



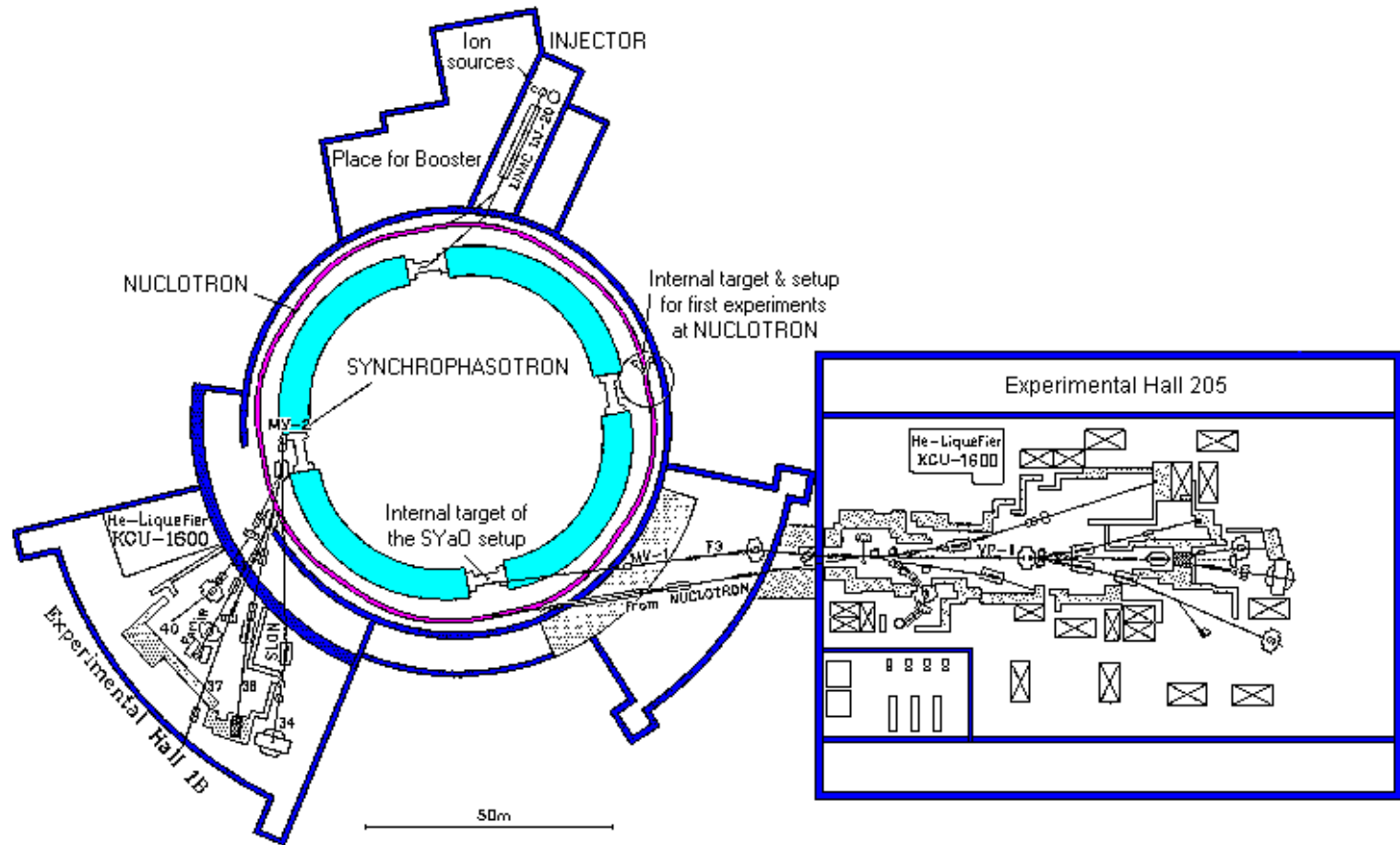
# COMPARATIVE ANALYSIS OF CROSS SECTIONS OF RESIDUAL NUCLEI ON SEPARATED TIN ISOTOPES AT A BEAM ENERGY OF PROTONS AND DEUTERONS 3.65 GeV/NUCLEON.

