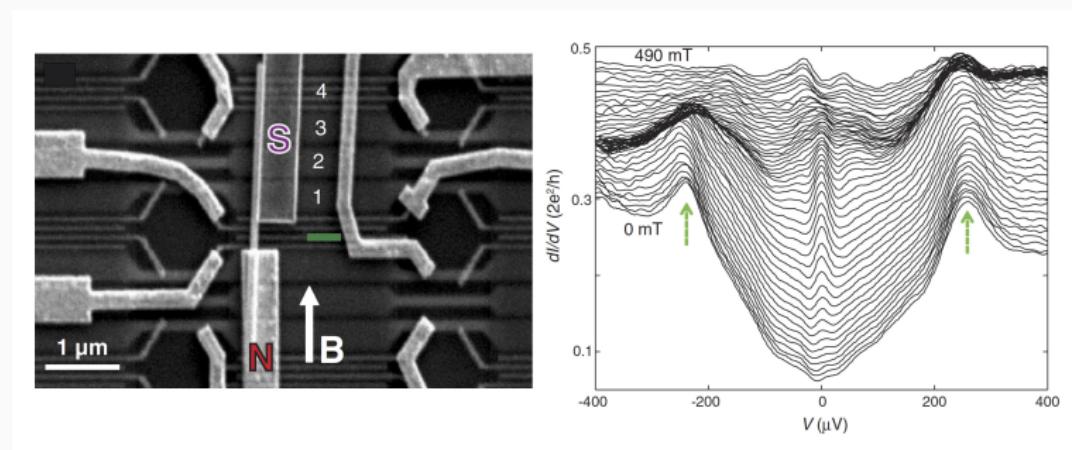
SPATIAL PROFILE OF MAJORANA QPS

Majorana qps are exponentially localized at the edges



EMPIRICAL REALIZATION: EXAMPLE # 1

Differential conductance dI/dV obtained for InSb nanowire at 70 mK upon varying a magnetic field.

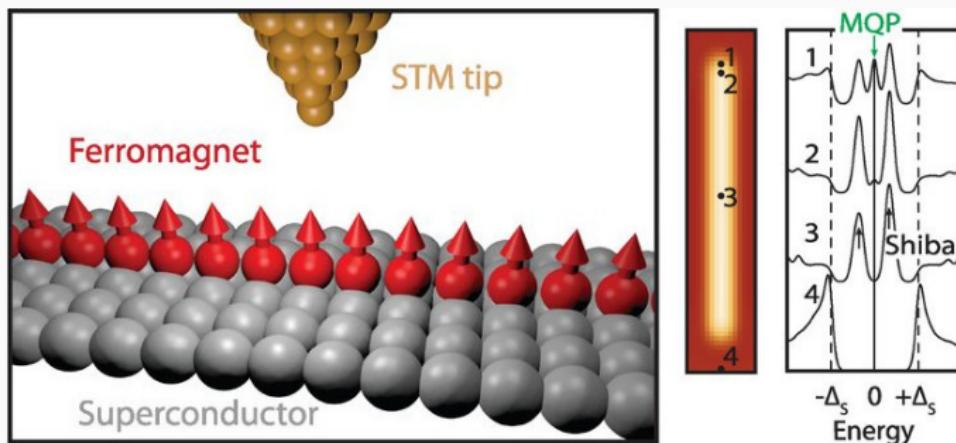


V. Mourik, ..., and L.P. Kouwenhoven, Science **336**, 1003 (2012).

/ Technical Univ. Delft, Netherlands /

EMPIRICAL REALIZATION: EXAMPLE # 2

STM measurements for the nanochain of Fe atoms self-organized on a surface of superconducting Pb.

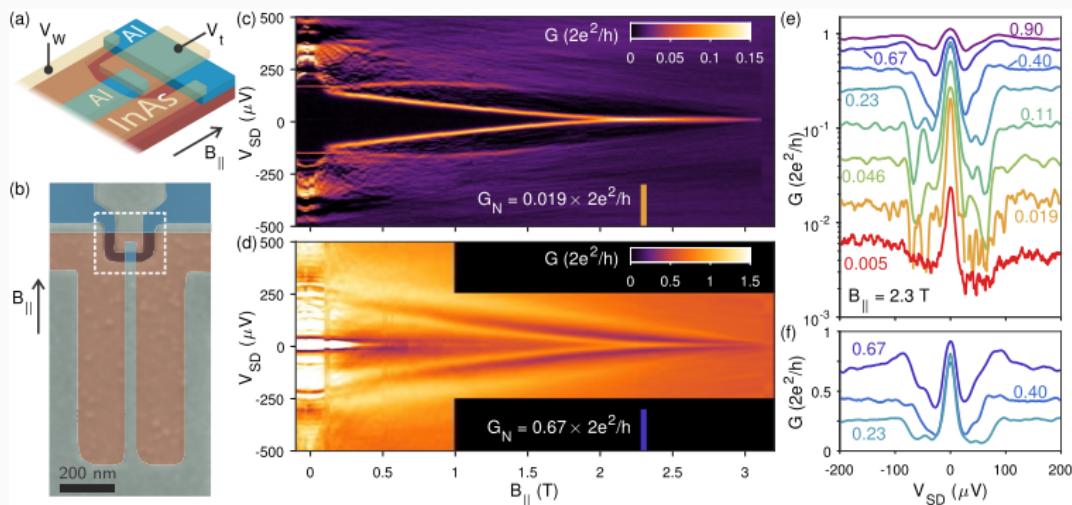


S. Nadj-Perge, ..., and A. Yazdani, Science **346**, 602 (2014).

/ Princeton University, USA /

EMPIRICAL REALIZATION: EXAMPLE # 3

Results for the lithographically fabricated Al nanowire

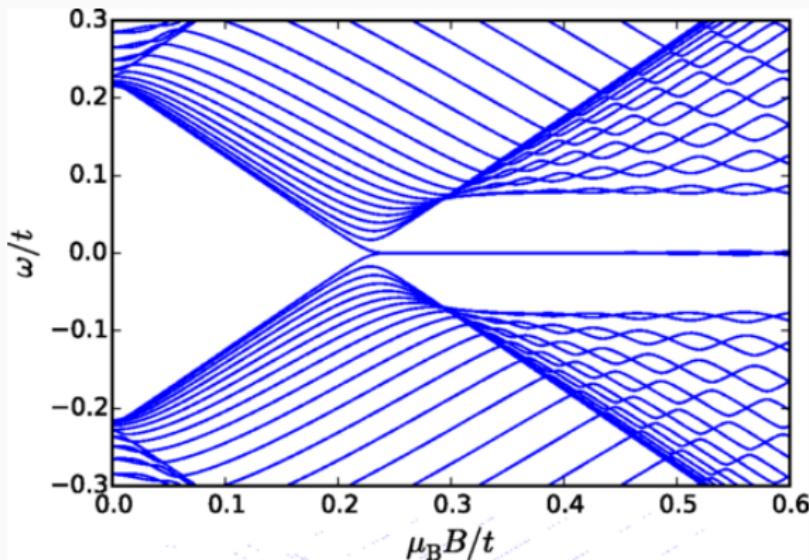


F. Nichele, ..., and Ch. Marcus, Phys. Rev. Lett. **119**, 136803 (2017).

/ Niels Bohr Institute, Copenhagen, Denmark /

TRANSITION FROM TRIVIAL TO TOPOLOGICAL PHASE

A pair of the Shiba (Andreev) states evolve into the Majorana qps



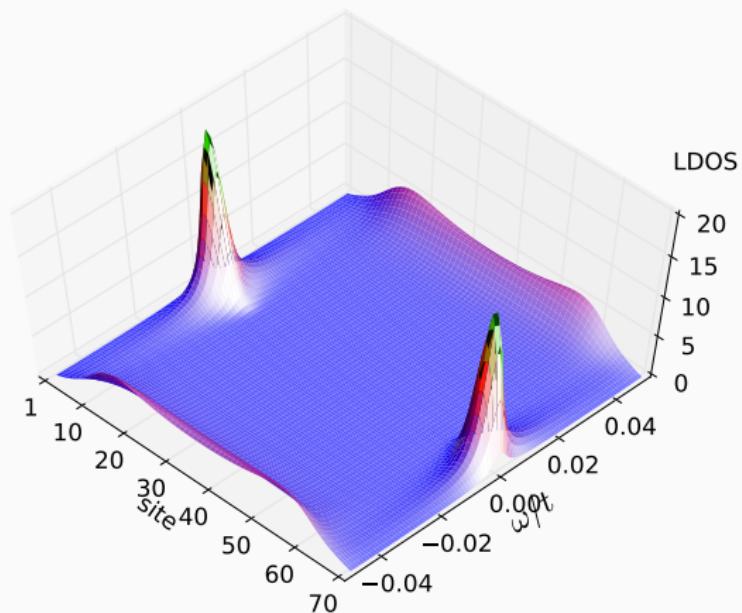
Mutation of the trivial bound states into the nontrivial Majorana modes

M.M. Maśka, A. Gorczyca-Goraj, J. Tworzydło, T. Domański, PRB 95, 045429 (2017).

TOPOLOGICAL PROTECTION

Low energy quasiparticles of the Rashba nanowire

$$t_{35}/t = 1.0$$

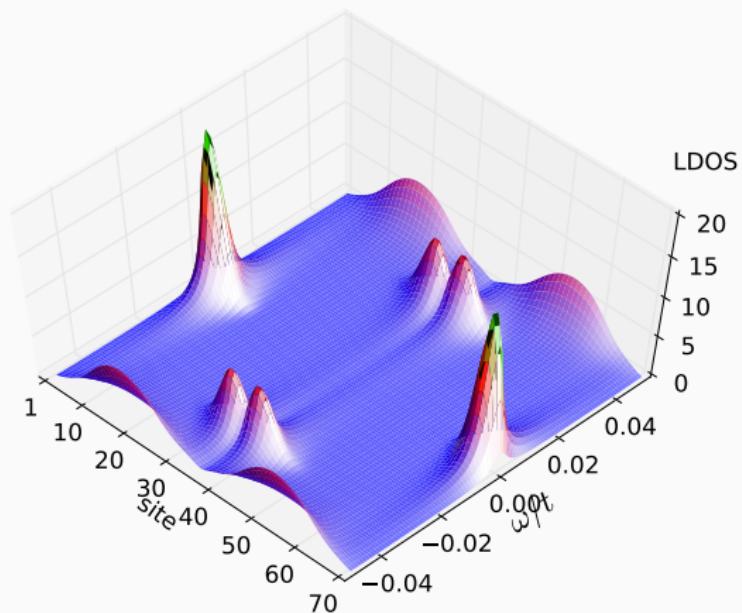


M.M. Maśka, A. Gorczyca-Goraj, J. Tworzydło, T. Domański, PRB 95, 045429 (2017).

TOPOLOGICAL PROTECTION

Low energy quasiparticles of the Rashba nanowire

$t_{35}/t = 0.8$

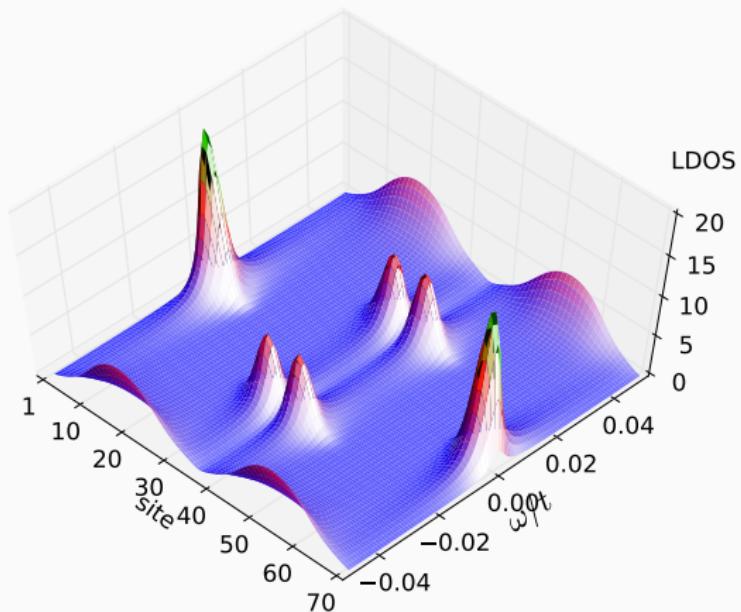


M.M. Maśka, A. Gorczyca-Goraj, J. Tworzydło, T. Domański, PRB 95, 045429 (2017).

