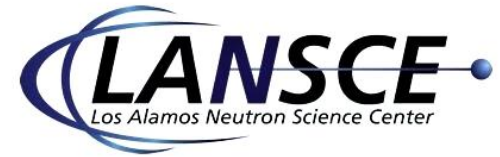
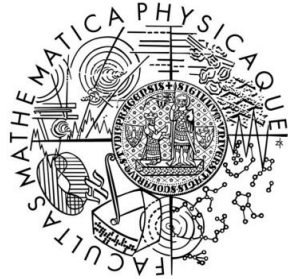


# Scissors Mode of Gd nuclei studied from resonance neutron capture at DANCE



**Jiří Kroll**

**for DANCE collaboration**

**Faculty of Mathematics and Physics, Charles University, Prague**

# Outline

- Motivation
- DANCE experiment at LANSCE
- DICEBOX simulations of gamma decay
- Main results
- Conclusions

# Scissors mode (SM) in $M1$ PSF

SM proposed in deformed nuclei by theorists in late 70's:

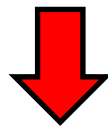
*N. Lo Iudice and F. Palumbo, PRL **53** (1978) 1532*

*R. R. Hilton, in Proceedings of the International Conference on Nuclear Structure, Dubna, 1976*

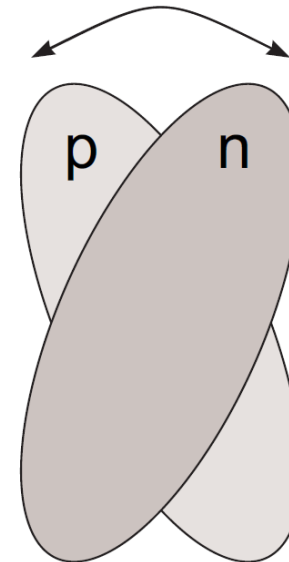
SM experimentally confirmed in high-resolution  $(e,e')$  experiments on rare-earth nuclei

*D. Bohle et al., Phys. Lett. **B137** (1984) 27*

SM for the GS transitions in even-even nuclei studied in detail in the 80's and 90's mainly using the  $(\gamma,\gamma')$  experiments



In well-deformed even-even nuclei  
 $E_{SM} \approx 3$  MeV and  $\Sigma B(M1) \approx 3 - 3.5 \mu_N^2$ .



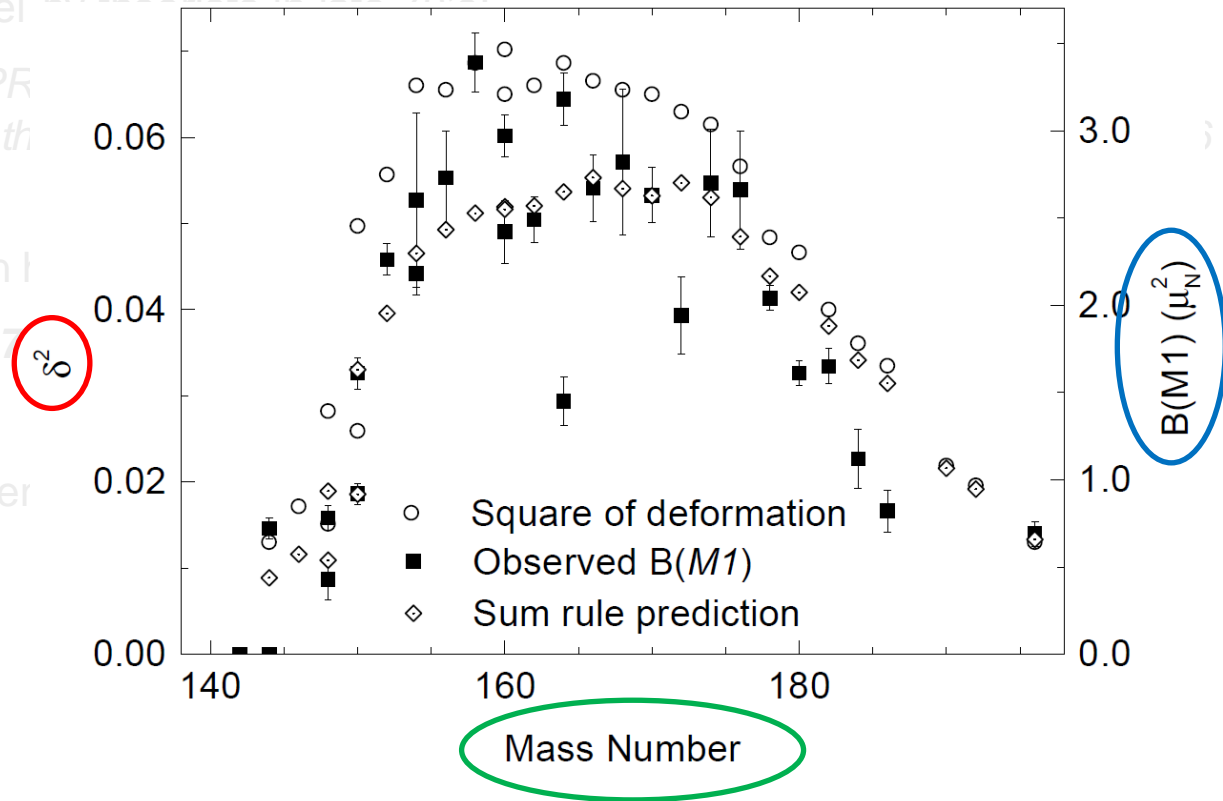
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*N. Lo Iudice and F. Palumbo, PR*  
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*D. Bohle et al., Phys. Lett. B137*

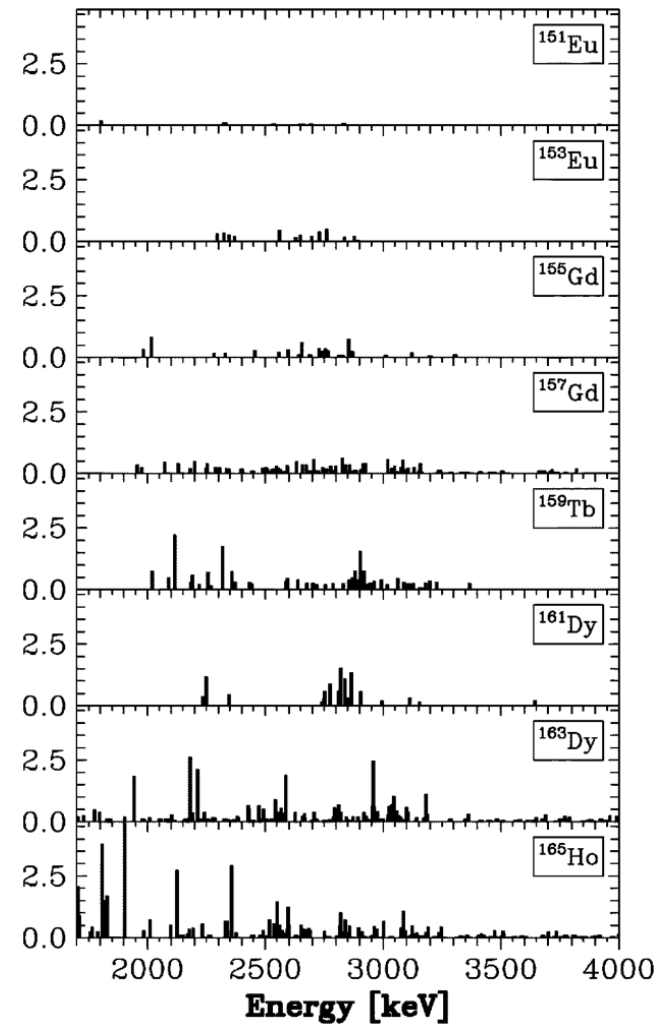
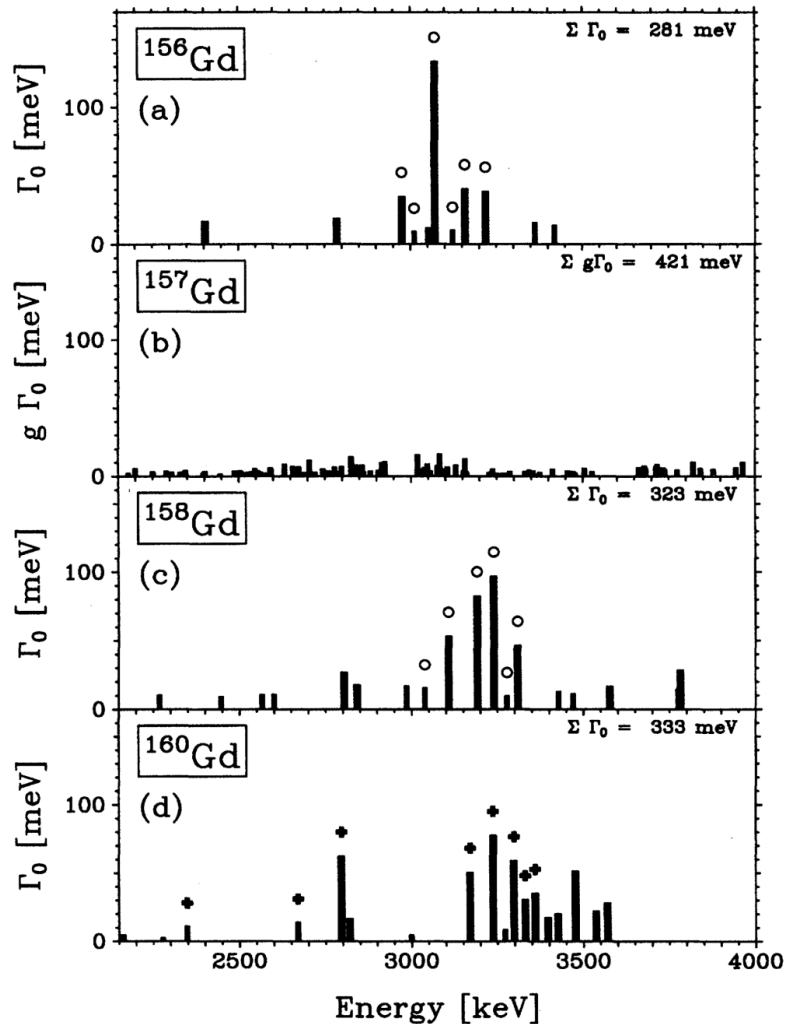
SM for the GS transitions in even-even nuclei using the  $(\gamma, \gamma')$  experiments



Exploiting data from  $(\gamma, \gamma')$  – a sum rule was derived by *N. Lo Iudice and A. Richter, Phys. Lett. B304 (1993) 193*

$$\sum B(M1) \uparrow \approx 0.0042 \frac{4NZ}{A^2} E_{SC} A^{5/3} (g_p - g_n)^2 \delta^2 [\mu_N^2]$$