A.R.Balabekyan  
Yerevan State University

Coauthors:  
N.A. Demekhina, A.E.Simonyan

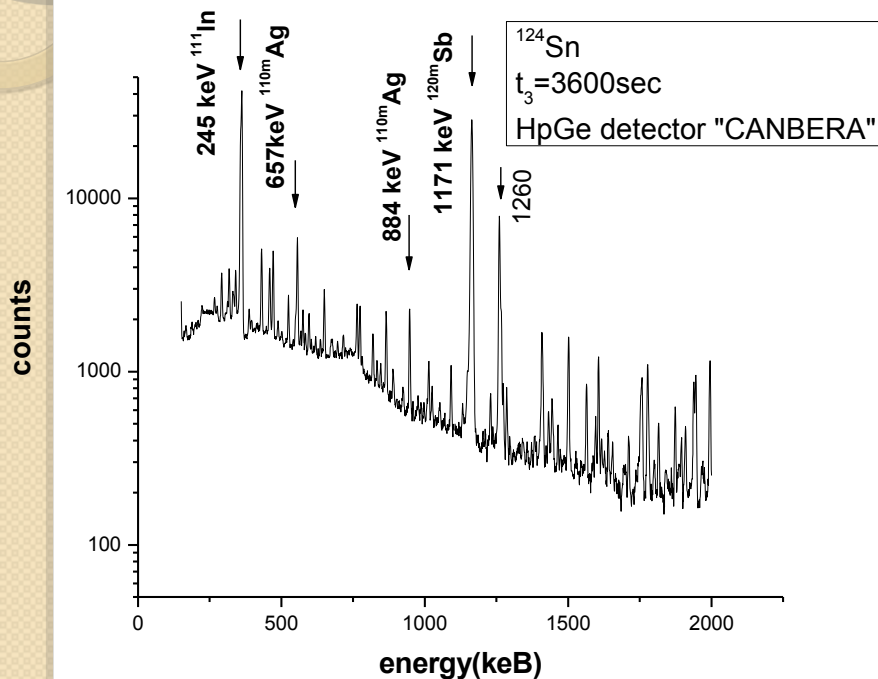


# Experimental Setup





# Characteristic Gamma Spectrum of residual nuclei



- Targets:  $^{112}\text{Sn}$

$^{118}\text{Sn}$

$^{120}\text{Sn}$

$^{124}\text{Sn}$

Energy of protons and  
deuterons beams:  
3.65 GeV/nucleon



# Analytic representation of cross-sections

$$\sigma(A, Z) = \exp(a_1 + a_2 \cdot A + a_3 \cdot A^2 + a_4 \cdot A^3 + (a_5 + a_6 \cdot A + a_7 \cdot A^2) \cdot |Z_p - Z|^{a_8})$$

$$Z_p = a_9 \cdot A + a_{10} \cdot A^2$$

$A_1, A_2, A_3, A_4$  give the shape of mass-yield curve  
 $A_5, A_6, A_7$  give the width of isobaric distribution  
 $A_9, A_{10}$  give the position of peak of isobaric distribution