TOPOLOGICAL PROTECTION

Low energy quasiparticles of the Rashba nanowire

$t_{35}/t = 0.6$

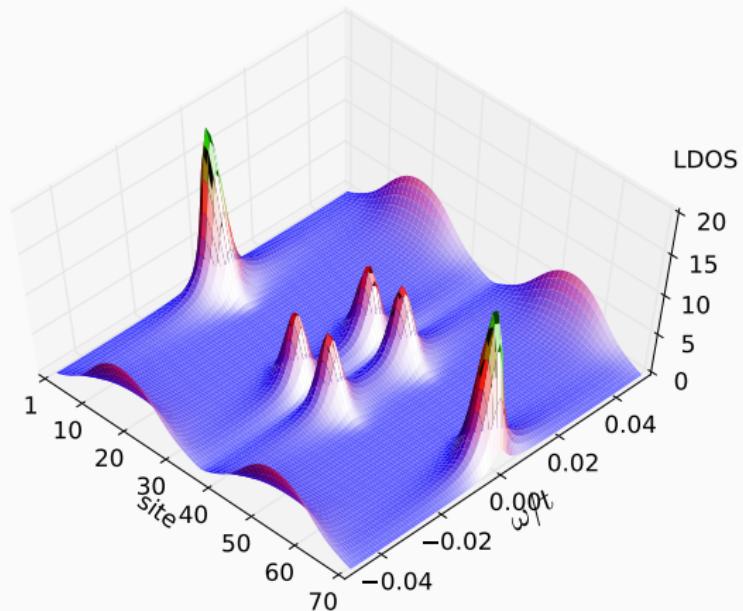


M.M. Maśka, A. Gorczyca-Goraj, J. Tworzydło, T. Domański, PRB 95, 045429 (2017).

TOPOLOGICAL PROTECTION

Low energy quasiparticles of the Rashba nanowire

$t_{35}/t = 0.4$

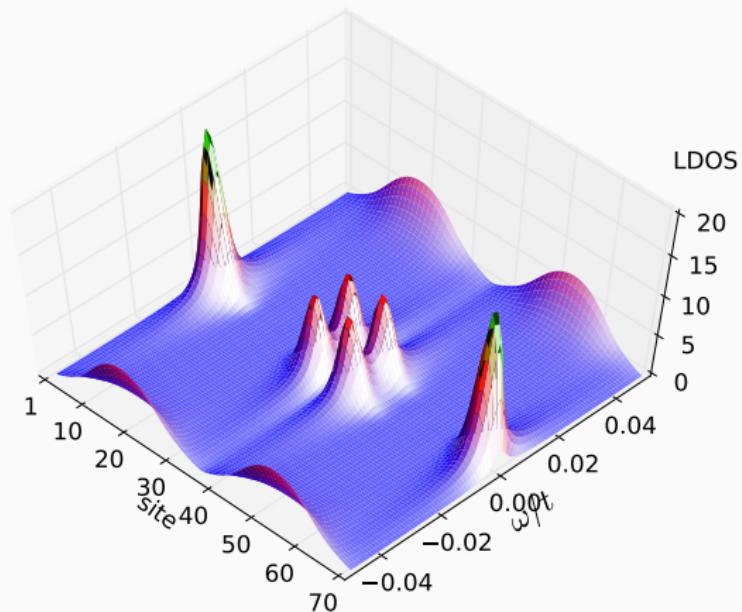


M.M. Maśka, A. Gorczyca-Goraj, J. Tworzydło, T. Domański, PRB 95, 045429 (2017).

TOPOLOGICAL PROTECTION

Low energy quasiparticles of the Rashba nanowire

$t_{35}/t = 0.2$

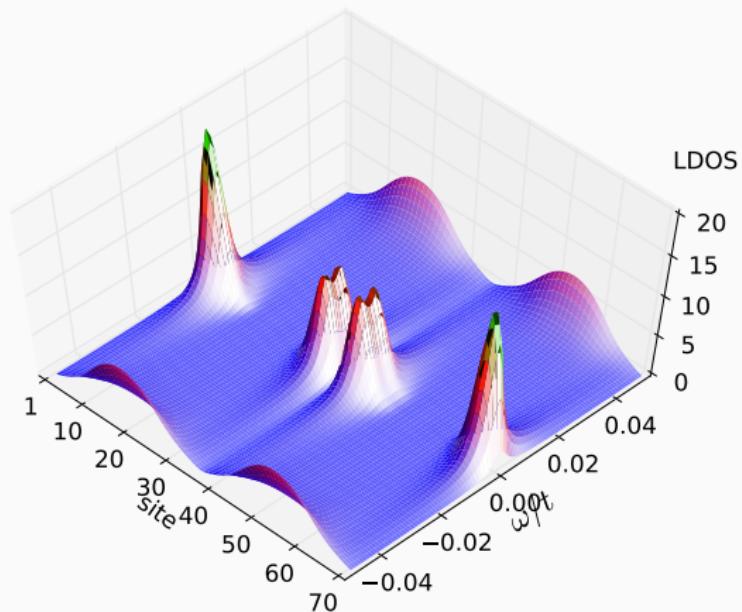


M.M. Maśka, A. Gorczyca-Goraj, J. Tworzydło, T. Domański, PRB 95, 045429 (2017).

TOPOLOGICAL PROTECTION

Low energy quasiparticles of the Rashba nanowire

$t_{35}/t = 0.1$

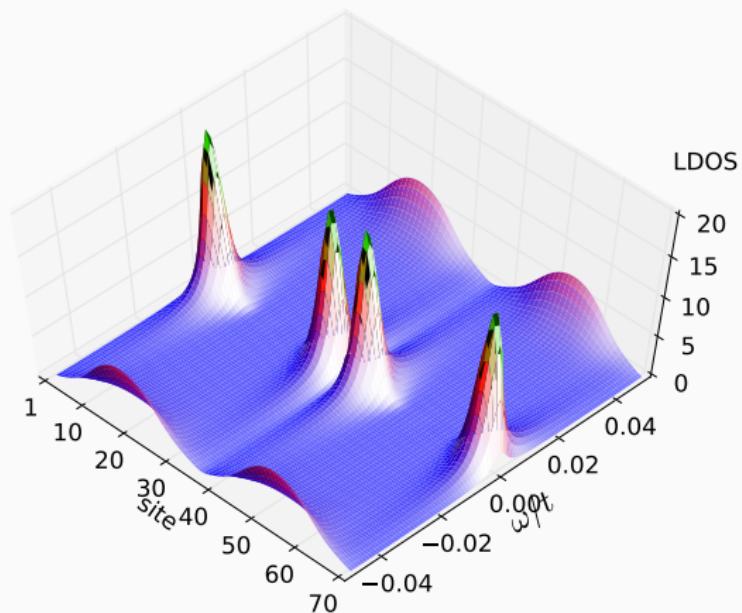


M.M. Maśka, A. Gorczyca-Goraj, J. Tworzydło, T. Domański, PRB 95, 045429 (2017).

TOPOLOGICAL PROTECTION

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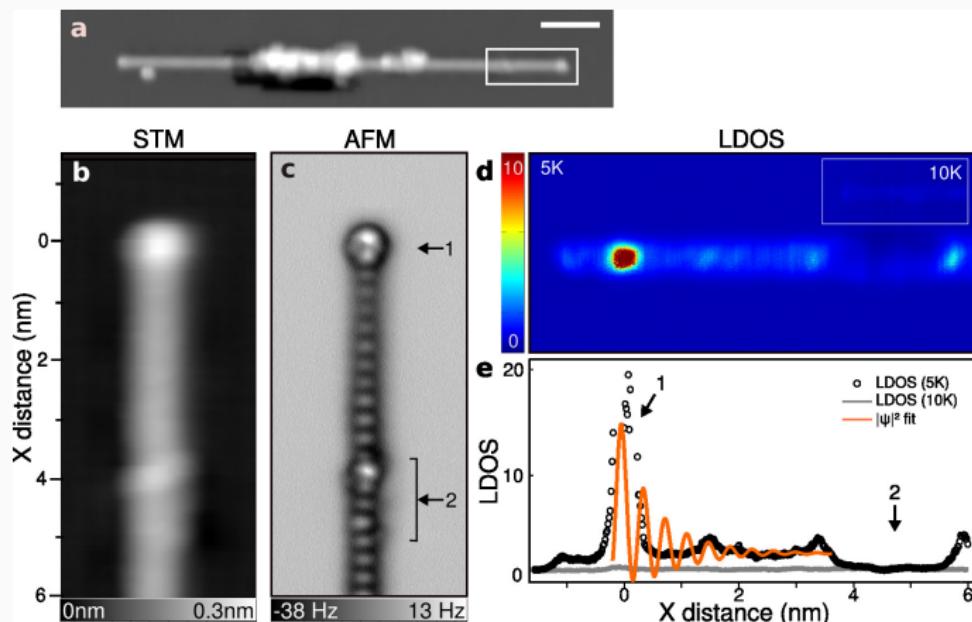
$t_{35}/t = 0.0$



M.M. Maśka, A. Gorczyca-Goraj, J. Tworzydło, T. Domański, PRB 95, 045429 (2017).

EXPERIMENTAL FACTS

AFM & STM data for Fe chain on Pb(110) surface

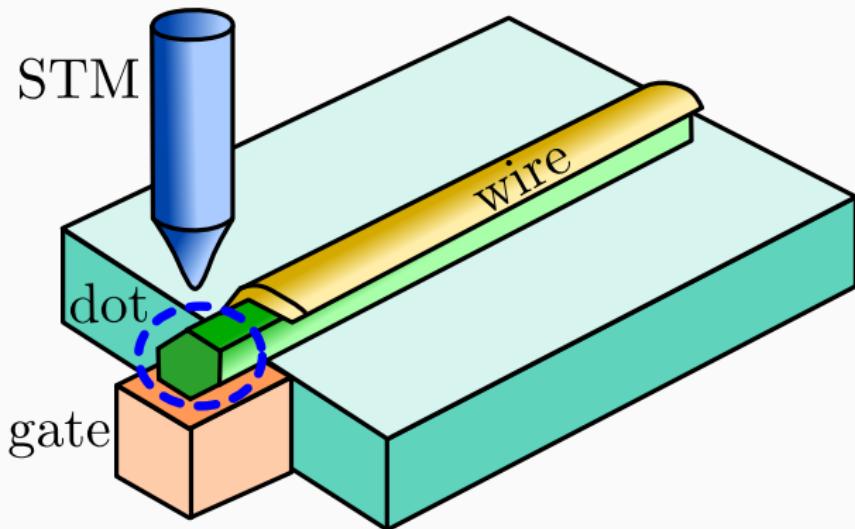


R. Pawlak, M. Kisiel *et al*, npj Quantum Information **2**, 16035 (2016).
/ University of Basel, Switzerland /

Trivial vs Majorana qps

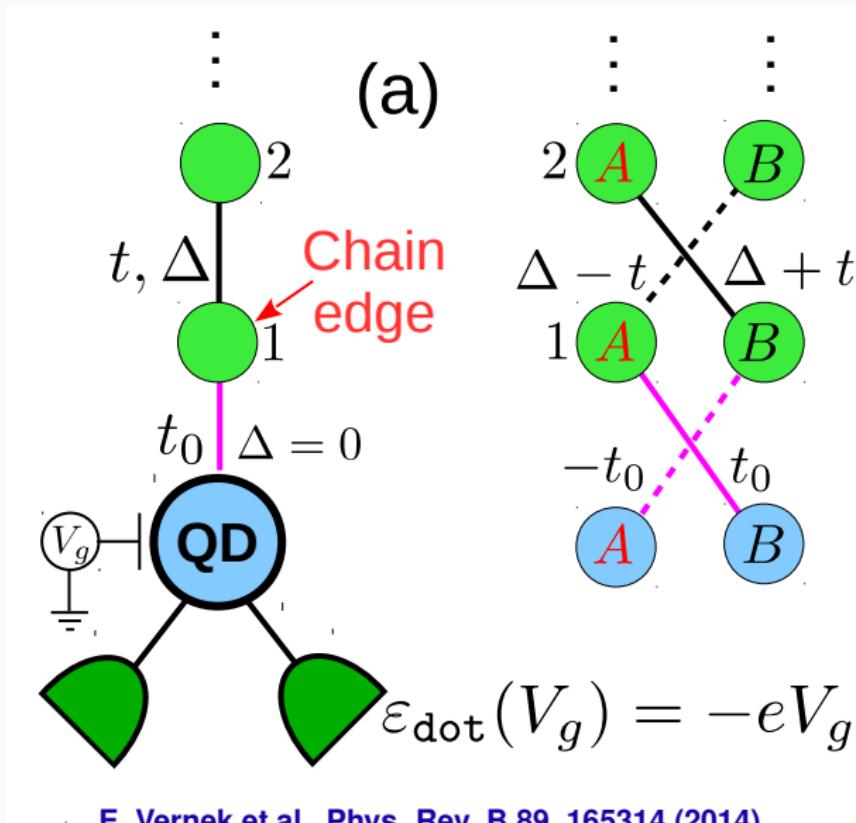
TRIVIAL VS MAJORANA BOUND STATES

Schematics of a quantum dot – nanowire hybrid structure.