# Scissors mode (SM) in $M1$ PSF

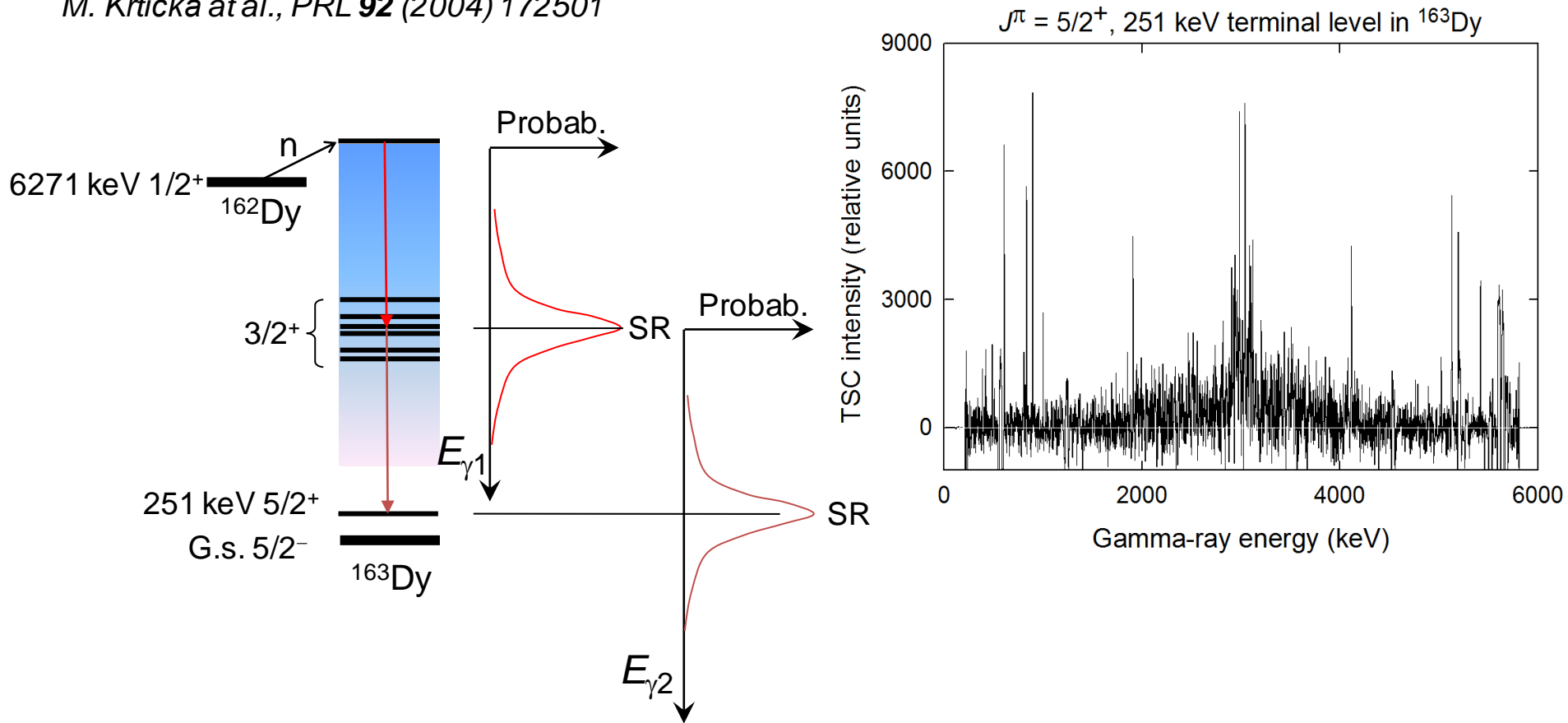


In odd nuclei  $\Sigma B(M1, \text{odd}) \approx 1/3 \Sigma B(M1, \text{e-e})$  from  $(\gamma, \gamma') \leftarrow$  problems with high NLD

# Scissors mode in $M1$ PSF observed from $(n,\gamma)$ reactions

SM on the excited states was observed for the first time in TSC experiment with  $^{163}\text{Dy}$  in 1995

*M. Krtička et al., PRL 92 (2004) 172501*



To get TSC spectra for separate final levels, the sum coincidence method was used  
*J. Honzátko et al., NIM A376 (1996) 434 .*

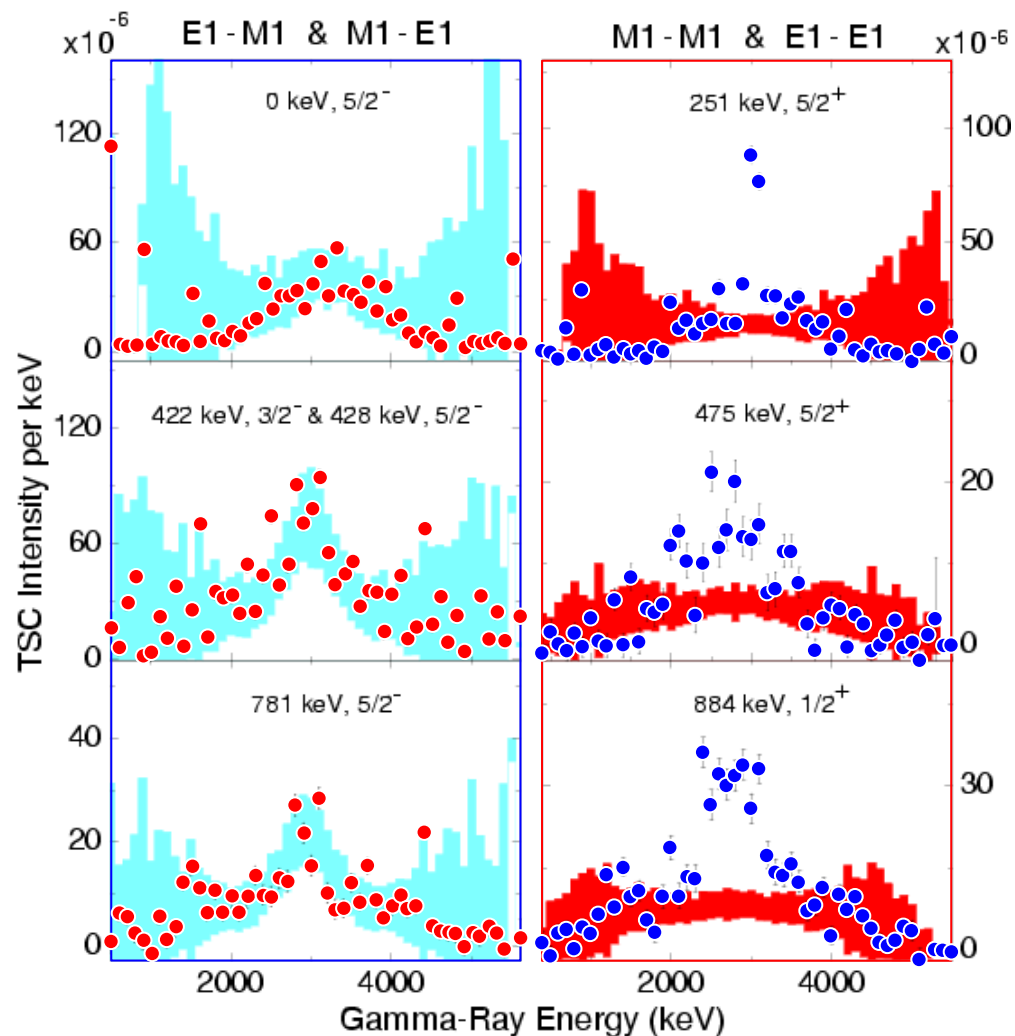
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SM on the excited states was observed for the first time in TSC experiment with  $^{163}\text{Dy}$

*M. Krtička et al., PRL 92 (2004) 172501*



**Simulation assumption:**  
**SM is built only on the states below the energy of 2.5 MeV**



Corridors represent the region of residual Porter-Thomas fluctuations.

# Scissors mode in $M1$ PSF observed from $(n,\gamma)$ reactions

SM on the excited states was observed for the first time in TSC experiment with  $^{163}\text{Dy}$

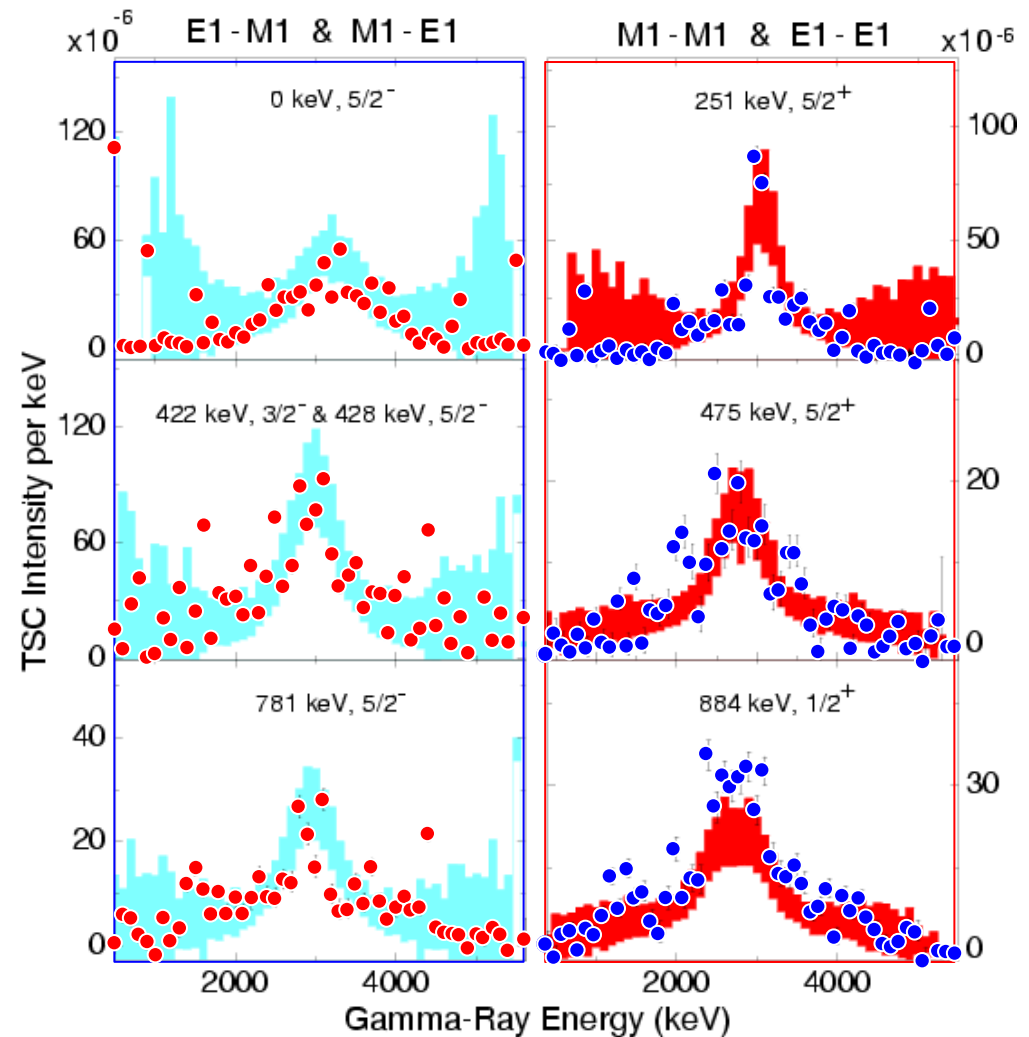
*M. Krtička et al., PRL 92 (2004) 172501*

■  $\pi_f = +$   
■  $\pi_f = -$

} DICEBOX Simulations

$E_{\text{SM}} = 3.0 \text{ MeV}$ ,  $\Gamma_{\text{SM}} = 0.6 \text{ MeV}$  and  
 $\Sigma B(M1)\uparrow \approx 6 \mu_N^2$

**Simulation assumption:**  
**SM is built on all  $^{163}\text{Dy}$  levels**

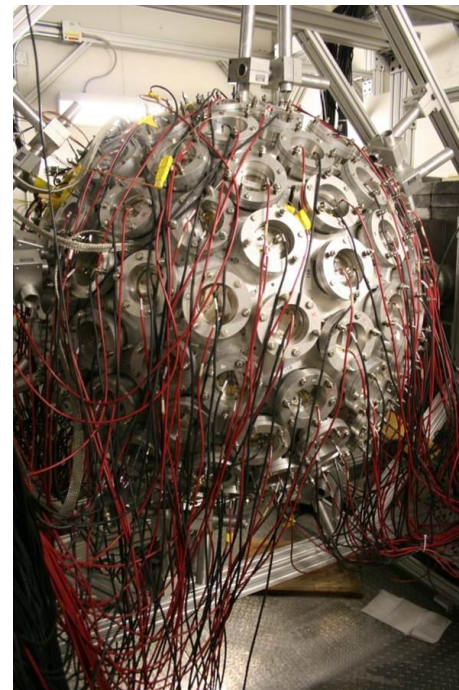
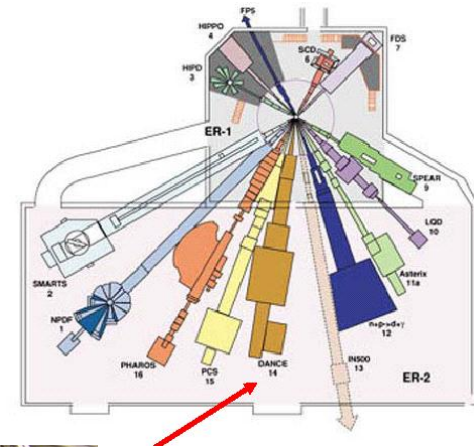


Corridors represent the region of residual Porter-Thomas fluctuations.