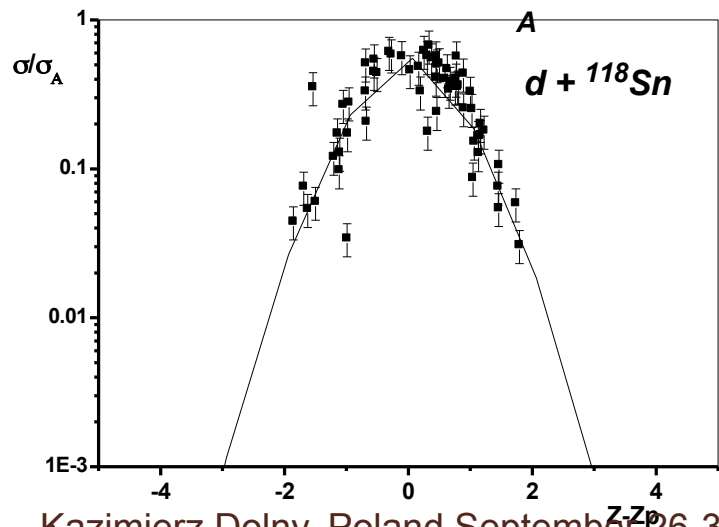
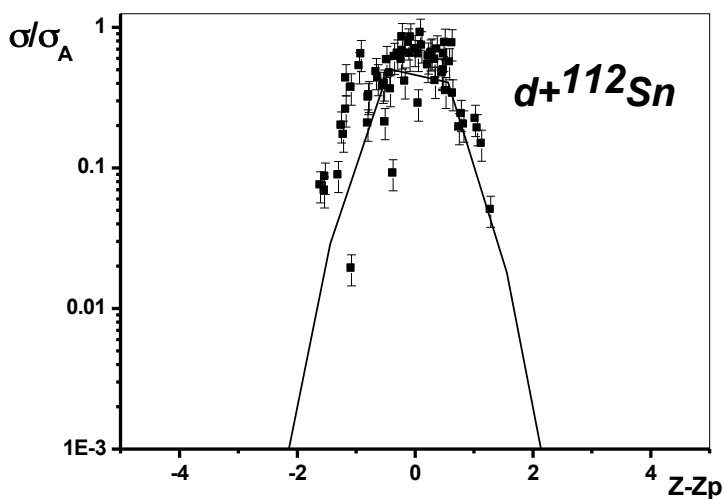
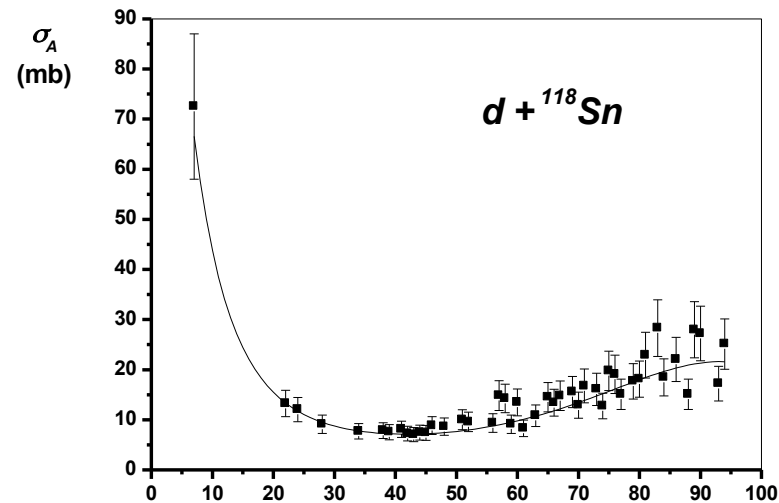
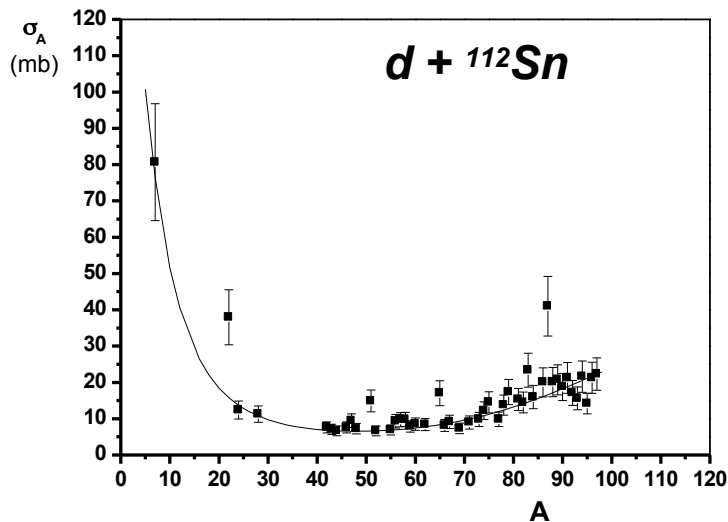


**Table 1.** The parameters of fitting for the targets  $^{112}\text{Sn}$ ,  $^{118}\text{Sn}$ ,  $^{120}\text{Sn}$  и  $^{124}\text{Sn}$

Parameters	$^{112}\text{Sn}$	$^{118}\text{Sn}$	$^{120}\text{Sn}$	$^{124}\text{Sn}$
a1	$5.1 \pm 0.11$	$5.1 \pm 0.2$	$7.31 \pm 0.2$	$4.2 \pm 0.2$
a2	$-0.167 \pm 0.002$	$-0.195 \pm 0.009$	$-0.325 \pm 0.009$	$-0.139 \pm 0.008$
a3	0.0025	$0.0033 \pm 0.00013$	$0.0058 \pm 0.00012$	$0.0026 \pm 0.00012$
a4	$(-10.71 \pm 0.12)10^{-6}$	$(-16.52 \pm 0.64)10^{-6}$	$(-30.39 \pm 0.53)10^{-6}$	$(-14.08 \pm 0.61)10^{-6}$
a5	$-1.54 \pm 0.06$	$-1.49 \pm 0.16$	$-4.14 \pm 0.22$	$-0.82 \pm 0.14$
a6	-0.018	$0.006 \pm 0.004$	$0.115 \pm 0.007$	$-0.018 \pm 0.003$
a7	$(20.4 \pm 0.6)10^{-5}$	$(1.4 \pm 0.3)10^{-5}$	$(-10.5 \pm 0.6)10^{-4}$	$(1.99 \pm 0.2)10^{-4}$
a8	1.7	1.7	1.8	1.7
a9	$0.483 \pm 0.0005$	$0.477 \pm 0.0004$	$0.4619 \pm 0.0005$	$0.4752 \pm 0.0005$
a10	$(-27.7 \pm 0.5)10^{-5}$	$(-29.1 \pm 0.5)10^{-5}$	$(-5.4 \pm 0.5)10^{-5}$	$(-31.8 \pm 0.6)10^{-5}$