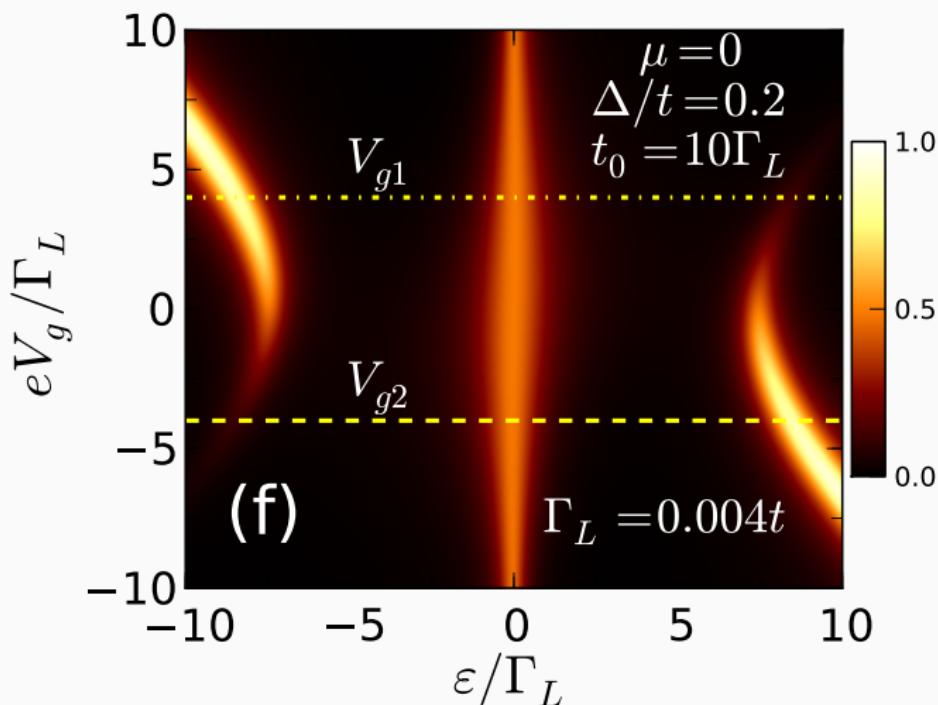
A. Ptak, A. Kobialka & T. Domański, Phys. Rev. 96, 195403 (2017).

KITAEV CHAIN + NORMAL SITE



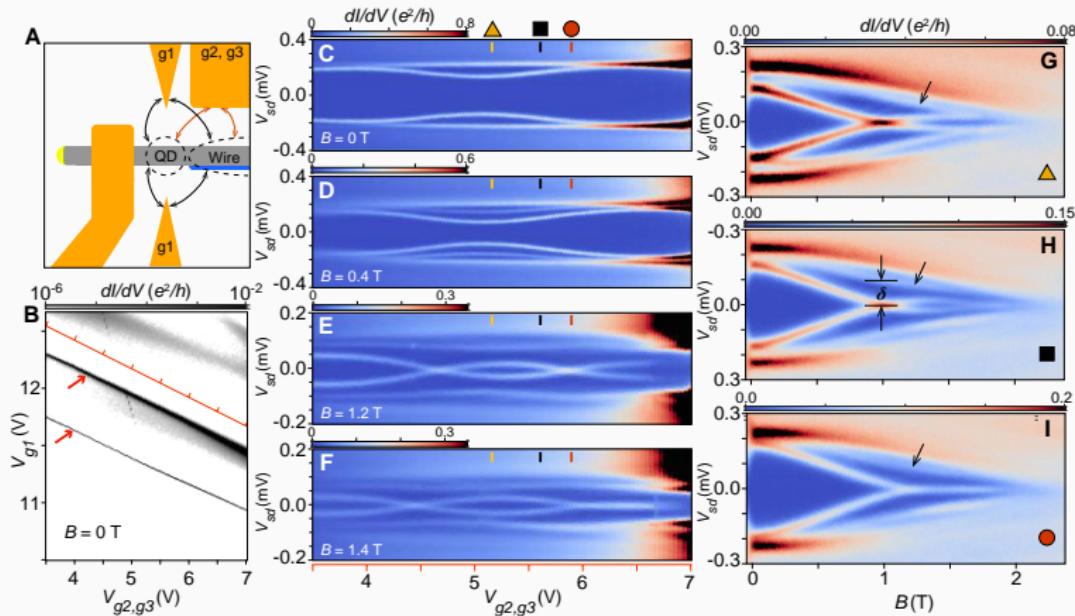
KITAEV CHAIN + NORMAL SITE

Subtle leakage of a Majorana mode into a quantum dot



LEAKAGE OF MAJORANAS ON QUANTUM DOT

'Coalescence' of the Andreev into Majorana qps

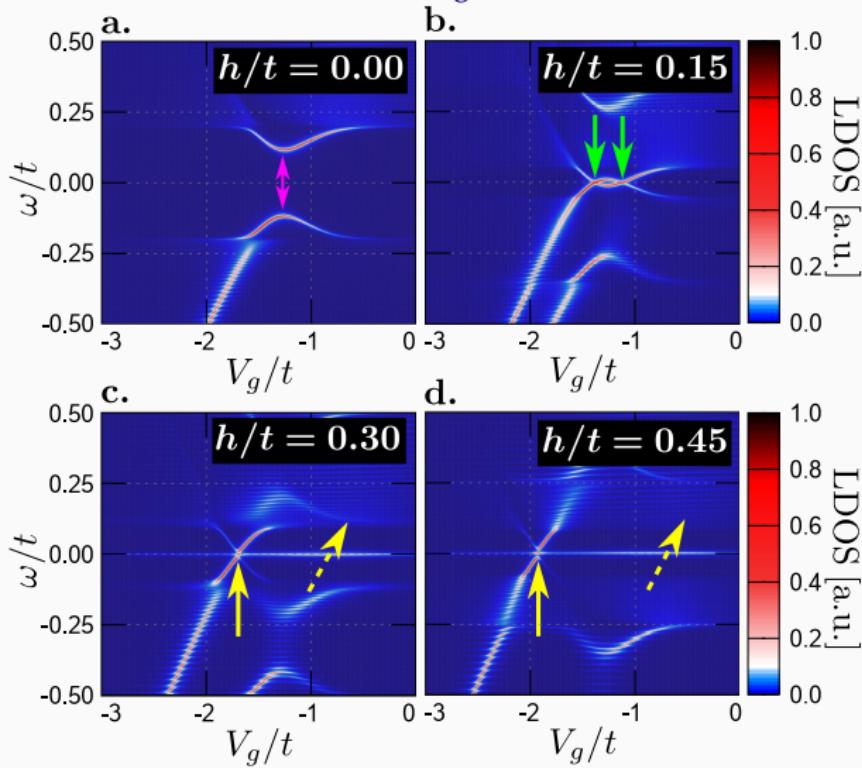


M.T. Deng, ..., and Ch. Marcus, Science 354, 1557 (2016).

/ Niels Bohr Institute, Copenhagen, Denmark /

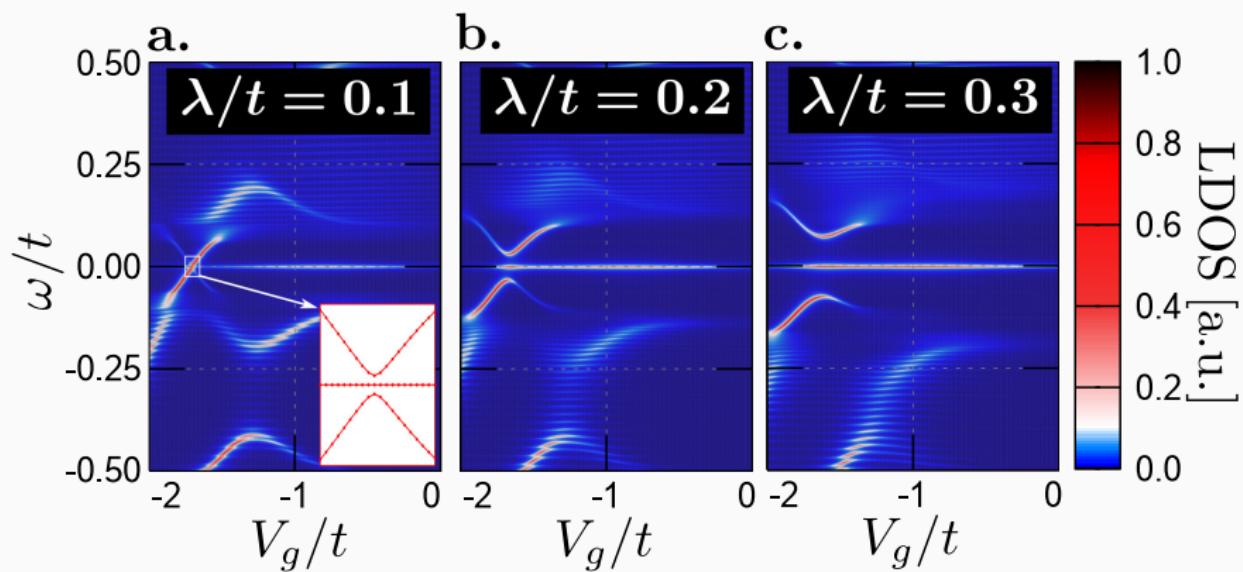
DISTINGUISHING ANDREEV FROM MAJORANA QPS

QD spectrum vs gate potential V_g for several magnetic fields h .



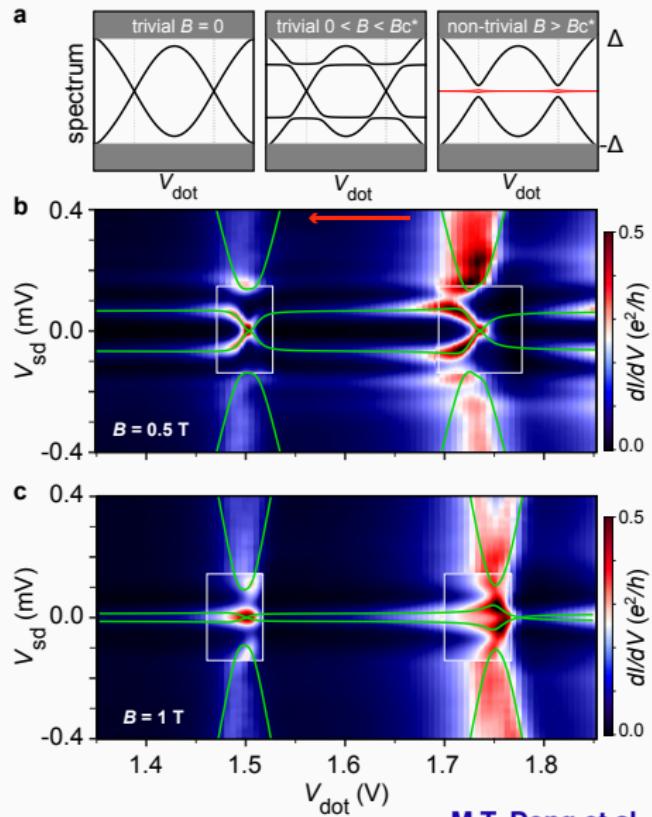
DISTINGUISHING ANDREEV FROM MAJORANA QPS

QD spectrum vs gate potential V_g for various spin-orbit couplings λ .