# DANCE experiment at LANSCE

- Moderated W target gives “white” neutron spectrum  $\approx 14$  n’s / proton
- Repetition rate 20 Hz
- Pulse width  $\approx 125$  ns
- DANCE detector is placed on a 20m long flight path /  $\approx 1$  cm beam after collimation
- DANCE consists of 160 BaF<sub>2</sub> crystals

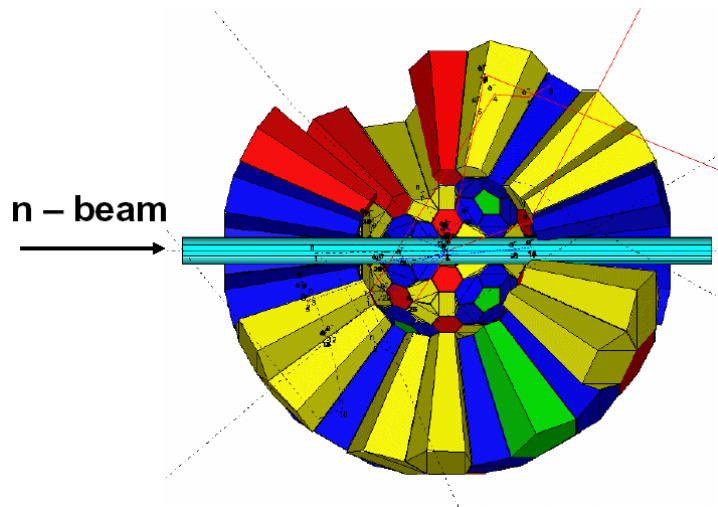
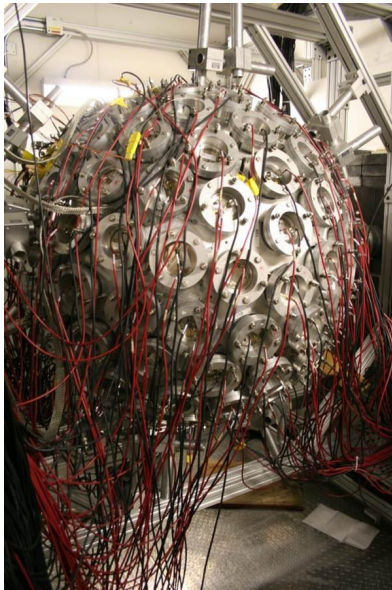
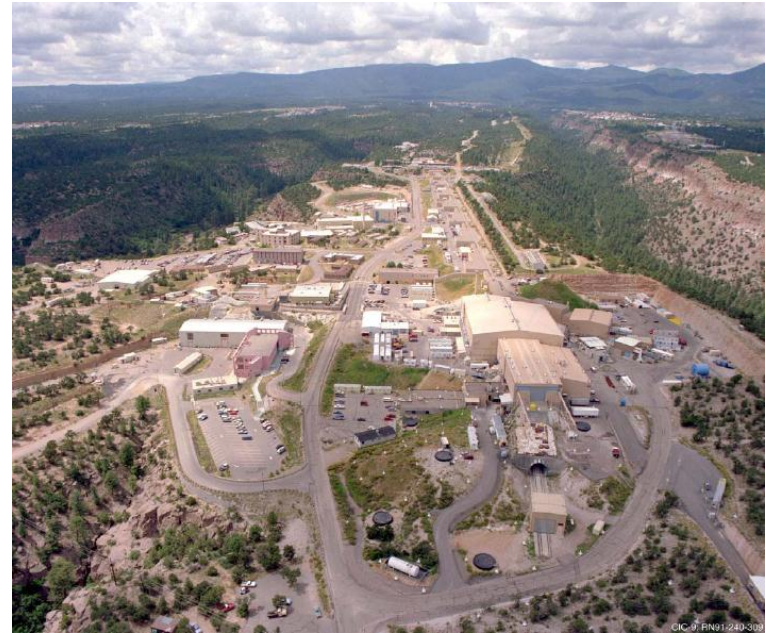


# DANCE experiment at LANSCE

With a DANCE detector we have measured stable Gd isotopes

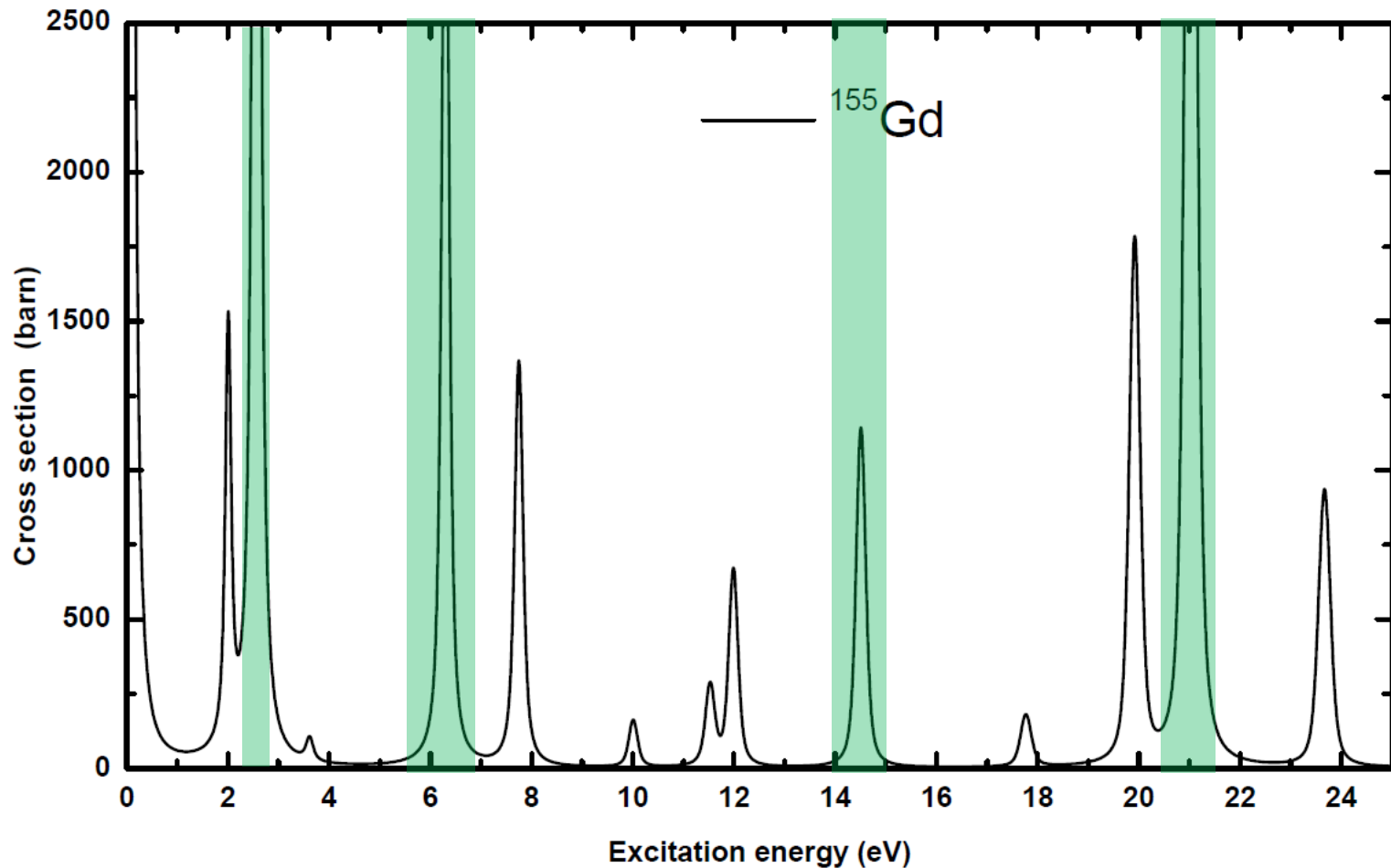
$^{153}\text{Gd}$ ,  $^{155}\text{Gd}$ ,  $^{156}\text{Gd}$ ,  $^{157}\text{Gd}$ ,  $^{158}\text{Gd}$ ,  $^{159}\text{Gd}$

mainly to get information about the Photon Strength Functions (PSFs)



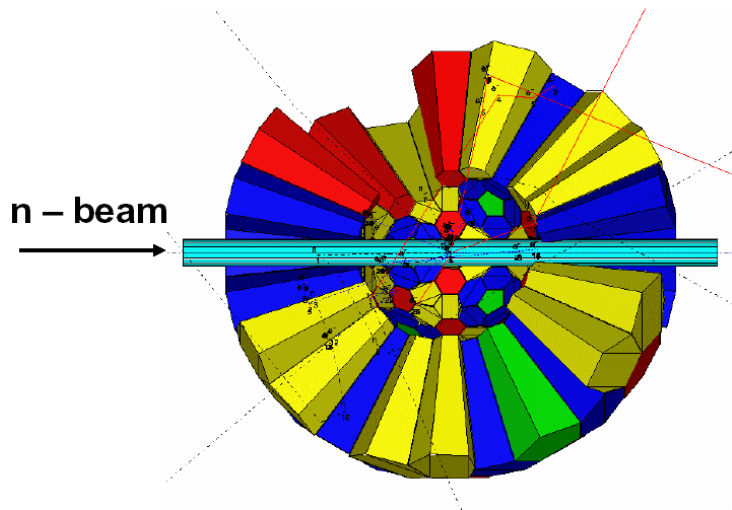
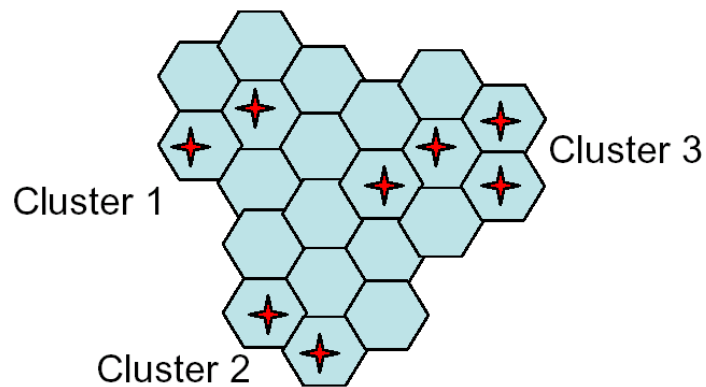
# DANCE experiment at LANSCE