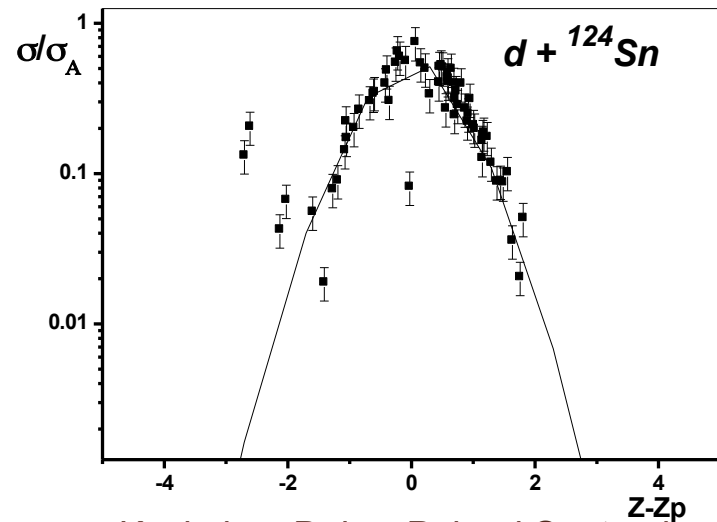
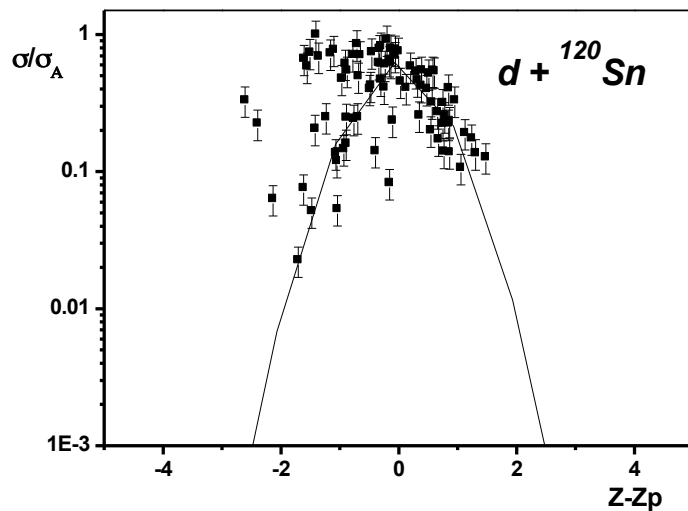
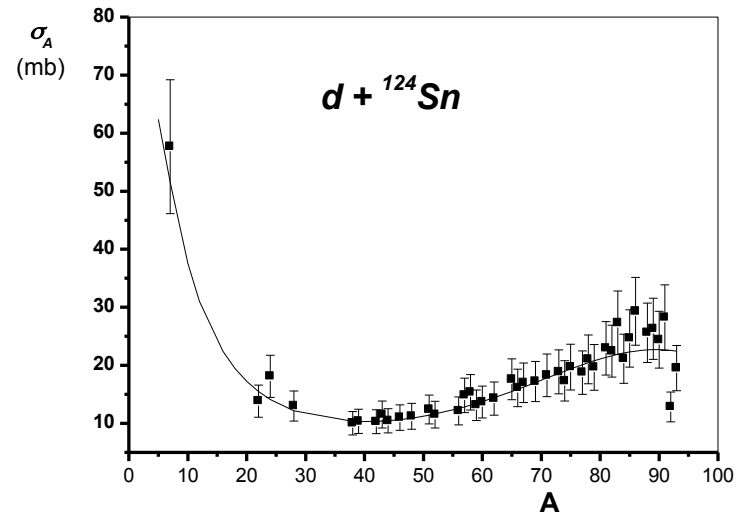
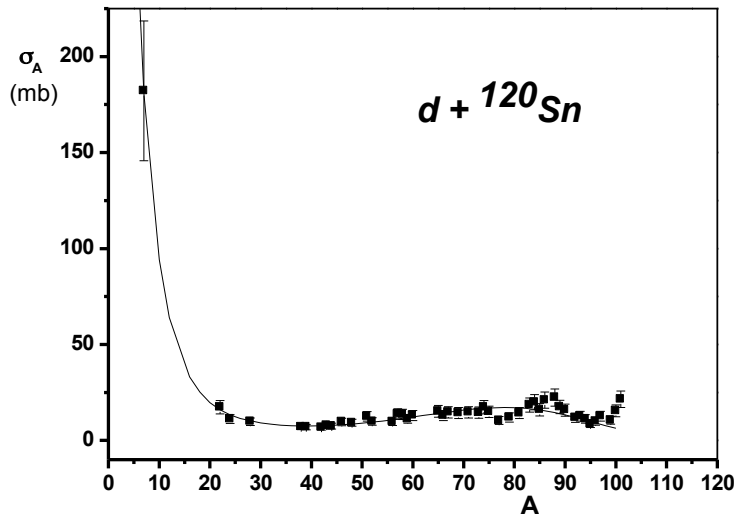