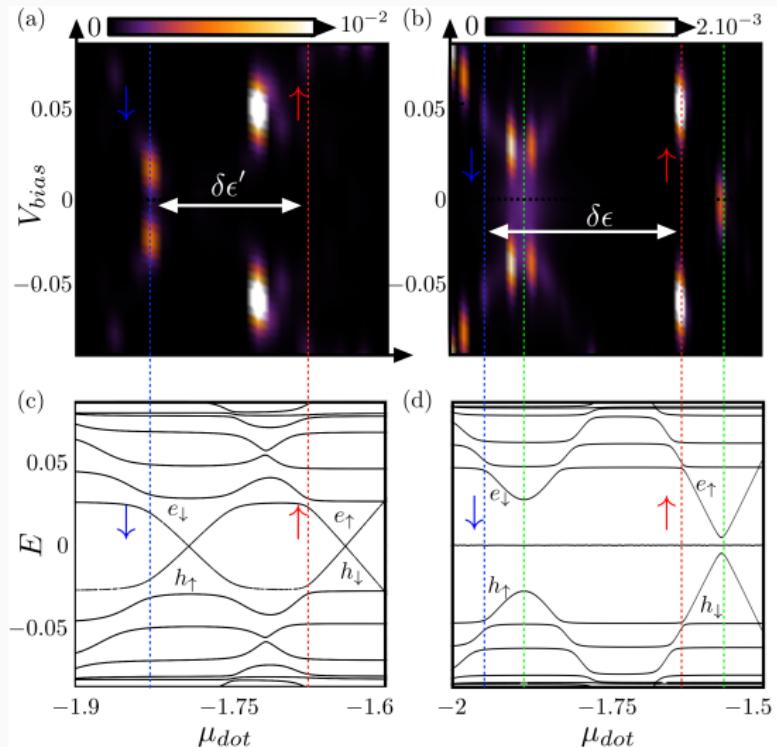


A. Ptak, A. Kobiałka & T. Domański, Phys. Rev. 96, 195403 (2017).

DISTINGUISHING ANDREEV FROM MAJORANA QPS



DISTINGUISHING ANDREEV FROM MAJORANA QPS



D. Chevallier, ... and J. Klinovaja, Phys. Rev. B 97, 04504 (2018).

ANDREEV VS MAJORANA: CONCLUSIONS

- Low energy features are very distinct:

ANDREEV VS MAJORANA: CONCLUSIONS

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 - ⇒ avoided-crossing behavior of Andreev/Shiba qps
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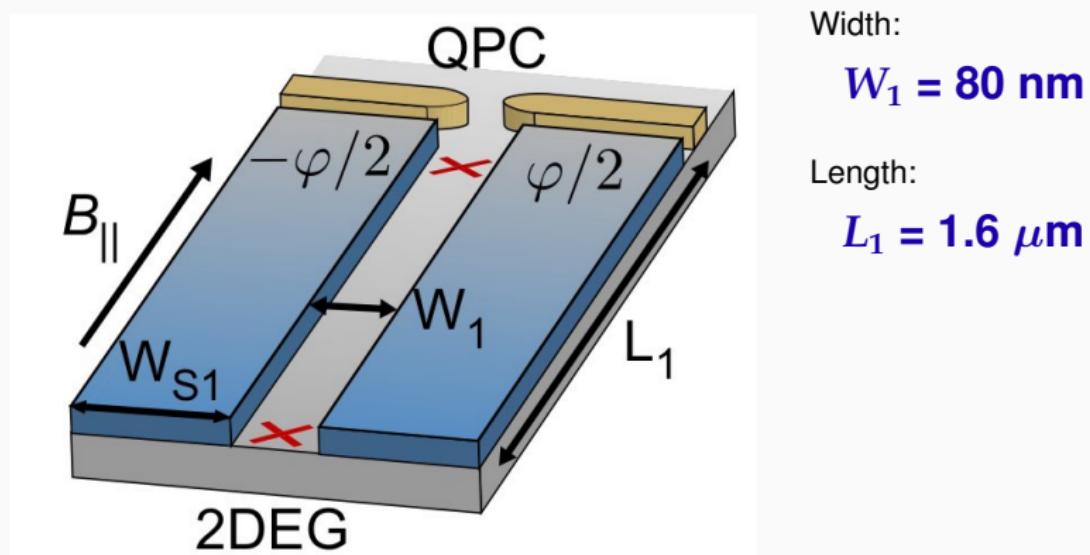
ANDREEV VS MAJORANA: CONCLUSIONS

- Low energy features are very distinct:
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 - ⇒ leakage of the zero-energy Majorana qps
- Misinterpretation:
 - ⇒ coalescence of Andreev into Majorana qps

Localized Majorana modes in dim=2

PLANAR JOSEPHSON JUNCTIONS

Two-dimensional electron gas of **InAs** epitaxially covered by a thin **Al** layer

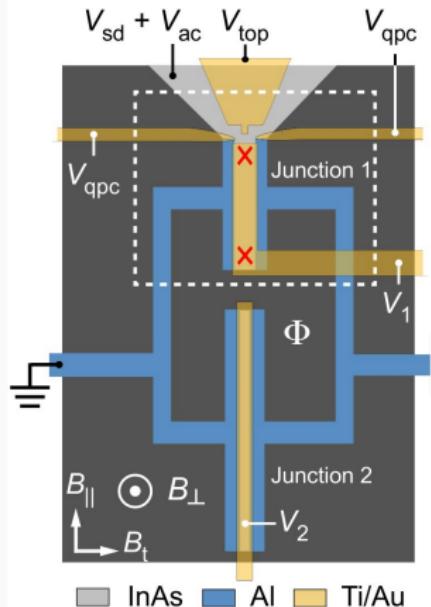


A. Fornieri, ..., Ch. Marcus and F. Nichele, arXiv:1809.03037 (9 Sept 2018).

/ Niels Bohr Institute (Copenhagen, Denmark) /

PLANAR JOSEPHSON JUNCTIONS

Majorana qps at the ends of 2DEG depend on the phase-difference Φ

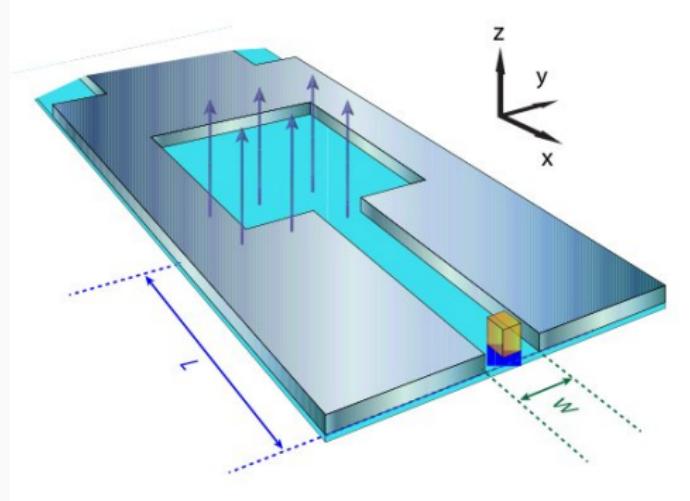


A. Fornieri, ..., Ch. Marcus and F. Nichele, arXiv:1809.03037 (9 Sept 2018).

/ Niels Bohr Institute (Copenhagen, Denmark) /

PLANAR JOSEPHSON JUNCTIONS

Two-dimensional **HgTe** quantum well coupled to thin **Al** film

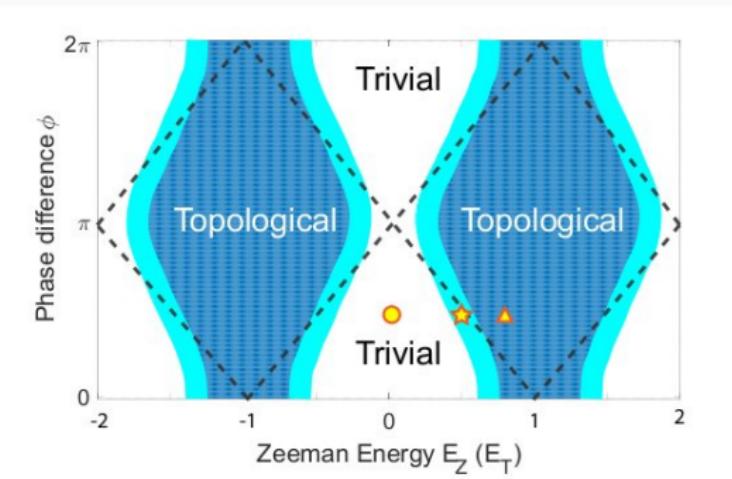


H. Ren, ..., L.W. Molenkamp, B.I. Halperin, A. Yacoby, arXiv:1809.03076
(10 Sept 2018).

/ Würzburg Univ. (Germany) + Harvard Univ. (USA) /

PLANAR JOSEPHSON JUNCTIONS

Tuning between the trivial and topological superconducting state
by phase difference ϕ and in-plane magnetic field



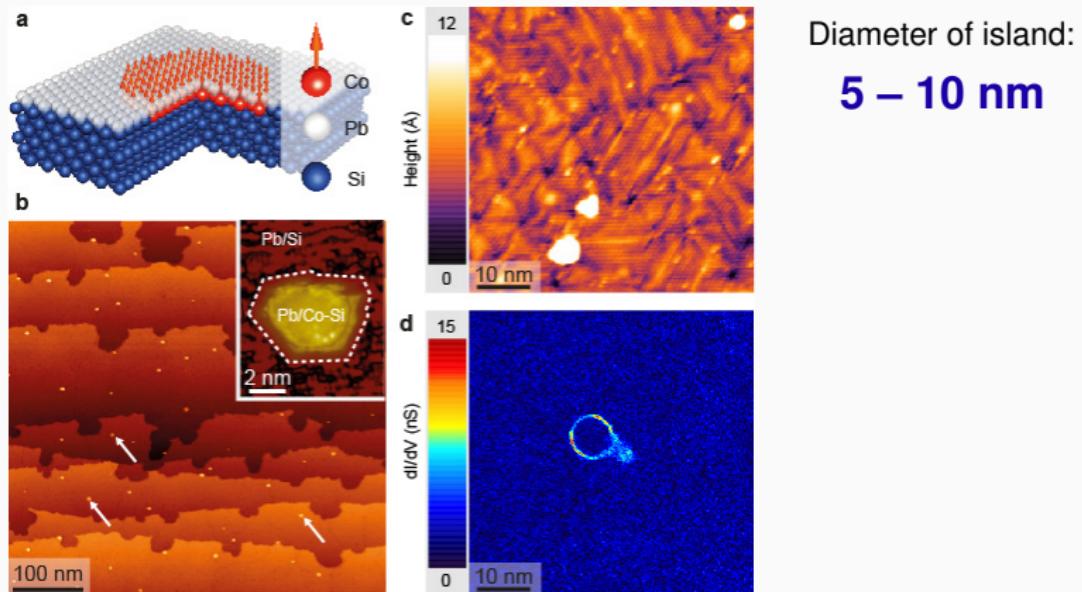
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(10 Sept 2018).