- **TOF method** → neutron capture at strong isolated resonances
- The background for these strong resonances is very small (can be subtracted)

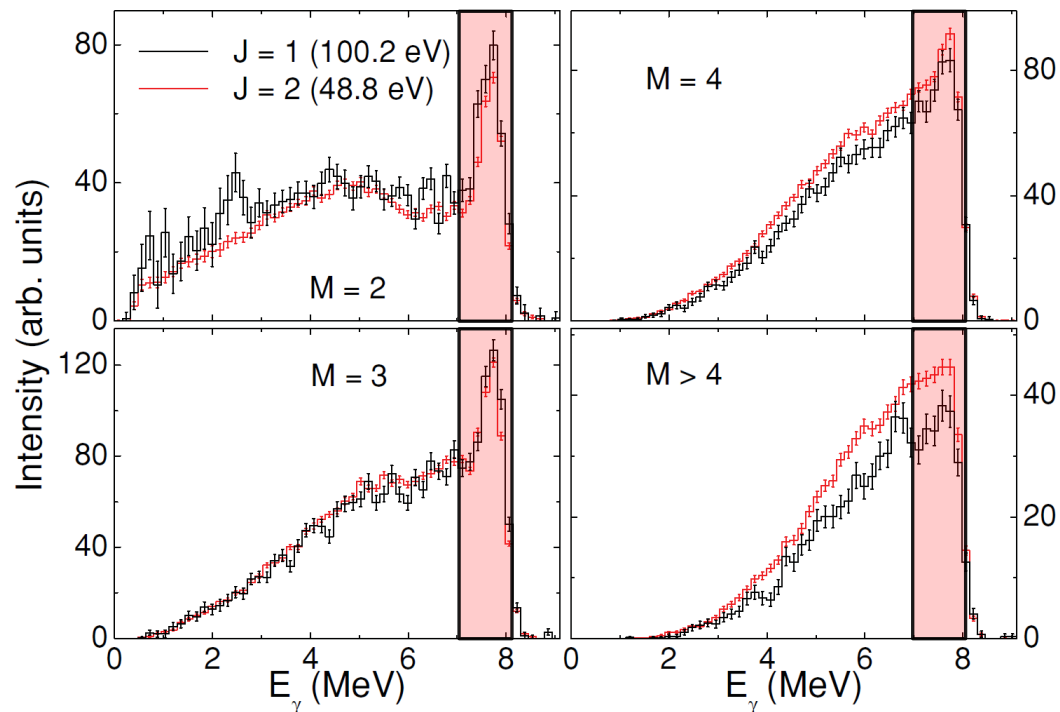




# DANCE experiment – data processing



Sum spectra for different multiplicities

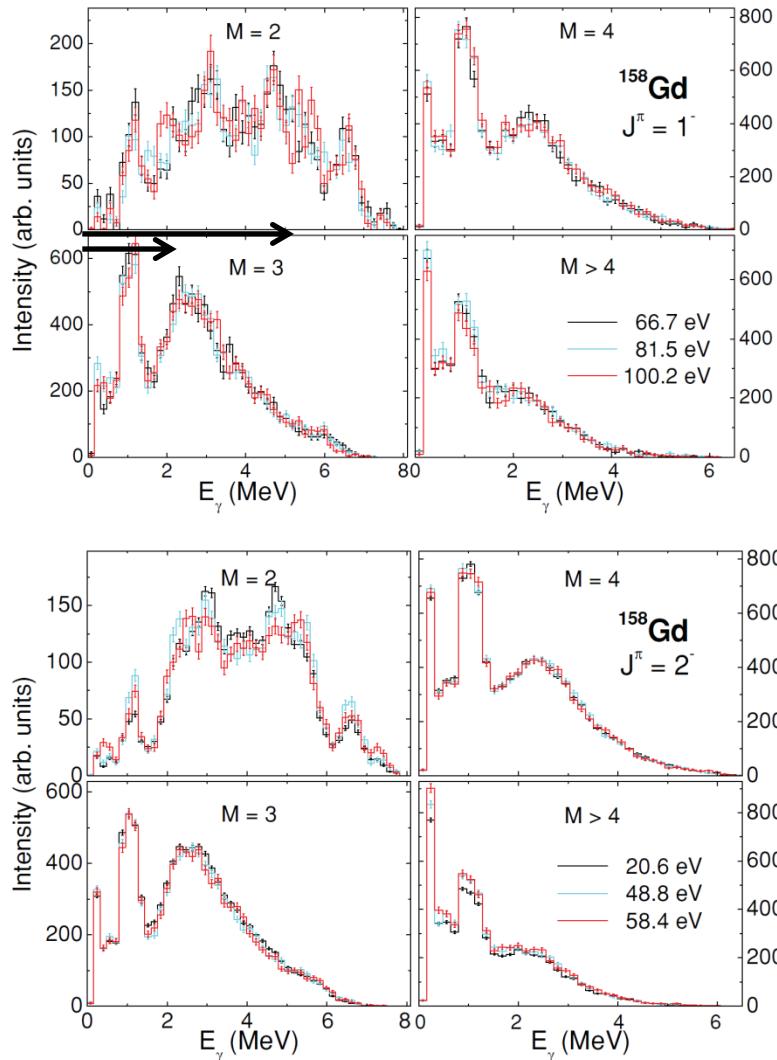


*M. Heil et al., NIM Phys. Res. A* **459**, 229 (2001).  
*R. Reifarth et al., NIM Phys. Res. A* **531**, 530 (2004).

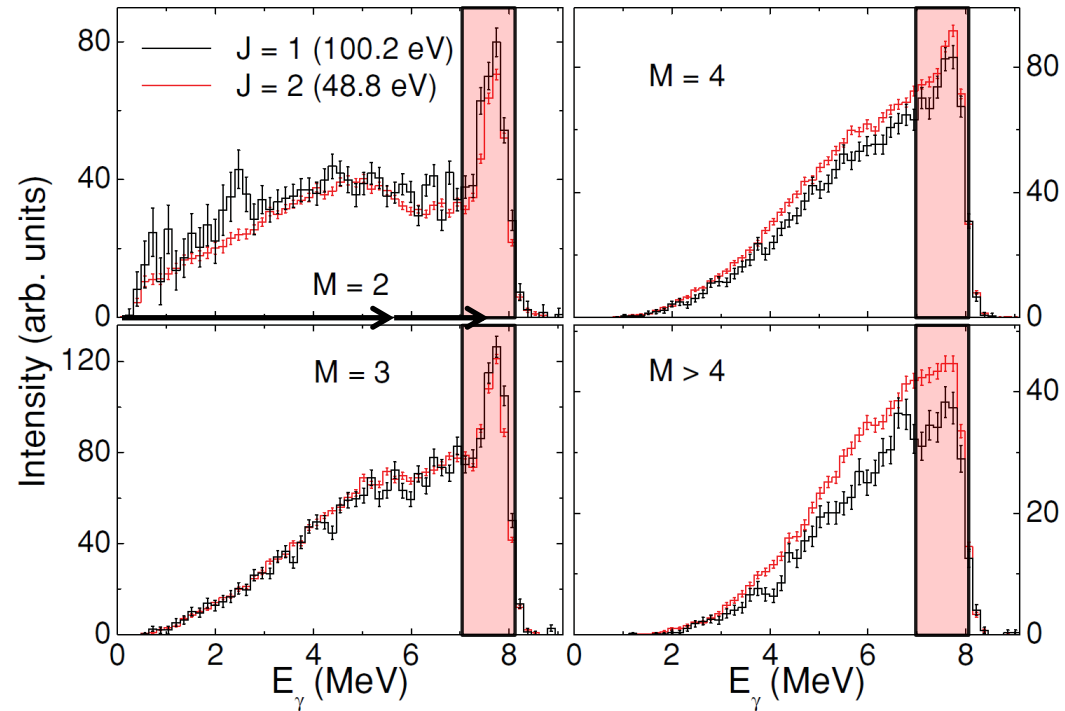
# DANCE experiment – data processing

What do we really compare with the outputs of simulations?

Experimental MSC spectra



Sum spectra for different multiplicities



# Simulations of gamma decay – DICEBOX

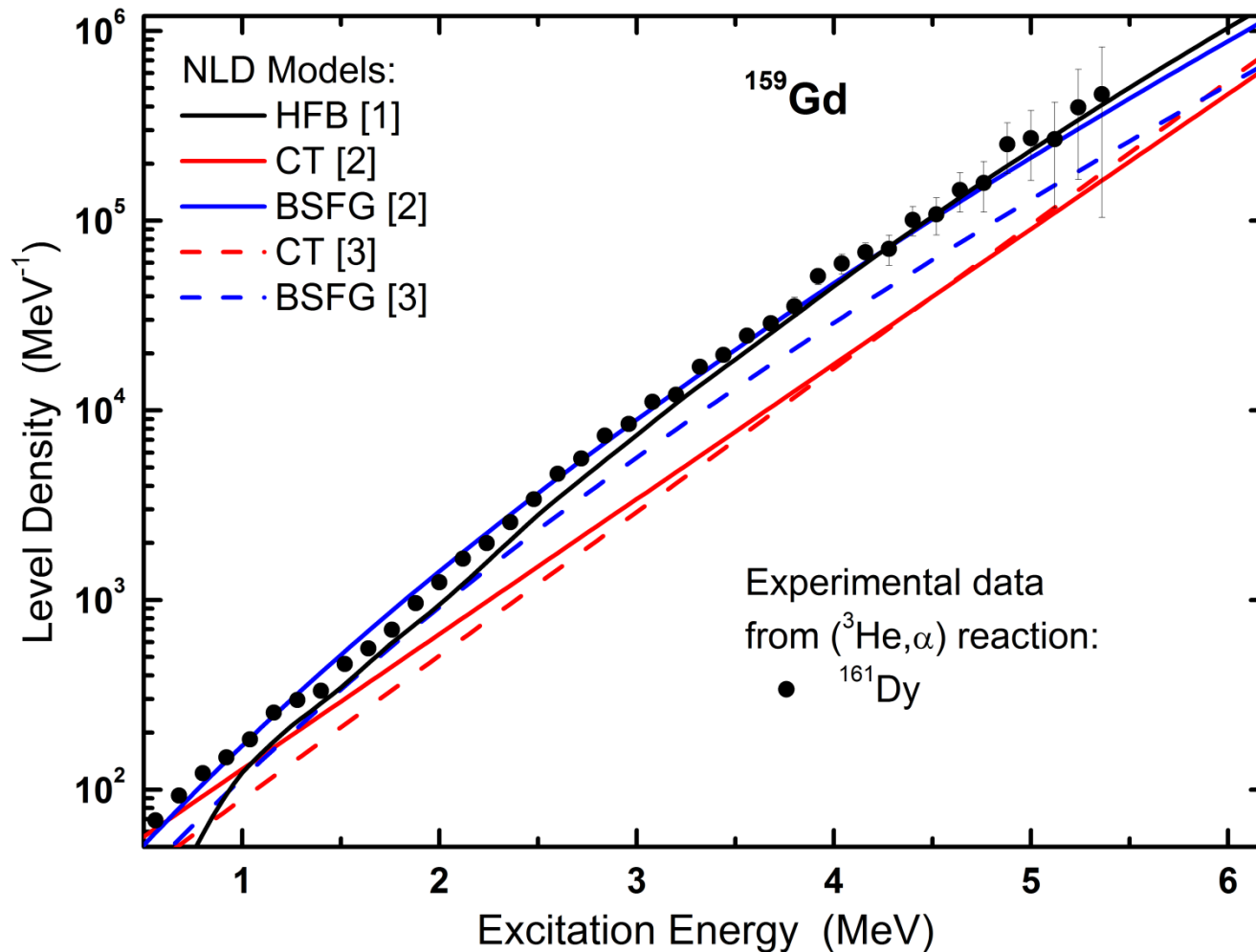
1. Below a **critical energy**  $E_{crit}$  the energies  $E$ , spins  $J$ , parities  $\pi$  and the decay properties of all levels are taken from known data

# Simulations of gamma decay – DICEBOX

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2. Above the critical energy  $E_{crit}$  the energies  $E$ , spins  $J$  and parities  $\pi$  of levels are obtained by random discretization of an *a priori* known level density

$$\rho(E_i, J_i, \pi_i) \text{ Level density}$$

# Simulations of gamma decay – NLD



[1] R. Capote *et al.*, Nucl. Data Sheets **110**, 3107 (2009).