# Mass yield and charge dispersion curves



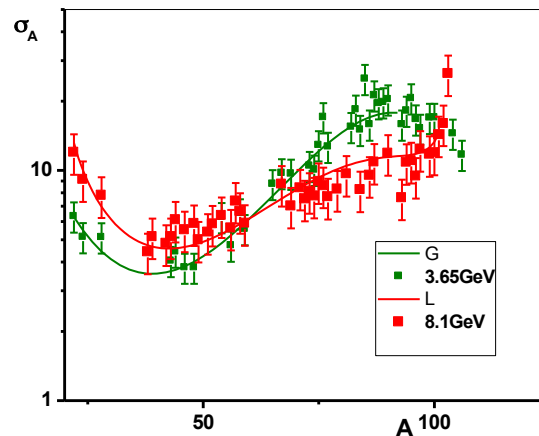
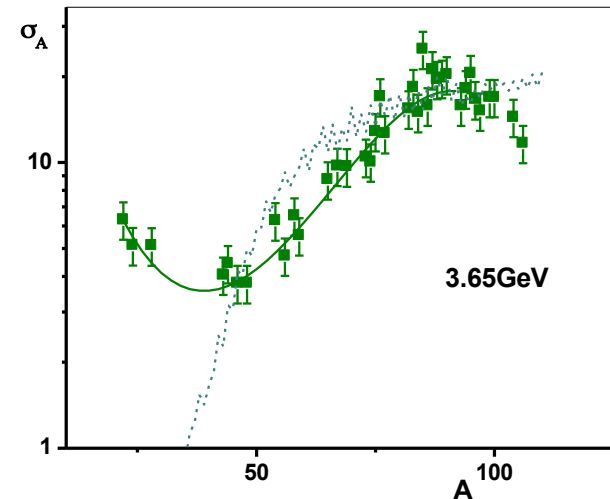
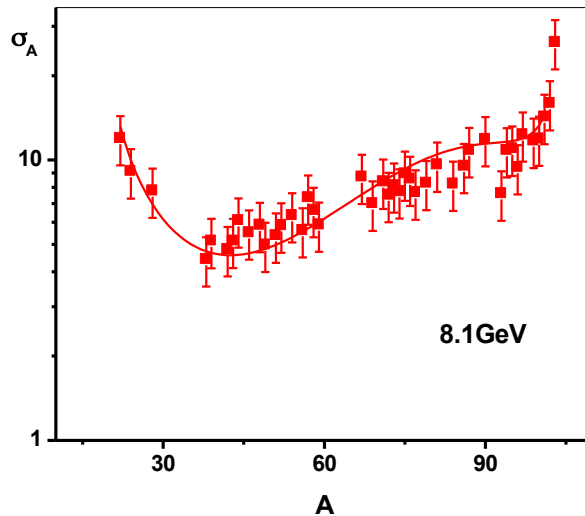


# Mass yield and charge dispersion curves





# Comparison of mass-yield curves for 3.65 GeV and 8.1 GeV protons

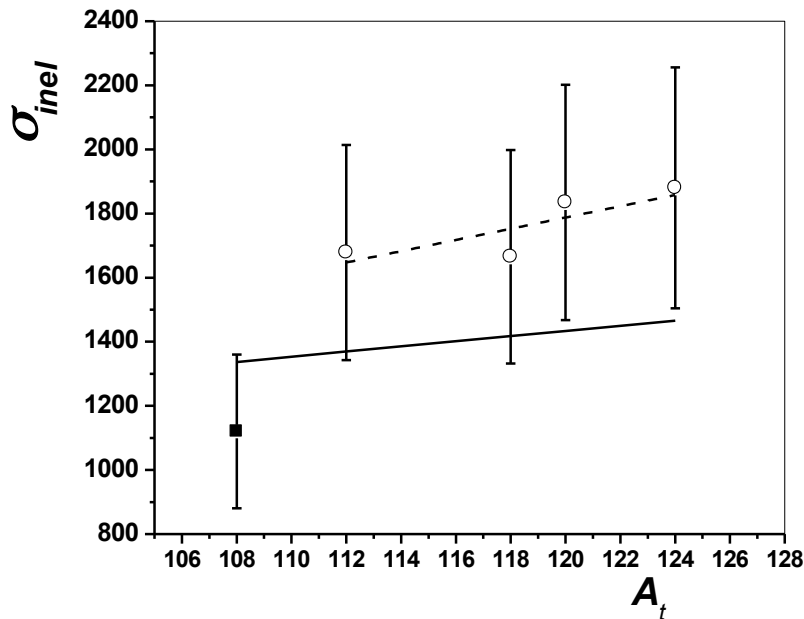


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# Total inelastic cross-sections