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Edge modes in dim=2 systems

TWO-DIMENSIONAL MAGNETIC STRUCTURES

Magnetic island of **Co** atoms deposited on the superconducting Pb surface

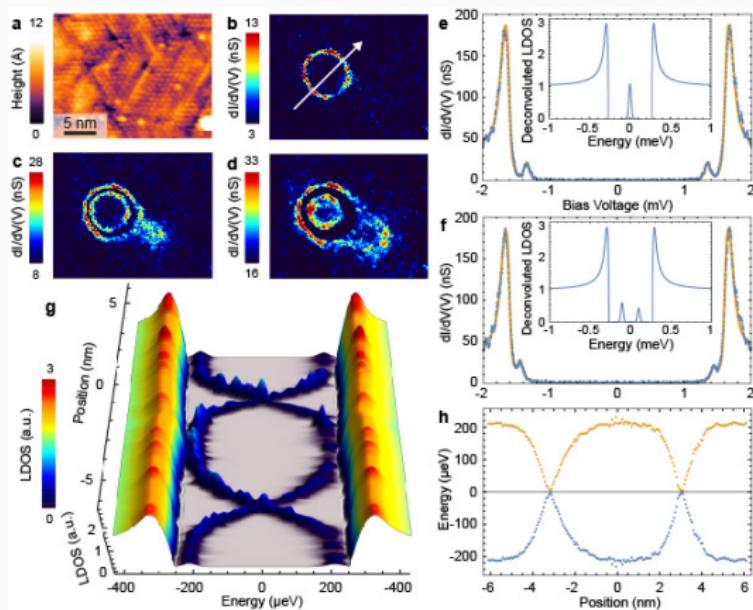


G. Ménard, ..., and P. Simon, Nature Commun. **8**, 2040 (2017).

/ P. & M. Curie University (Paris, France) /

EVIDENCE FOR DELOCALIZED MAJORANA MODES

Majorana modes propagating along magnetic islands

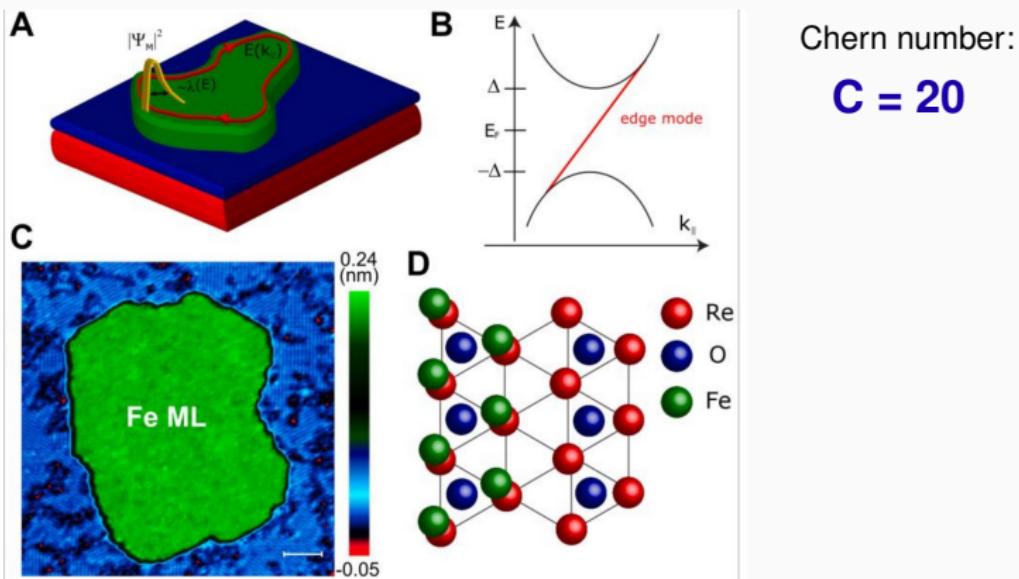


G. Ménard, ..., and P. Simon, Nature Commun. **8**, 2040 (2017).

/ P. & M. Curie University (Paris, France) /

PROPAGATING MAJORANA EDGE MODES

Magnetic island of **Fe** atoms deposited on the superconducting Re surface



Chern number:

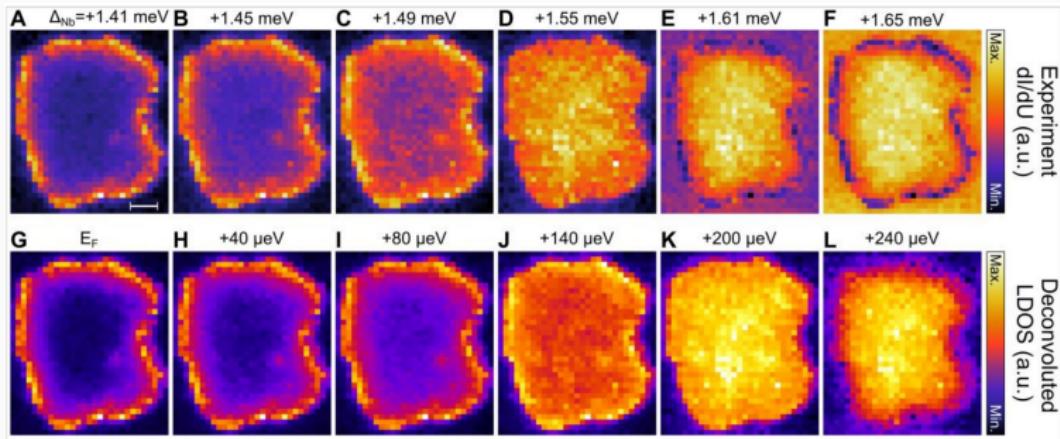
$$\mathbf{C} = 20$$

A. Palacio-Morales, ..., and R. Wiesendanger, arXiv:1809.04503 (preprint).

/ University of Hamburg (Germany) /

PROPAGATING MAJORANA EDGE MODES

Real space maps of the tunneling conductance (top panel) and deconvoluted DOS (bottom panel) obtained for various energies (as indicated) in the subgap regime ($\Delta = 240 \mu eV$).



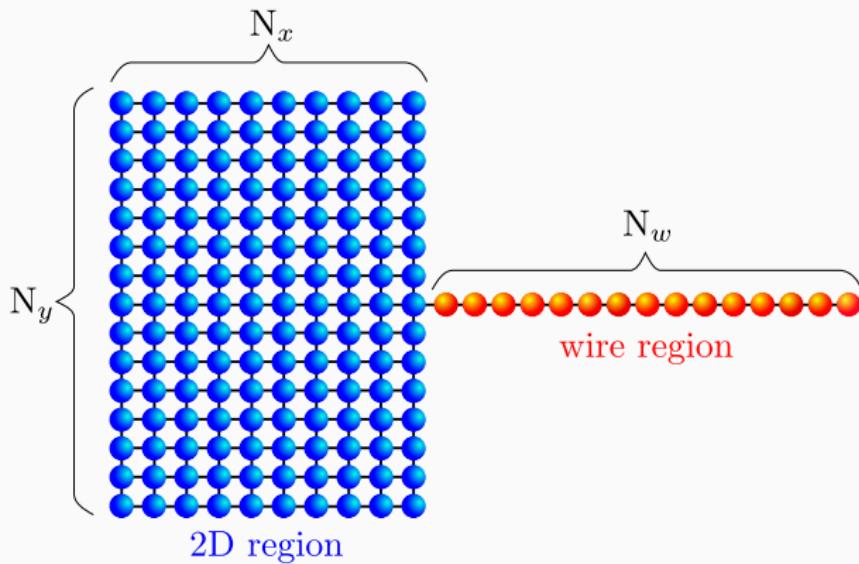
A. Palacio-Morales, ..., and R. Wiesendanger, arXiv:1809.04503 (preprint).

/ University of Hamburg (Germany) /

Mixed – dimensionality structures

CAN MAJORANA QPS BE DECONFINED ?

Our project: Majorana qps of the 1D–2D hybrid structure



A. Kobiałka, T. Domański & A. Ptok, arXiv:1808.05281

TOPOLOGICAL INVARIANTS

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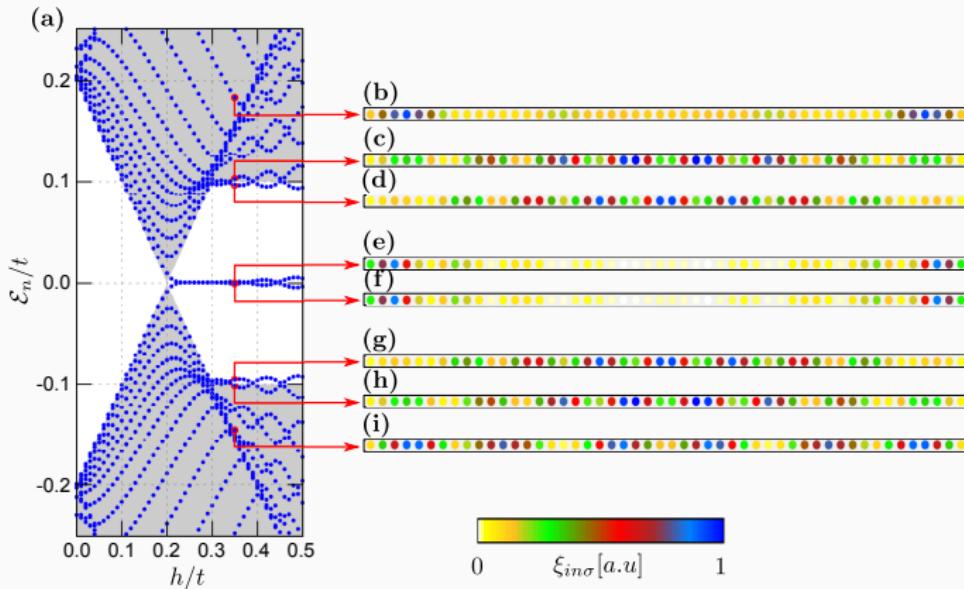
which can be characterized by the Chern number, that is equivalent to the Thouless–Kohmoto–Nightingale–den Nijs number.

For details, concerning the topological criteria see e.g.

- A. Kitaev, AIP Conf. Proc. 1134, 22 (2009);
- M.Z. Hasan & C.L. Kane, Rev. Mod. Phys. 82, 3045 (2010);
- X.-L. Qi & S.-C. Zhang, Rev. Mod. Phys. 83, 1057 (2011).

TRIVIAL VS MAJORANA MODES

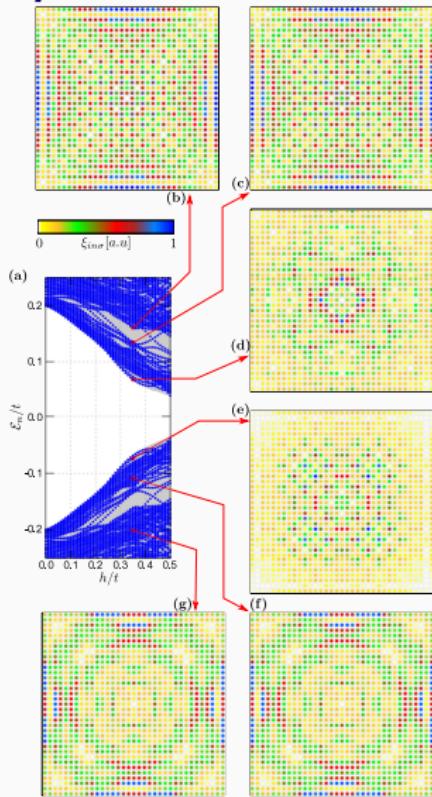
Spatial distribution of quasiparticles in the nanowire