[2] T. von Egidy and D. Bucurescu, Phys. Rev. **C72**, 044311 (2005).

[3] T. von Egidy and D. Bucurescu, Phys. Rev. **C80**, 054310 (2009).



# Simulations of gamma decay – DICEBOX

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$$\rho(E_i, J_i, \pi_i) \text{ Level density}$$

3. **Partial radiation widths**  $\Gamma_{if}$  for transitions between initial (i) and final (f) levels are generated according to the formula:

$$\Gamma_{if} = \sum_{XJ} y_{ifXJ}^2 (E_i - E_f)^{2J+1} \frac{f^{(XJ)}(E_i - E_f)}{\rho(E_i, J_i, \pi_i)}$$

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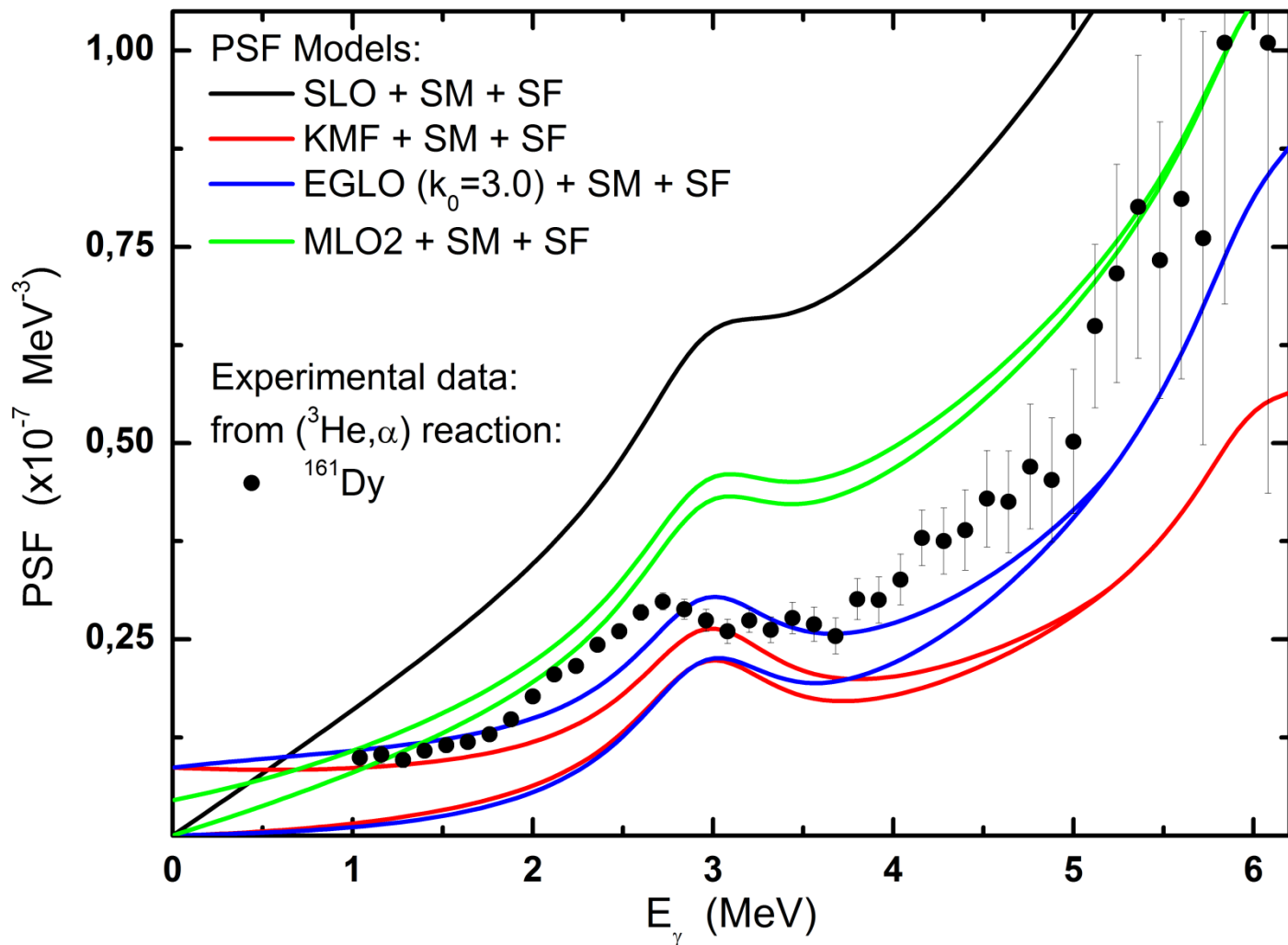
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3. **Partial radiation widths**  $\Gamma_{if}$  for transitions between initial (i) and final (f) levels are generated according to the formula:

$$\Gamma_{i\gamma f} = \sum_{XJ} y_{ifXJ}^2 (E_i - E_f)^{2J+1} \frac{f^{(XJ)}(E_i - E_f)}{\rho(E_i, J_i, \pi_i)}$$

PSFs

# Simulations of gamma decay – PSFs



The energy of the SM is 3.0 MeV, damping width is 1.0 MeV and the strength  $\Sigma B(M1, 2.7\text{-}3.7)\uparrow \approx 3.39 \mu_N^2$ .

# Simulations of gamma decay – DICEBOX

1. Below a **critical energy**  $E_{crit}$  the energies  $E$ , spins  $J$ , parities  $\pi$  and the decay properties of all levels are taken from known data
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PSFs

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P-T fluctuations                      PSFs

# Simulations of gamma decay – DICEBOX

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P-T fluctuations                      PSFs

4. Partial radiation widths  $\Gamma_{i\gamma f}$  for different initial and/or final levels are statistically independent.

# Simulations of gamma decay – DICEBOX

Nuclear Realization:

10<sup>6</sup> energy levels

10<sup>12</sup>  $\Gamma_{i\gamma f}$

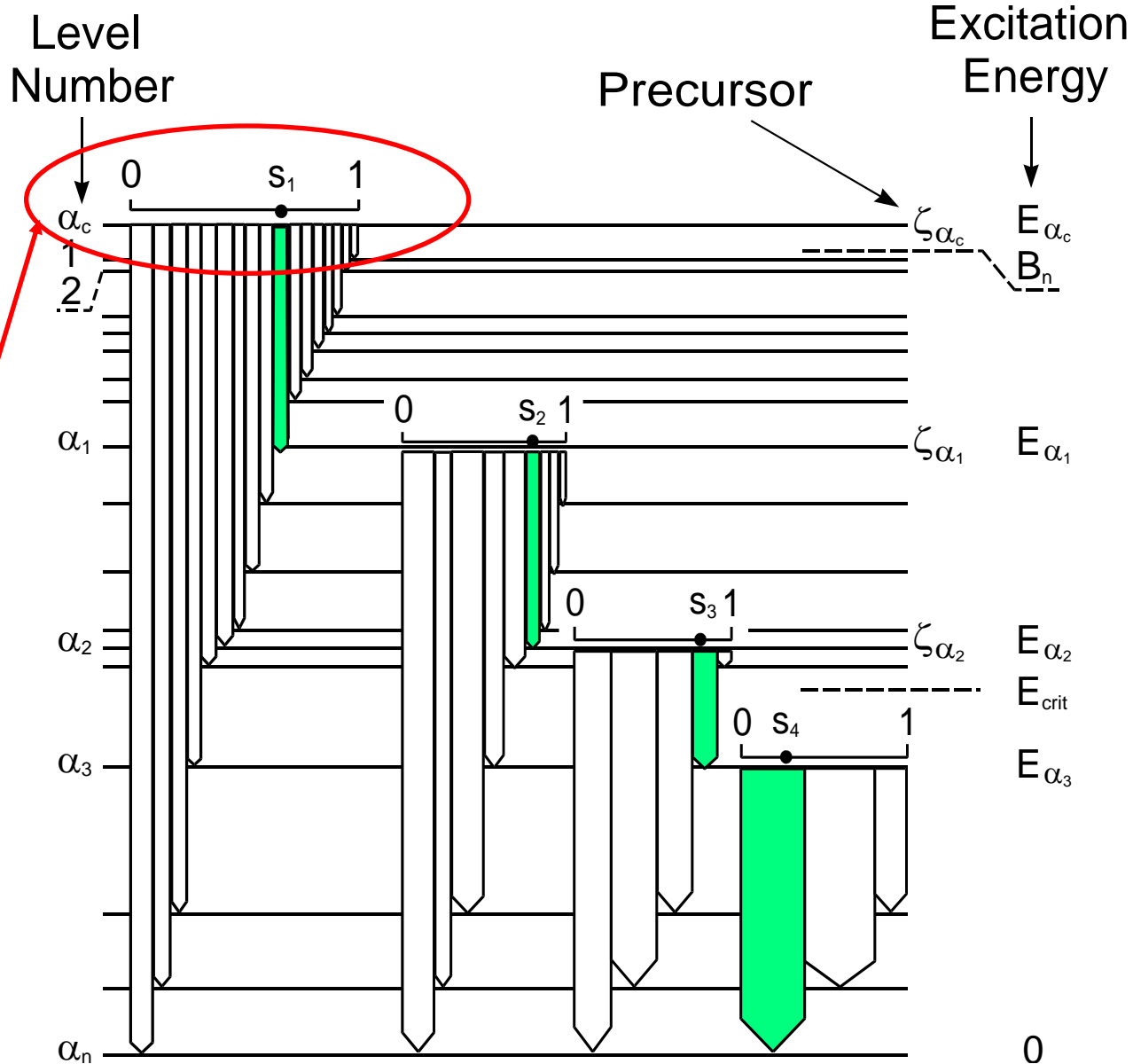
System of precursors

P-T fluctuations

$$P(x)dx = \frac{1}{\sqrt{2\pi x}} e^{-x/2} dx$$

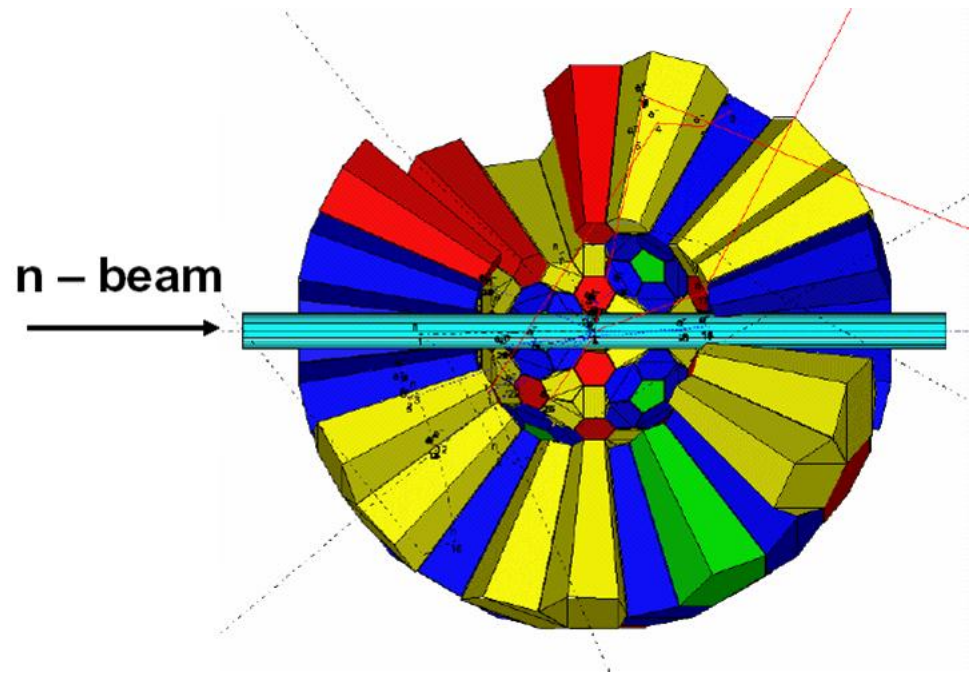
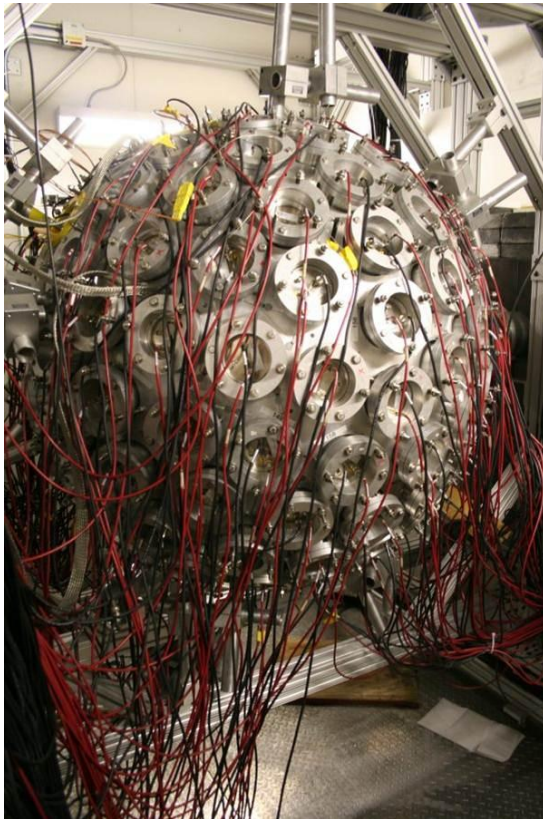
$$x = \Gamma_{i\gamma f} / \bar{\Gamma}$$

F. Bečvář, NIM A417  
(1998) 434



# Detector response – Geant4

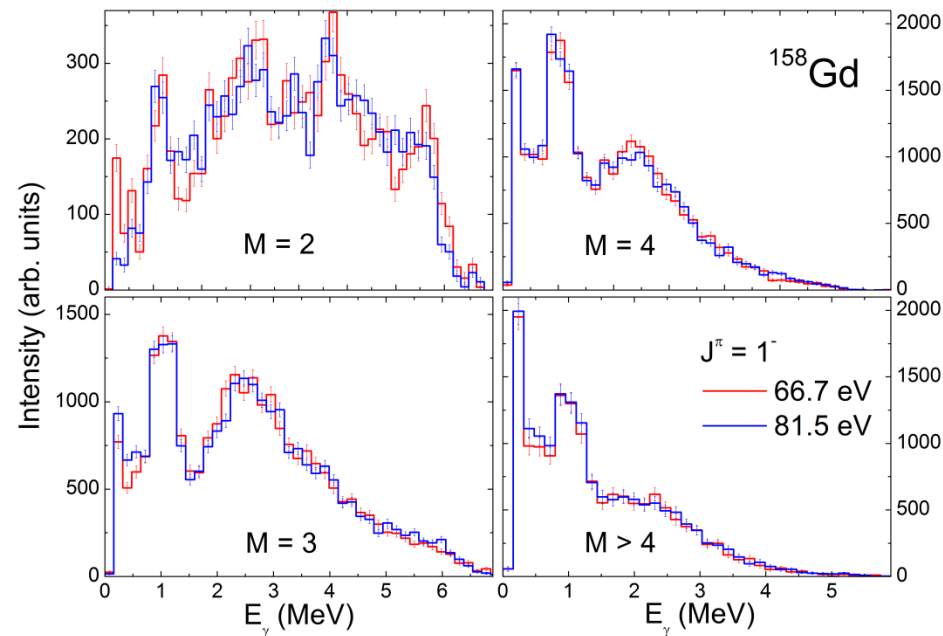
- The outputs of DICEBOX simulations are transformed to the form of Geant4 input.
- Simulations of detector response include the exact geometry and chemical composition (regular and irregular pentagonal and hexagonal  $\text{BaF}_2$  crystals), all shielding, aluminium beamline, radioactive target holder, etc.



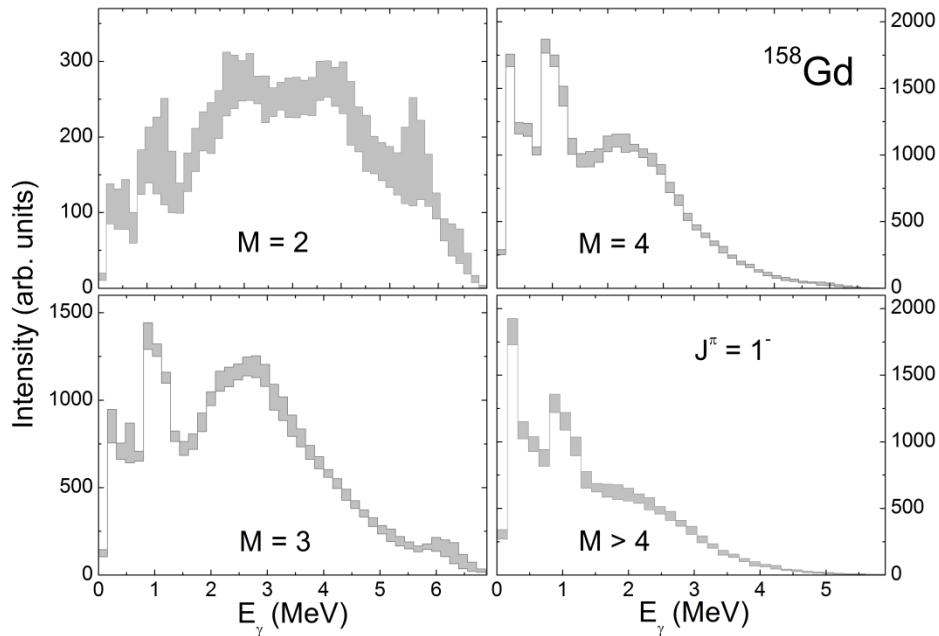


# Comparison of experimental data with the outputs of simulations

- To get information on PSFs and LD we compare experimental data with outputs of simulations.

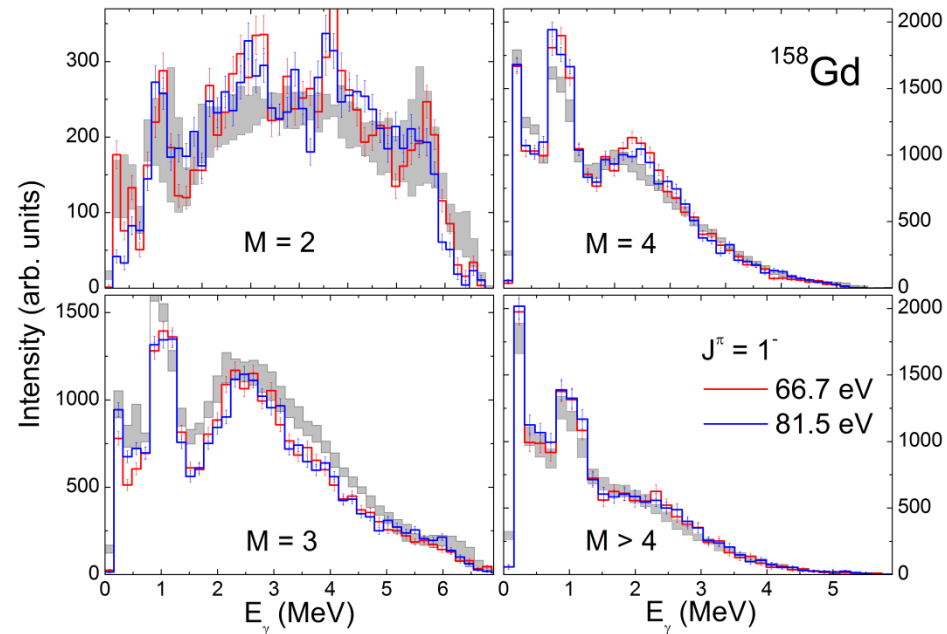
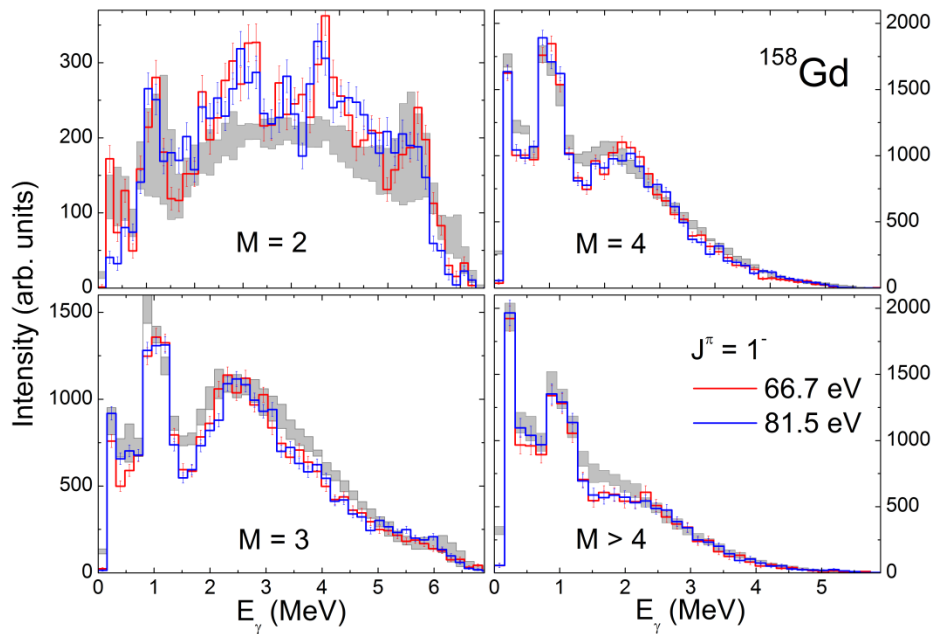