Dashed curve is the  $\sigma \approx A^{2/3}$  dependence

$$\sigma(A) = \sum_Z \sigma(A, Z)$$

$$\sigma_{inel} = \sum_A \sigma(A)$$

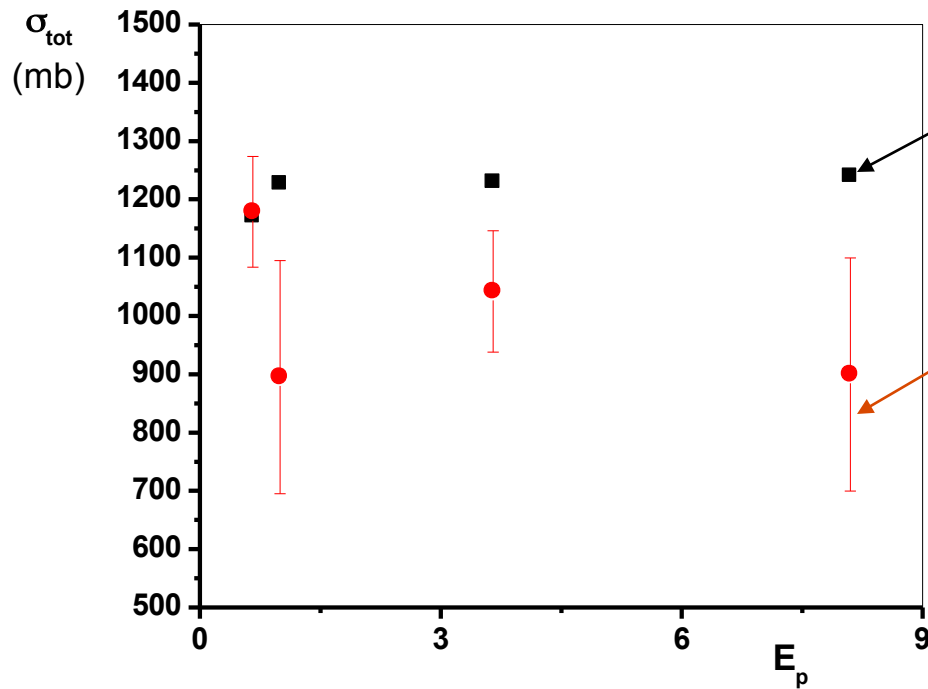
Theoretical estimation made by the formula (H.H.Hekman, D.E.Greiner, P.J.Lindstrom, Phys.Rev.C 17,1735,1978)

$$\sigma_{inel} = \pi r_0^2 [A_B^{1/3} + A_T^{1/3} - b_0 (A_B^{-1/3} + A_T^{-1/3})]^2$$

where  $b_0$  is the overlap parameter,  $A_B$  is the mass number of the beam nucleus and  $A_T$  is the mass number of the target nucleus