/ topological phase /

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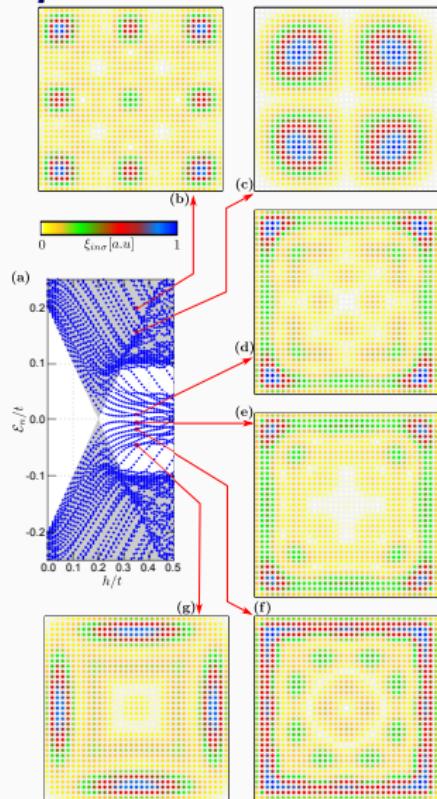
Spatial distribution of quasiparticles in the plaquette



nontopological phase

TRIVIAL VS MAJORANA MODES

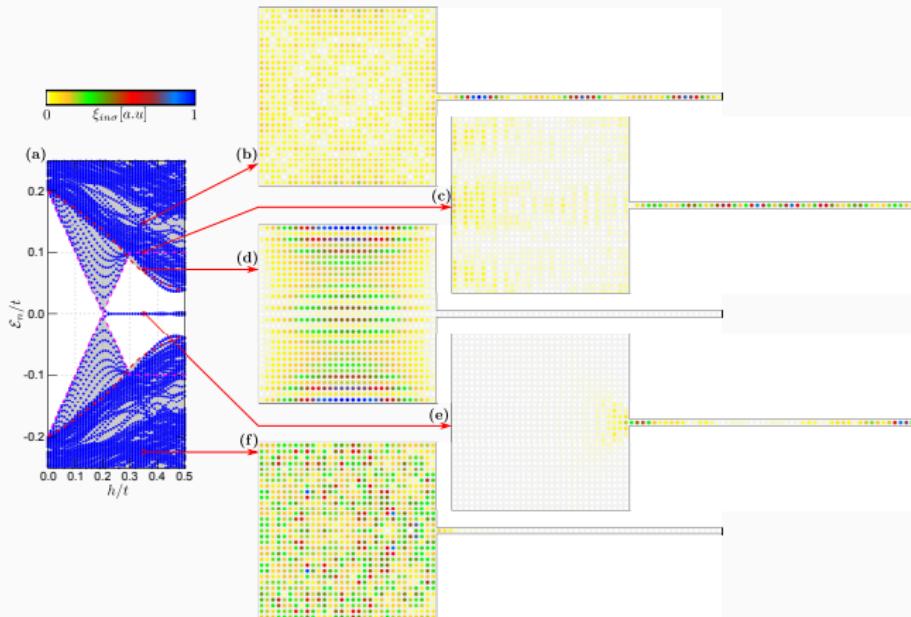
Spatial distribution of quasiparticles in the plaquette



topological phase

TRIVIAL VS MAJORANA MODES

Majorana/Andreev quasiparticles of a wire-plaquette hybrid

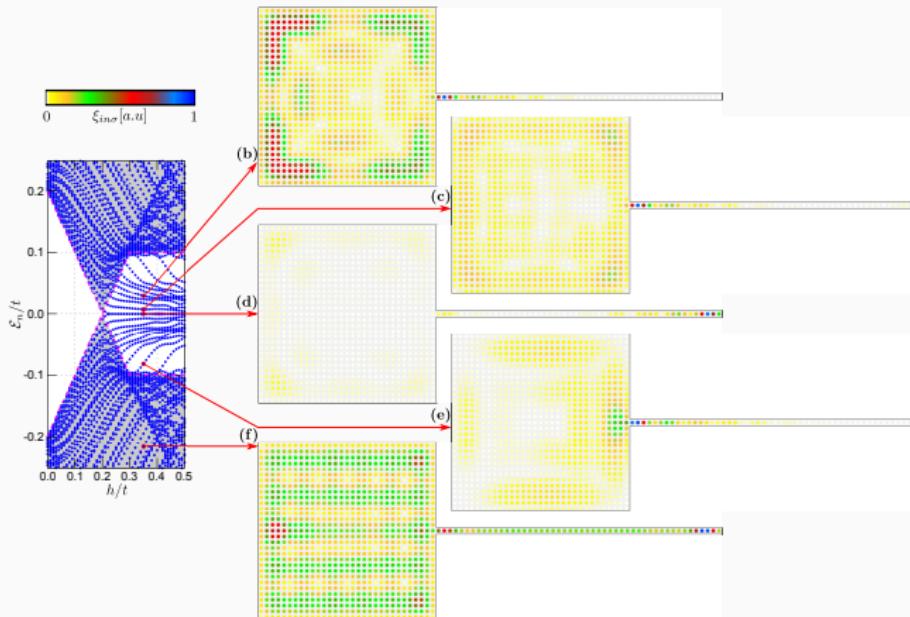


plaquette: nontopological

nanowire: topological

TRIVIAL VS MAJORANA MODES

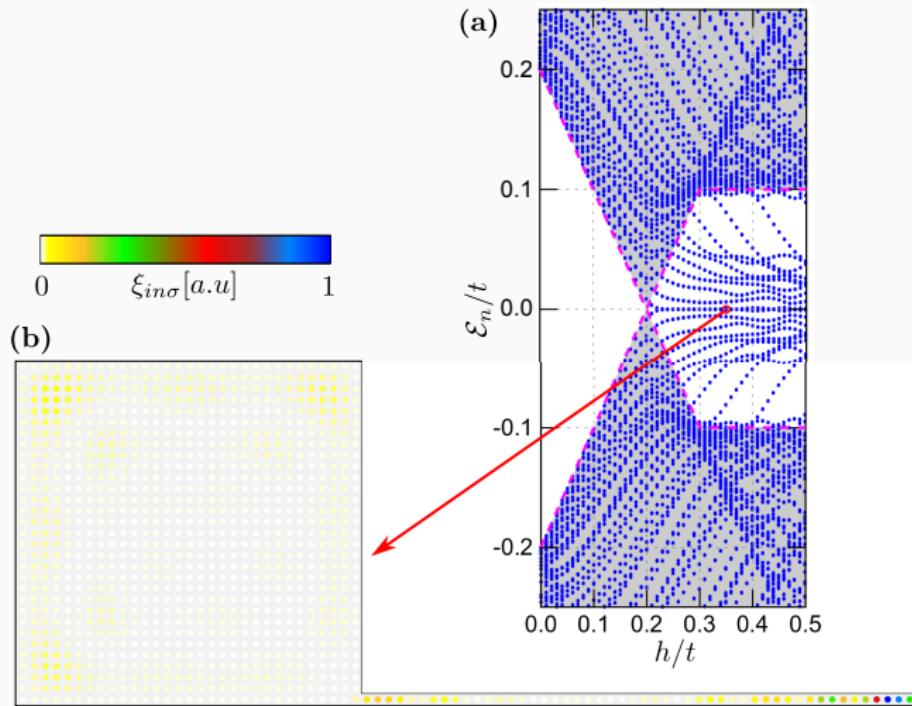
Majorana/Andreev quasiparticles of a wire-plaquette hybrid



Both regions are assumed to be in topological sc phase.

TRIVIAL VS MAJORANA MODES

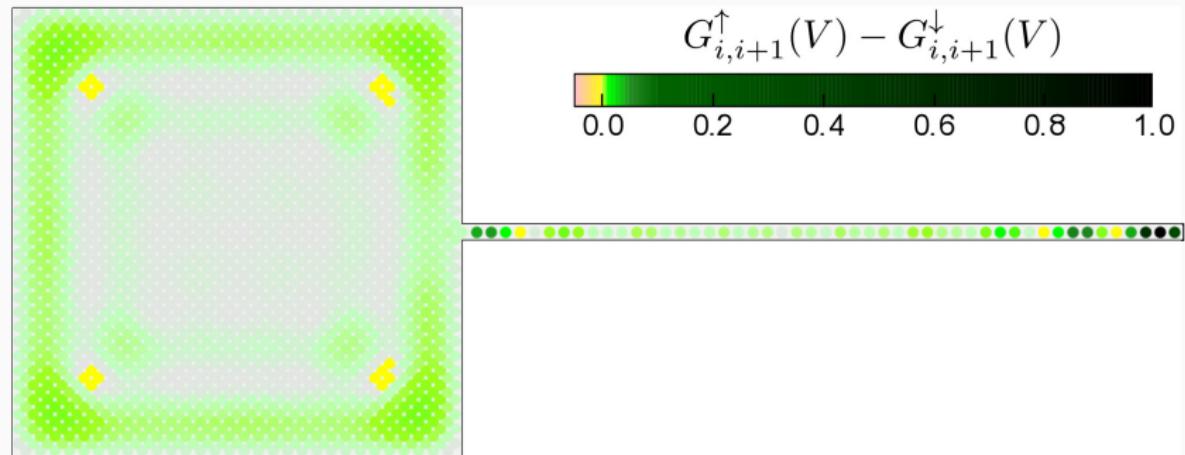
Majorana/Andreev quasiparticles of a wire-plaquette hybrid



Both regions are assumed to be in topological sc phase.

HOW TO DETECT (DE)LOCALIZED MAJORANA QPS

Maps of the SESAR tunneling conductance at zero-bias.



SE SAR = Selective Equal Spin Andreev Reflection

A. Kobiałka, T. Domański & A. Ptok, arXiv:1808.05281

DIMENSIONAL HYBRID: CONCLUSION

Plaquette-nanowire hybrid structures enables:

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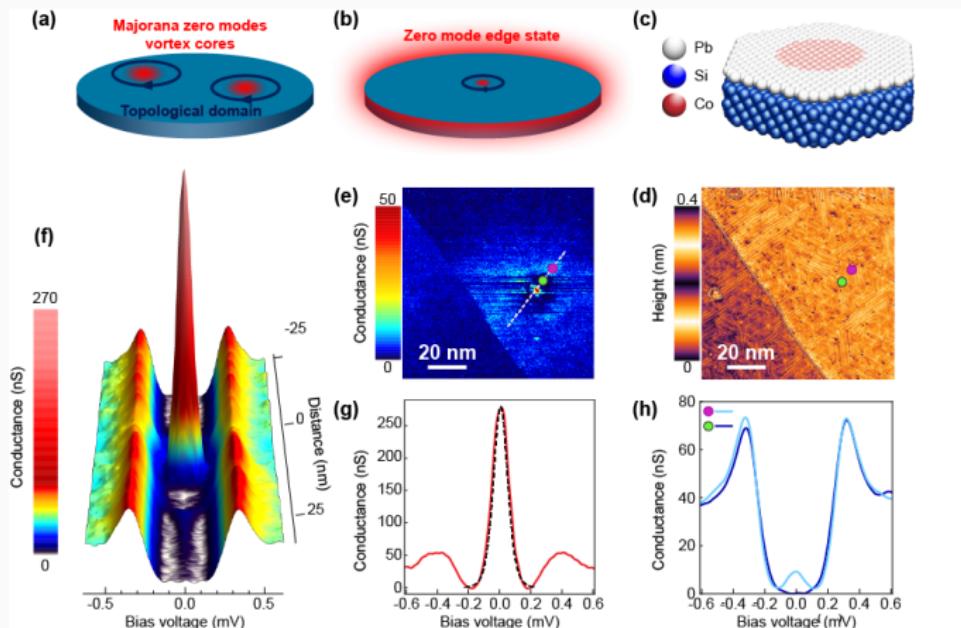
- ⇒ conversion of the Majorana quasiparticle
- ⇒ into the delocalized edge-mode

Is this edge mode itinerant ?