Experimental MSC spectra for two different resonances with  $J^\pi = 1^-$



Simulated MSC spectra produced by DICEBOX and Geant4 (grey corridors are consequence of Porter-Thomas fluctuations)

# SM in even nuclei



Simulation assumption:

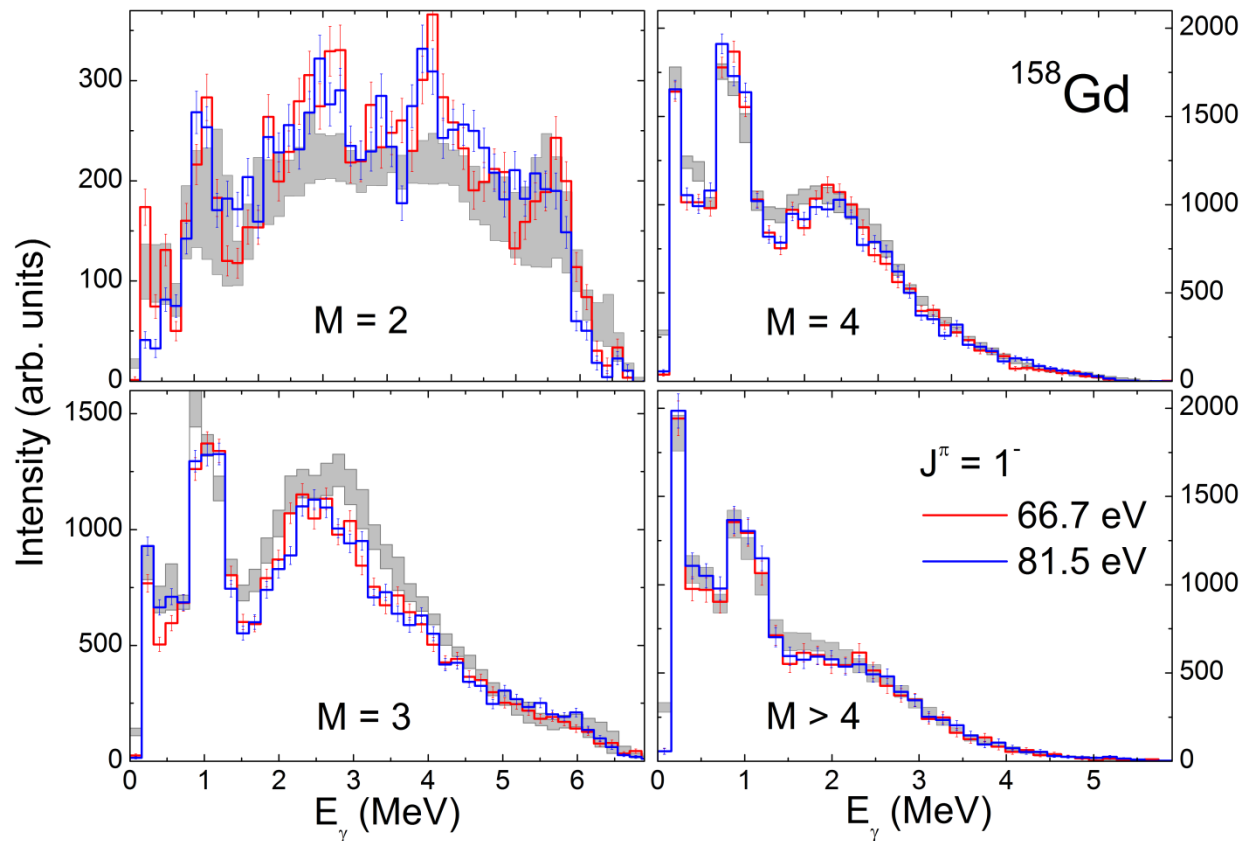
KMF + **SP** + SP + BSFG(1)

**E1 M1 E2 LD**

Simulation assumption:

KMF + **SF** + **SP** + SP + BSFG(1)

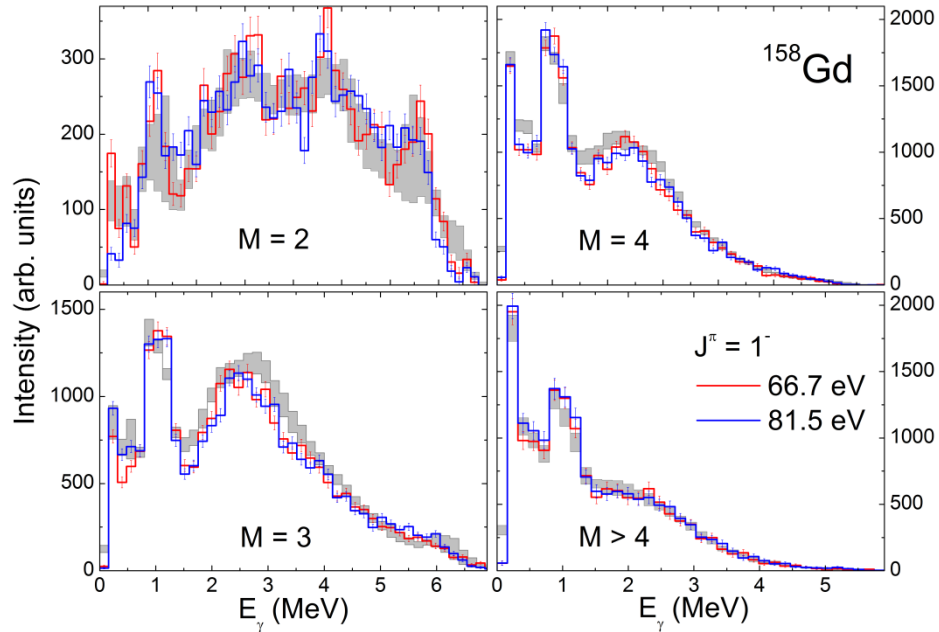
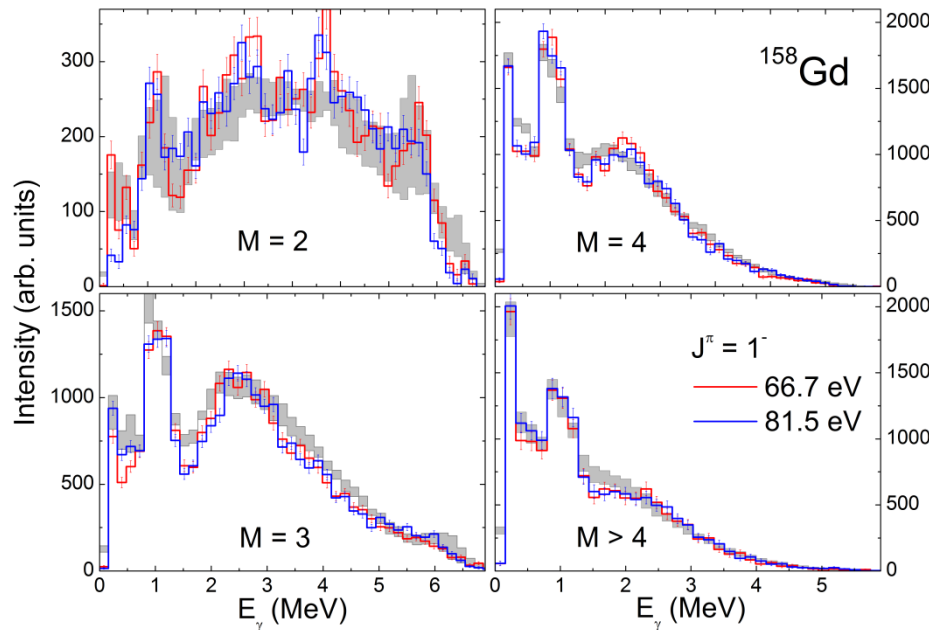
# SM in even nuclei



Simulation assumption:  
KMF + RS + **SF** + **SP** + SP + BSFG(1)

RS parametrization:  
 $E_{\text{RS}} = 3.0 \text{ MeV}$ ,  $\Gamma_{\text{RS}} = 1.0 \text{ MeV}$ ,  
 $\Sigma B(E1, \text{RS}) \approx 2.0 \mu_N^2$

# SM in even nuclei



$^{158}\text{Gd}$  simulation assumption:

KMF + **SM** + **SF** + **SP** + SP + BSFG(1)

$E_{\text{SM}} = 3.0 \text{ MeV}, \Gamma_{\text{SM}} = 1.0 \text{ MeV},$

$\Sigma B(M1, \text{SM}) \approx 2.0 \mu_N^2$

**SM postulated only on the GS**

$^{158}\text{Gd}$  simulation assumption:

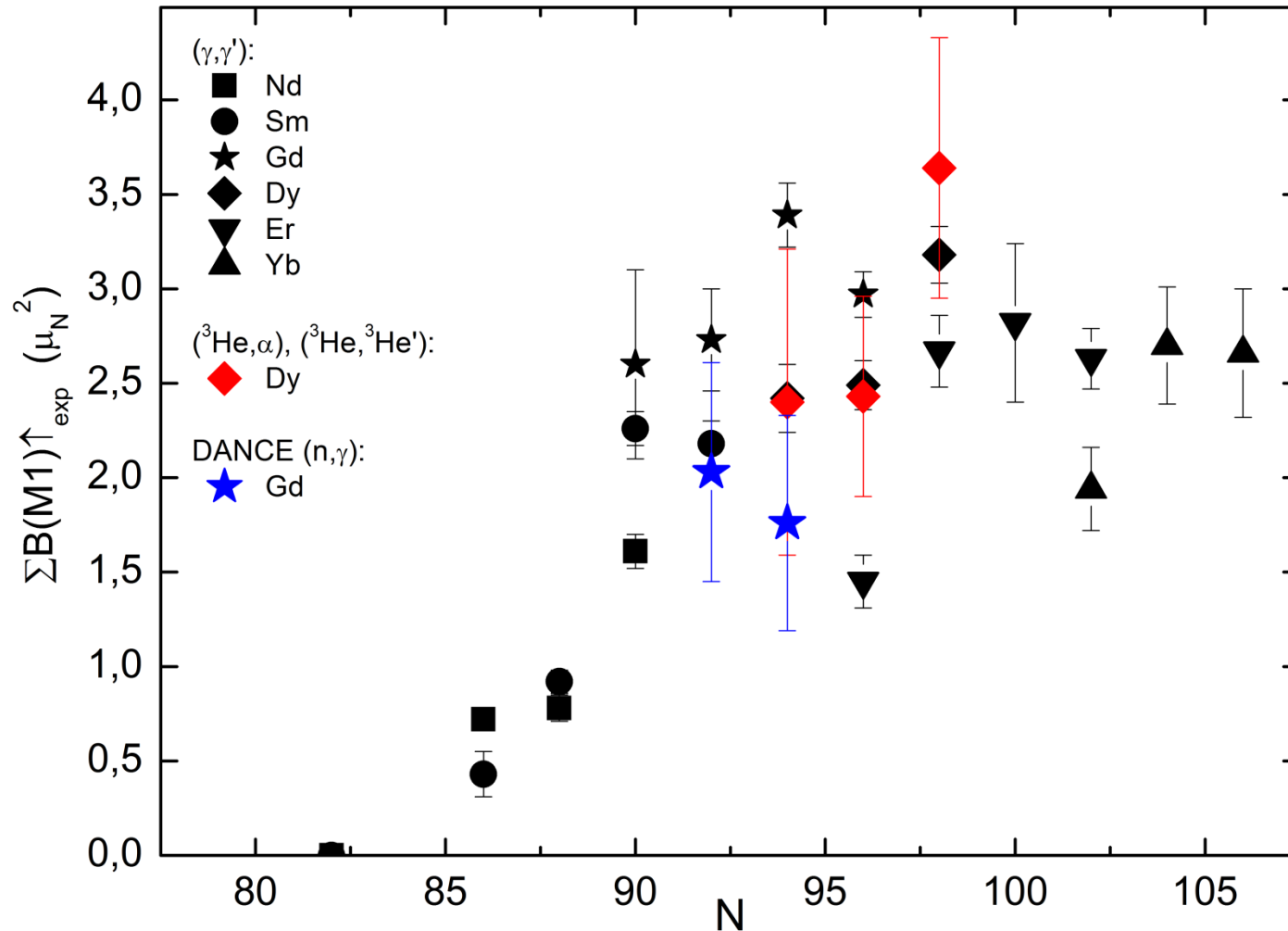
KMF + **SM** + **SF** + **SP** + SP + BSFG(1)

$E_{\text{SM}} = 3.0 \text{ MeV}, \Gamma_{\text{SM}} = 1.0 \text{ MeV},$

$\Sigma B(M1, \text{SM}) \approx 2.0 \mu_N^2$

**SM built on all levels**

# $\Sigma B(M1, 2.7-3.7) \uparrow$ in even nuclei



NRF data [black] *U. Kneissl et al., Prog. Part. Nucl. Phys.* **37** 349 (1996).