# Dependence of inelastic cross sections via energy of protons

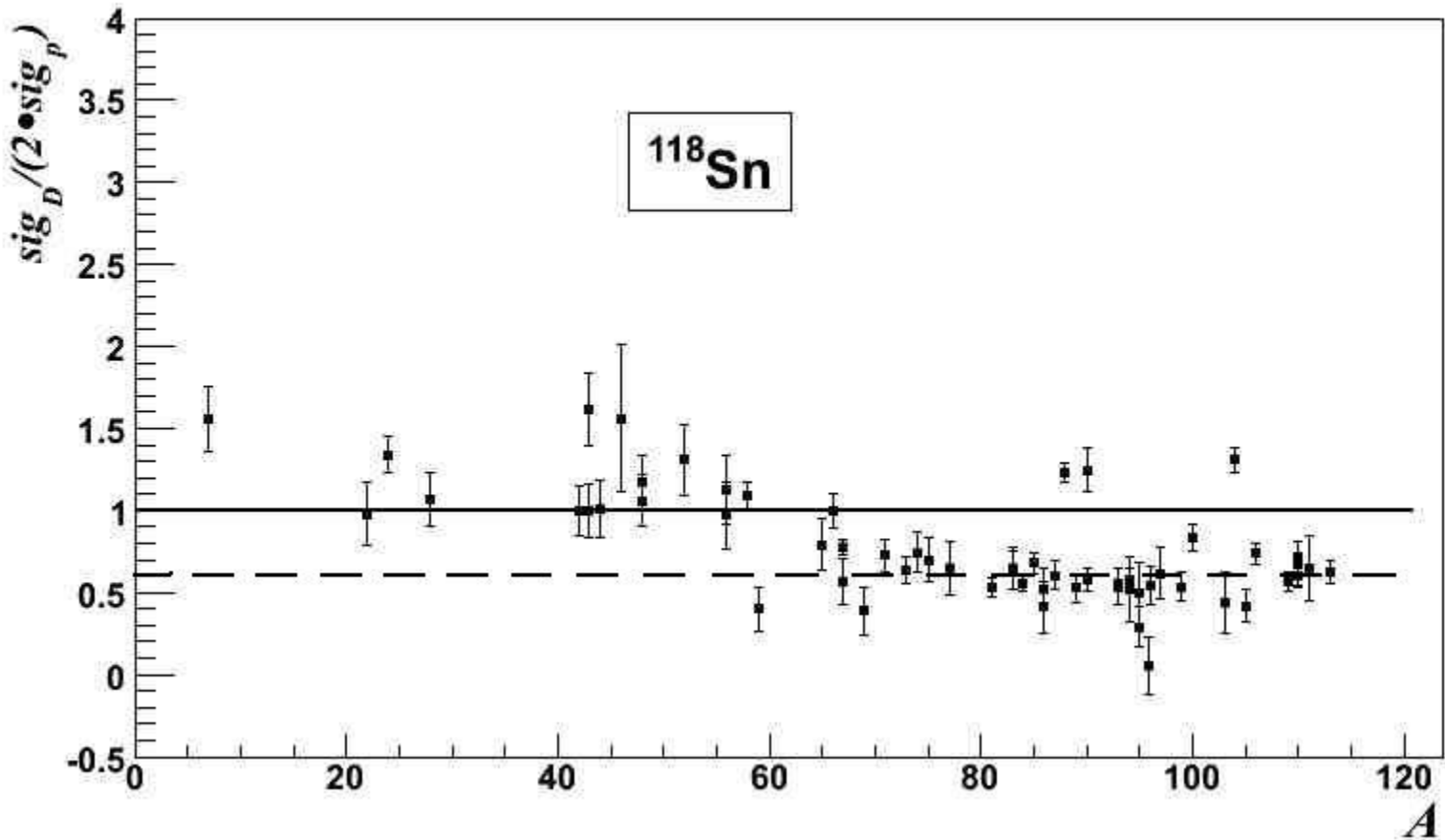


Calculation of cascade evaporation model

Experimental estimations

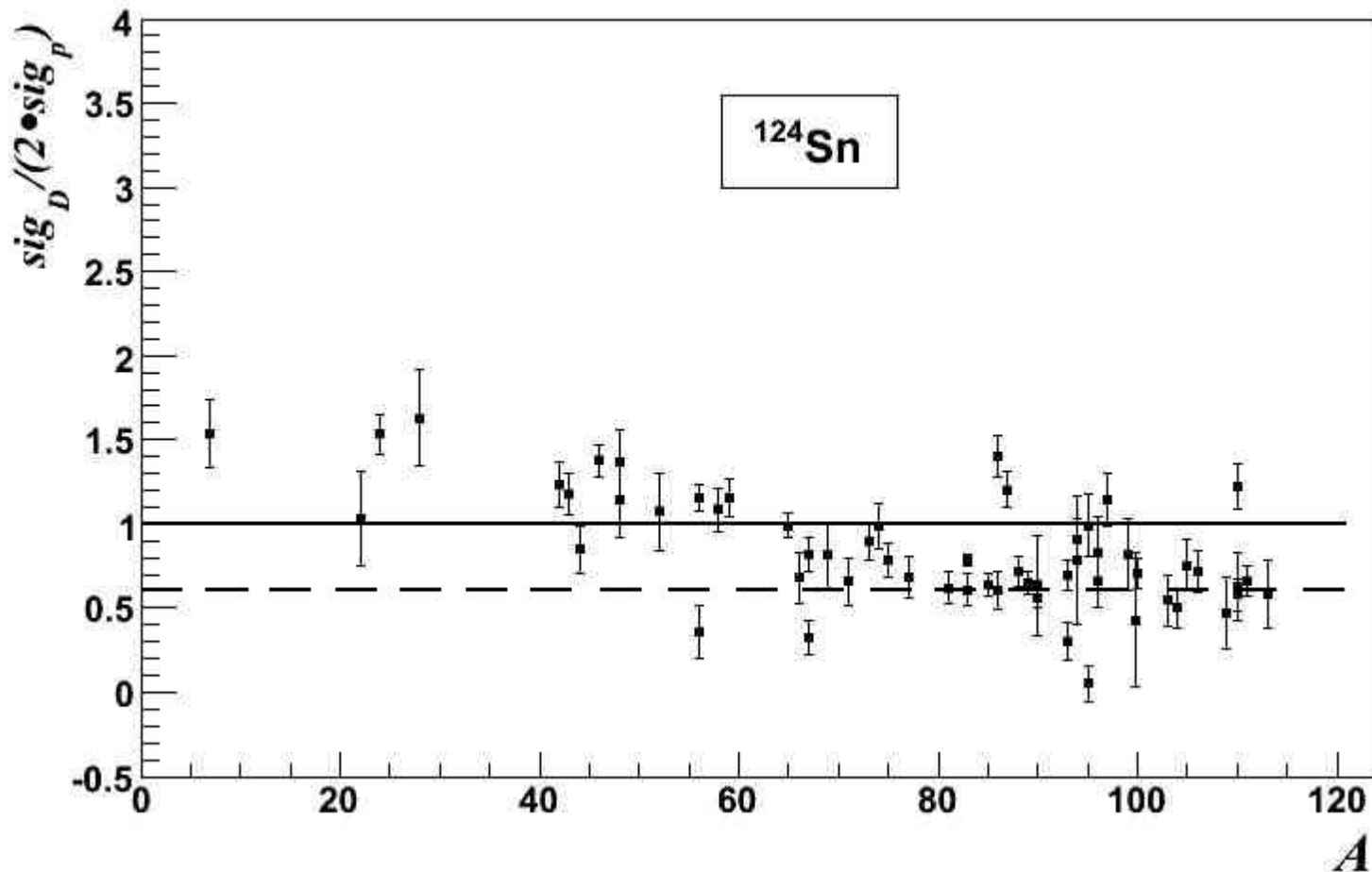


# The dependence of ratio on the mass number of products





# The dependence of ratio on the mass number of products





**Table 2.** The total cross sections of deuteron incident reactions for the targets  $^{112}\text{Sn}$ ,

$^{118}\text{Sn}$  и  $^{124}\text{Sn}$

Targets	$\sigma_{\text{tot}}$ (theor.), mb	$\sigma_{\text{tot}}$ (exp.), mb	$\frac{2\sigma_p}{\sigma_D}$ (theor.)	$\frac{2\sigma_p}{\sigma_D}$ (exp.)	$\Delta$ (theor.), mb	$\Delta$ (exp.), mb
$^{112}\text{Sn}$	1578.34	$1689 \pm 338$	1.7	$1.23 \pm 0.34$	1106.2	$391.0 \pm 109.5$
$^{118}\text{Sn}$	1630.43	$1665 \pm 333$	1.71	$1.14 \pm 0.32$	1150.3	$237.3 \pm 66.4$
$^{124}\text{Sn}$	1681.58	$1880 \pm 376$	1.71	$1.19 \pm 0.33$	1194.6	$204.0 \pm 57.12$

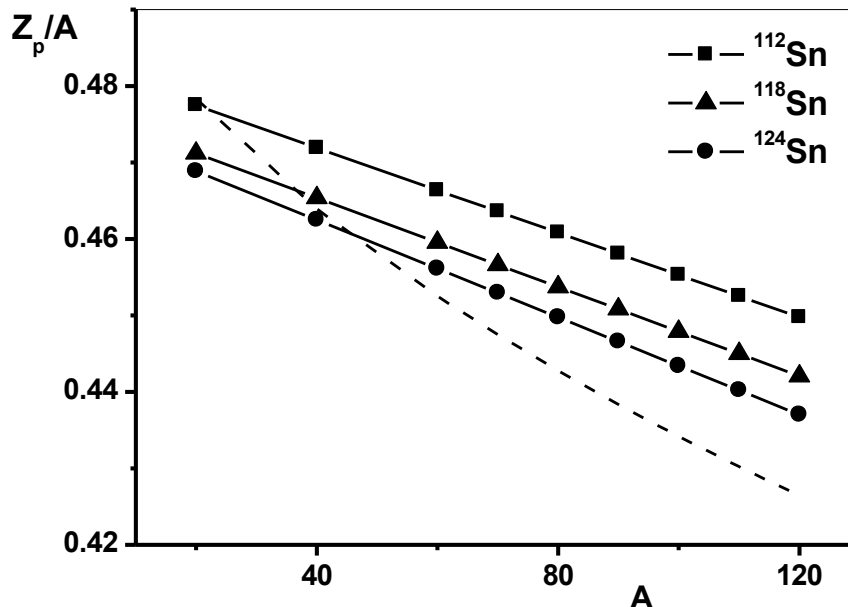
$$\sigma_d^{\text{tot}} = \sigma_p^{\text{tot}} + \sigma_n^{\text{tot}} - \Delta$$



$$\Delta = 2 \cdot \sigma_p^{\text{tot}} - \sigma_d^{\text{tot}}$$



# The dependence of $Z_p/A$ on the mass number of products



- the dotted line marks the position of  $Z_A/A$  more stable charge for a given A.

For the products  $A < 40$  the peak position of the isobaric distribution is on the neutron deficient side of the line of beta stability. And for the rest of the products the peak position lies on the neutron-rich side of the line of beta stability with increasing mass number of the target to move to a more neutron-rich nuclei of the residual.



# Conclusion

- The parameter computed from the experimental data of scattering of fast protons and deuterons on separated tin isotopes do not coincide with the theoretical predictions. Theoretical and experimental ratio of the cross sections for deuteron nuclear reactions to a double proton nuclear reaction cross-section are the same for the reactions of deep spallation.
- The experimental estimates can be used to refine the model representations of nuclear reactions in the above energy and mass regions.



THANK YOU  
FOR YOUR  
ATTENTION!