Further outlook

SIMILAR IDEAS: DEFECTS IN MAGNETIC ISLAND

Localized Majorana at point-like defect, coexisting with itinerant Majorana edge mode (observed in Co-Si island on disordered Pb)

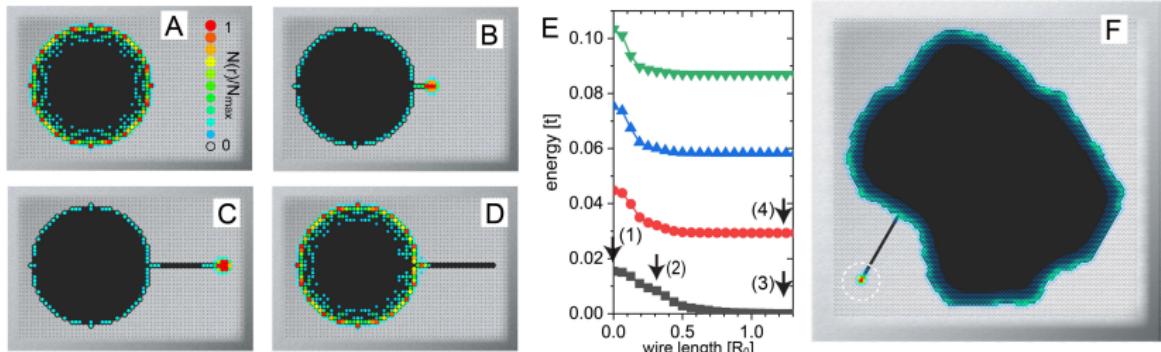


G.C. Ménard, ..., P. Simon and T. Cren, arXiv:1810.09541

Paris (France)

SIMILAR IDEAS: ISLAND + NONOWIRE

Itinerant Majorana mode leaking into side-attached nanowire.

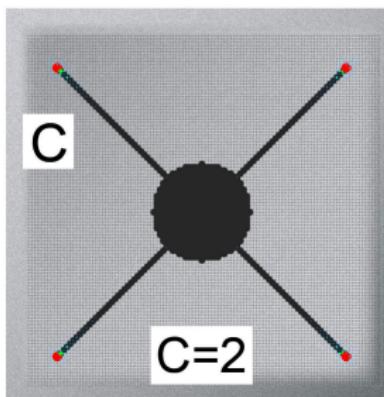
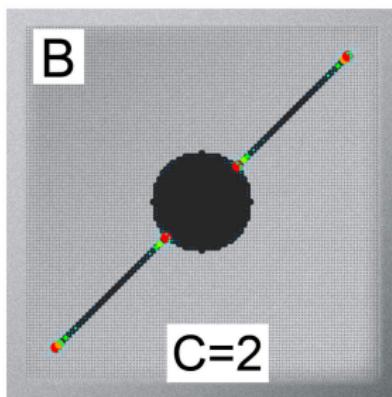
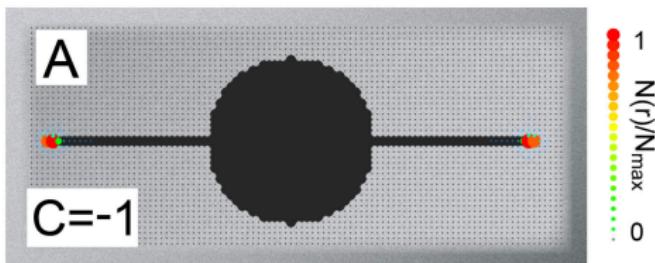


E. Mascot, S. Cocklin, S. Rachel, and D.K. Morr, arXiv:1811.06664

Univ. of Illinois at Chicago (USA)

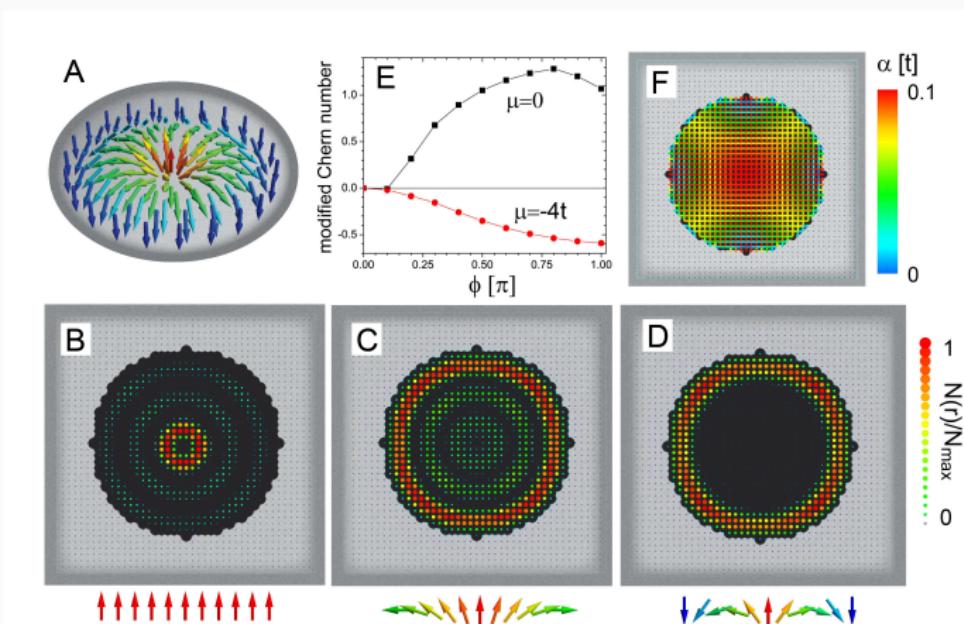
SIMILAR IDEAS: ISLAND + NONOWIRE

Majorana modes leaking to the side-attached nanowires.



PERSPECTIVES: SKYRMIONS IN SUPERCONDUCTORS

Creation of topological phase through skyrmions.



E. Mascot, S. Cocklin, S. Rachel, and D.K. Morr, arXiv:1811.06664

Univ. of Illinois at Chicago (USA)

DIMENSIONAL HYBRIDS: CONCLUSIONS

Magneto - superconducting hybrid (MSH) structures enable:

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DIMENSIONAL HYBRIDS: CONCLUSIONS

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- ⇒ controllable leakage of Majorana qps
- ⇒ (de)localisation of Majorana qps

Would it help to realise braiding of Majorana qps ?

ACKNOWLEDGEMENTS

- Majorana quasiparticles

⇒ M. Maśka & A. Gorczyca-Goraj (Katowice),
A. Kobiałka (Lublin), A. Ptak (Kraków),
J. Tworzydło (Warsaw), N. Sedlmayr (Rzeszów).

- Shiba states/bands in topological phases

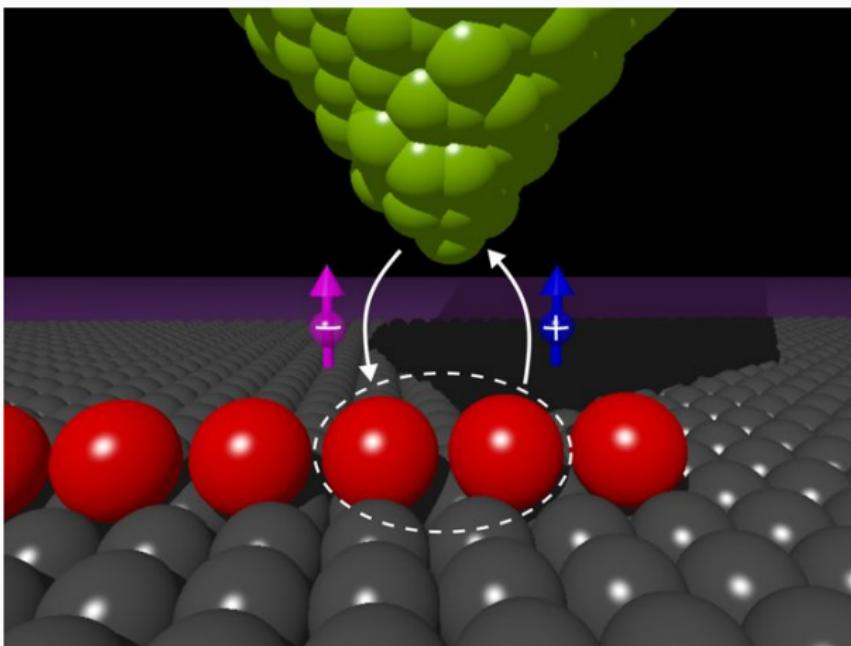
⇒ Sz. Głodzik (Lublin)

- Majorana vs Kondo

⇒ I. Weymann (Poznań), G. Górski (Rzeszów),
T. Novotný, M. Žonda & V. Janiš (Prague).

SELECTIVE EQUAL SPIN ANDREEV REFLECTIONS

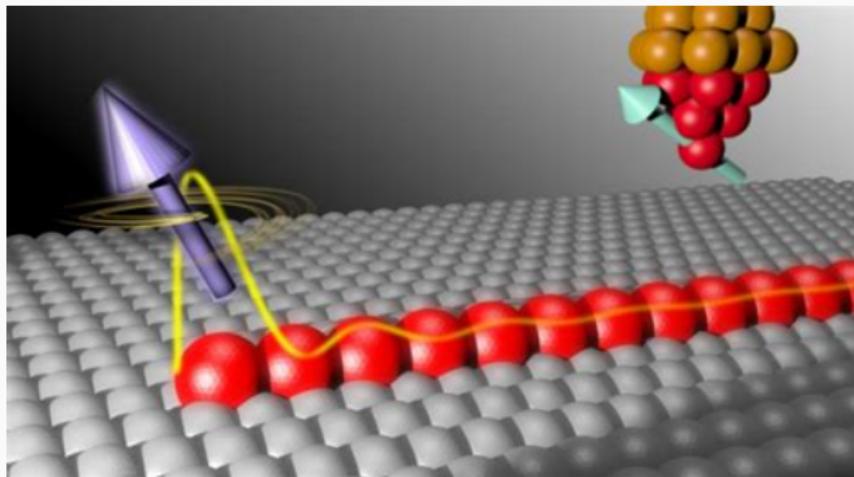
Microscopic idea of the SESAR mechanism



M. Maśka and T. Domański, Scientific Reports 7, 16193 (2017).

SPIN-POLARIZED SPECTROSCOPY

STM-type measurements for probing the Majorana qps



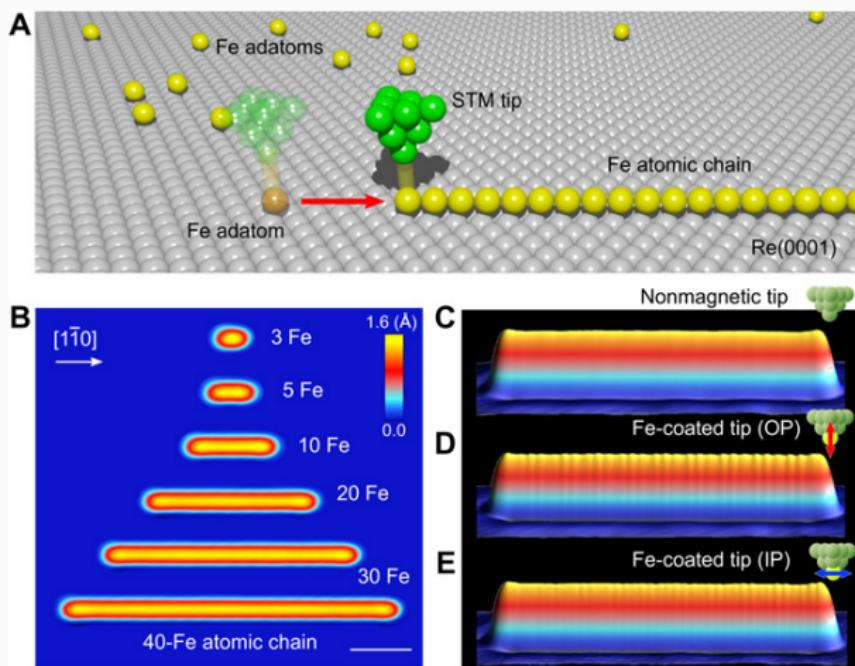
S. Jeon, ... and A. Yazdani, Science **358**, 772 (2017).

/ Princeton University, USA /

Kondo vs Majorana

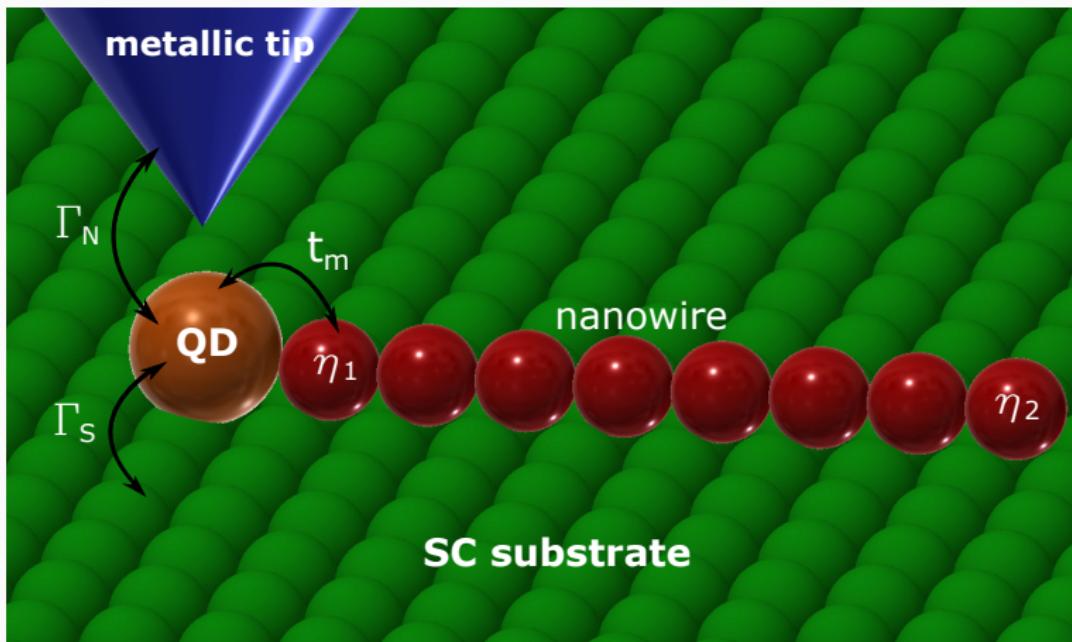
POSSIBLE EXPERIMENTAL REALISATION

Deposition of individual atoms on superconducting surface



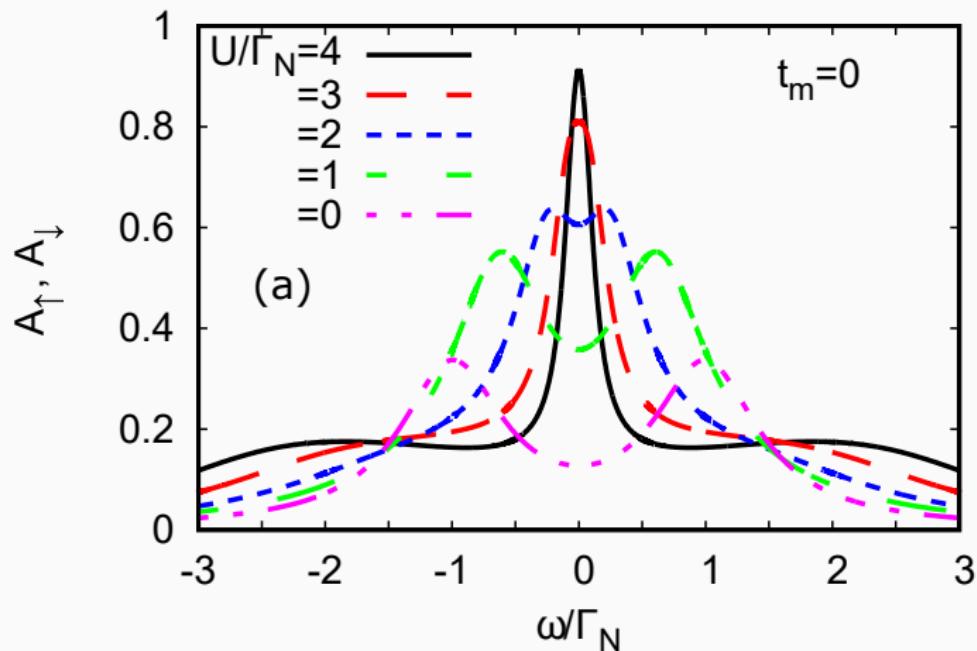
KONDO AND MAJORANA PHYSICS

STM-type setup for probing the Kondo – Majorana – pairing effects.



SUBGAP KONDO PHYSICS

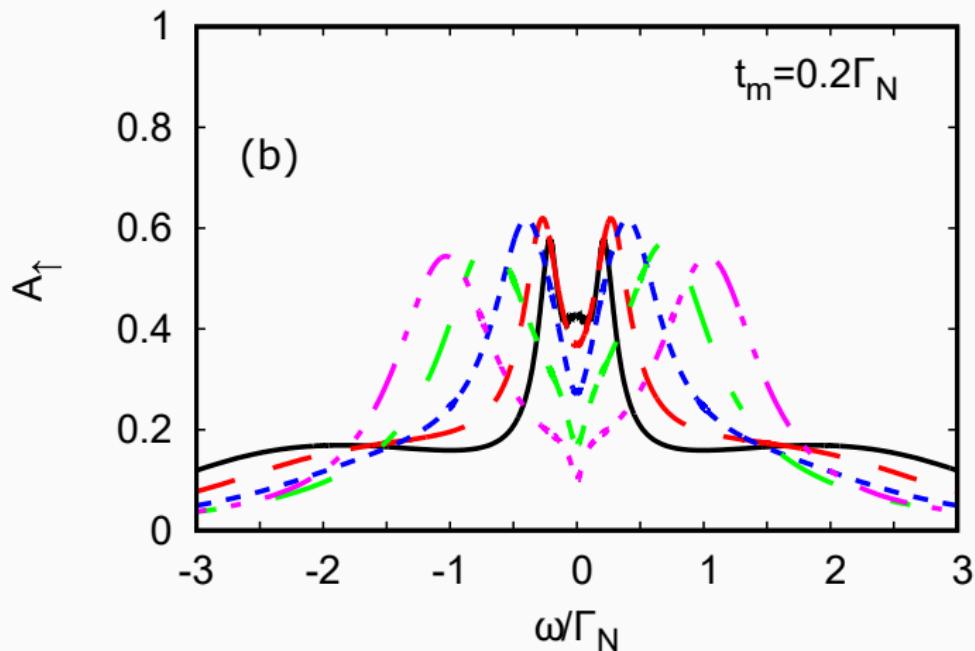
Spectrum of a quantum dot in absence of the Majoranas.



Results obtained for $t_m = 0$

KONDO VS MAJORANA

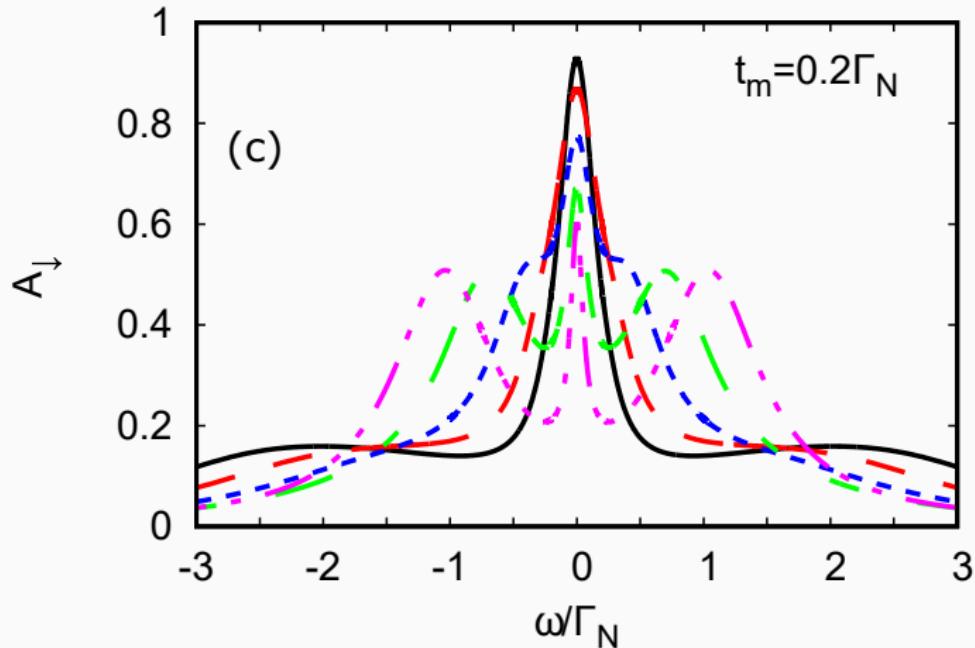
Spectrum of a quantum dot in its Kondo regime.



Results obtained for \uparrow spin, assuming $t_m = 0.2\Gamma_N$

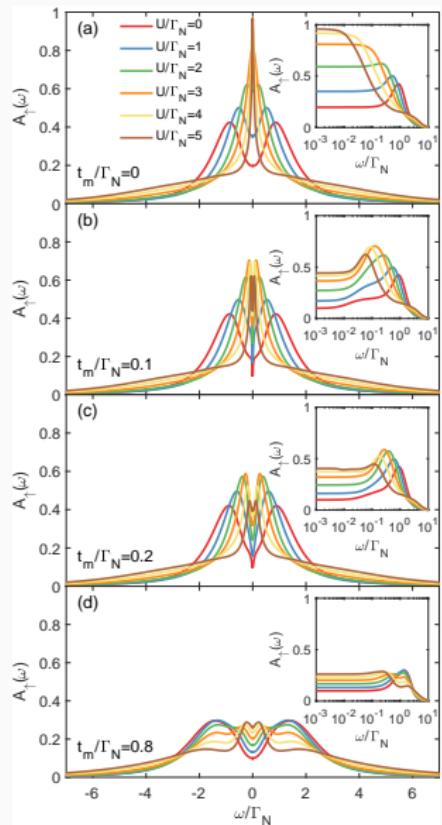
KONDO VS MAJORANA

Spectrum of the correlated QD in its Kondo regime.

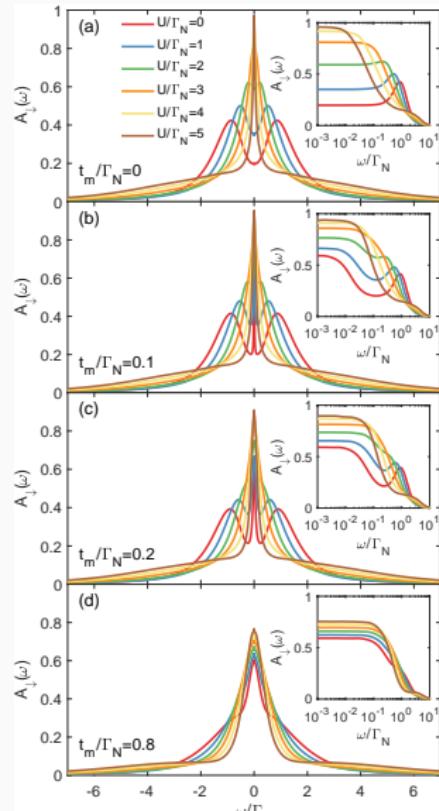
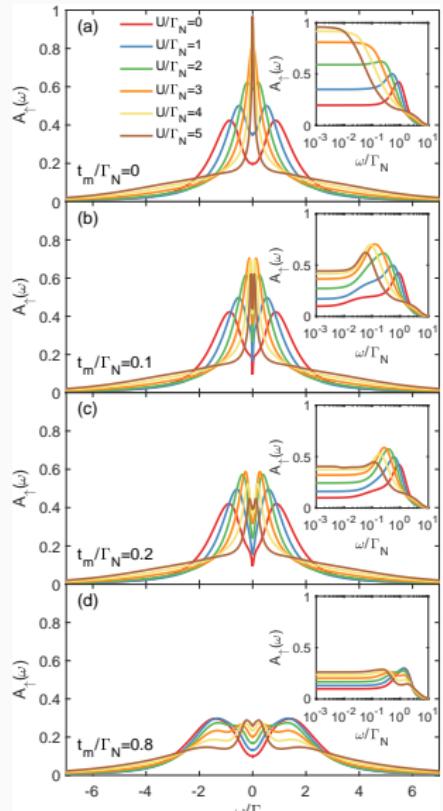


Results obtained for \downarrow spin, assuming $t_m = 0.2\Gamma_N$

SPIN-RESOLVED NRG DATA



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KONDO VS MAJORANA: CONCLUSIONS

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