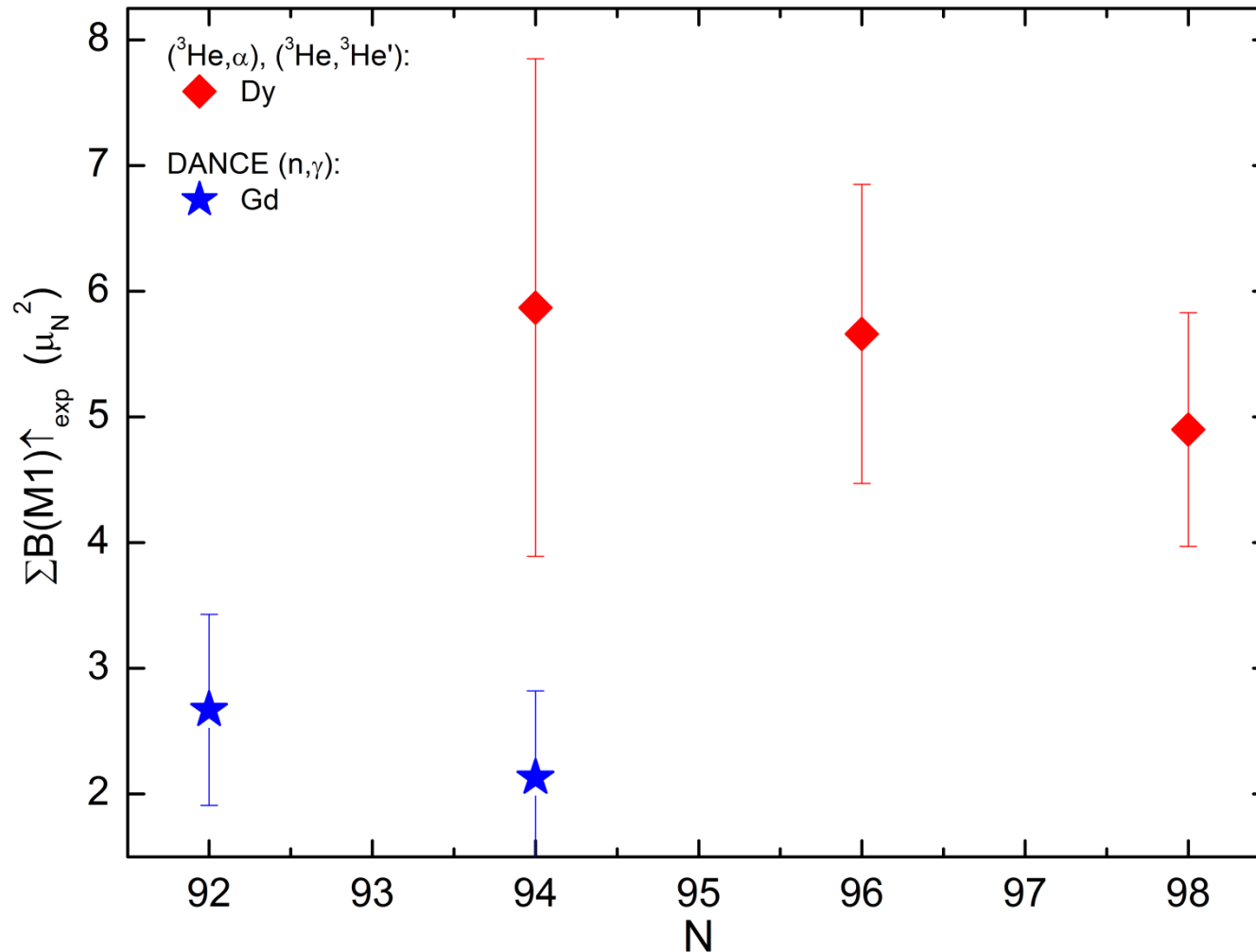
$^{160,162}\text{Dy}$  [red] *M. Guttormsen et al., PRC* **68**, 064306 (2003).

$^{164}\text{Dy}$  [red] *H.T. Nyhus et al., PRC* **81**, 024325 (2010).

$^{158}\text{Gd}$  [blue] *A. Chyzh et al., PRC* **84**, 014306 (2011).

$^{156}\text{Gd}$  [blue] *B. Baramsai et al., submitted to PRC.*

# $\Sigma B(M1, SM) \uparrow$ in even nuclei



$^{160,162}\text{Dy}$  [red] M. Guttormsen et al., PRC **68**, 064306 (2003).

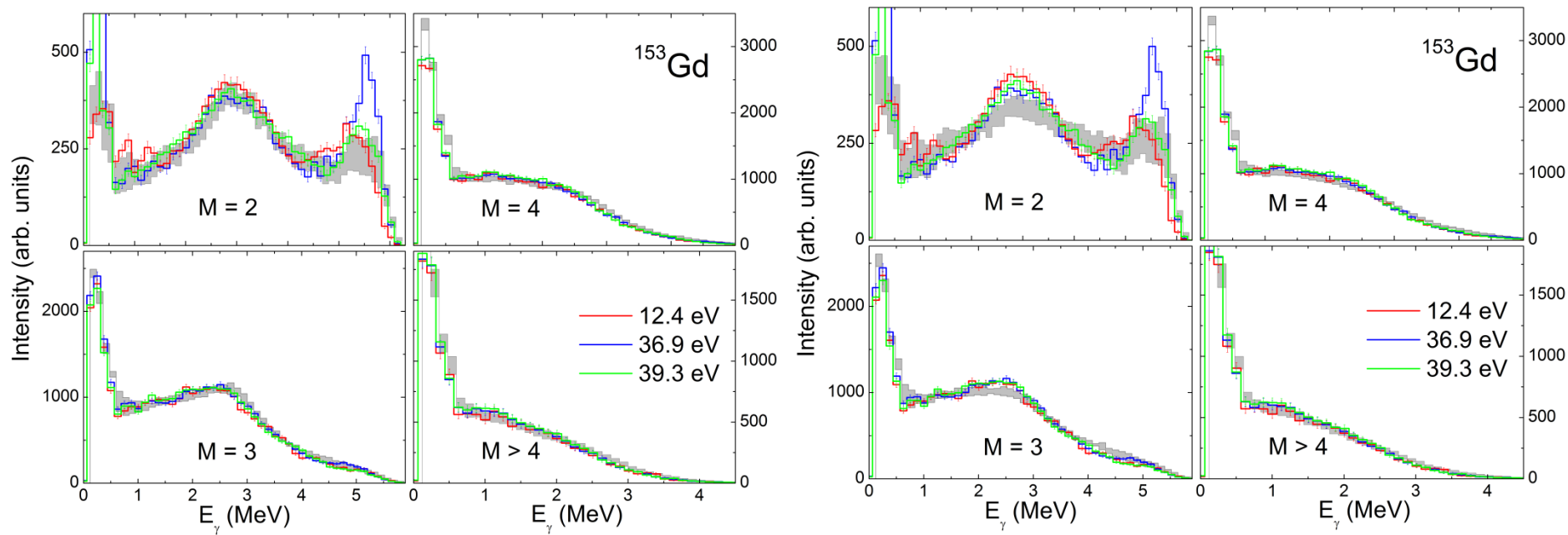
$^{164}\text{Dy}$  [red] H.T. Nyhus et al., PRC **81**, 024325 (2010).

$^{158}\text{Gd}$  [blue] A. Chyzh et al., PRC **84**, 014306 (2011).

$^{156}\text{Gd}$  [blue] B. Baramsai et al., submitted to PRC.

# $^{153}\text{Gd}$ results

Comparison of preliminary results obtained for  $^{153}\text{Gd}$



$^{153}\text{Gd}$  simulation assumption:

KMF + **SM** + **SF** + **SP** + SP + BSFG(1)

$E_{\text{SM}} = 2.9 \text{ MeV}$ ,  $\Gamma_{\text{SM}} = 1.0 \text{ MeV}$ ,

$\Sigma B(M1, \text{SM}) \approx 2.0 \mu_N^2$

**SM built on all levels**

$^{153}\text{Gd}$  simulation assumption:

KMF + **SM** + **SF** + **SP** + SP + BSFG(1)

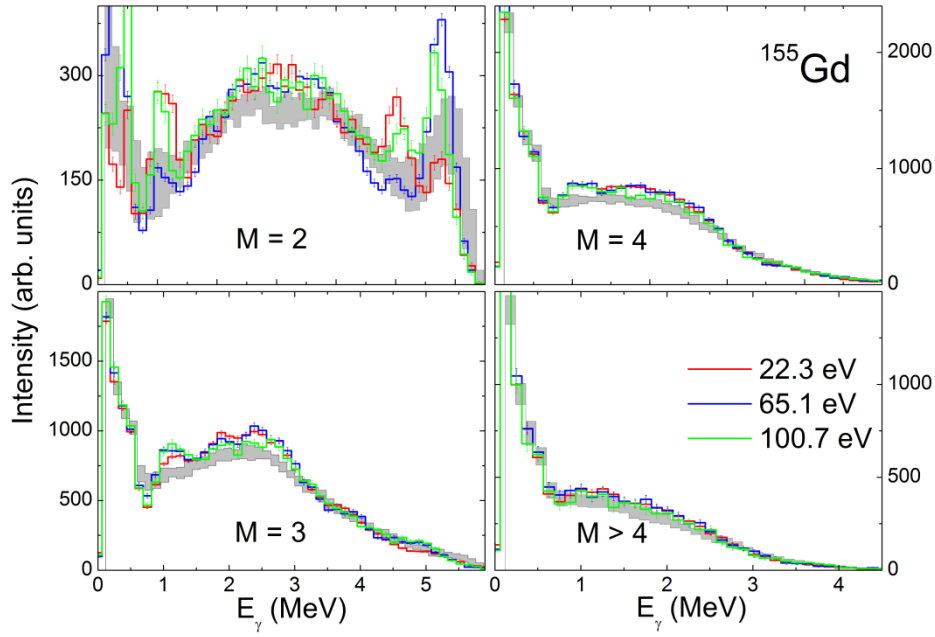
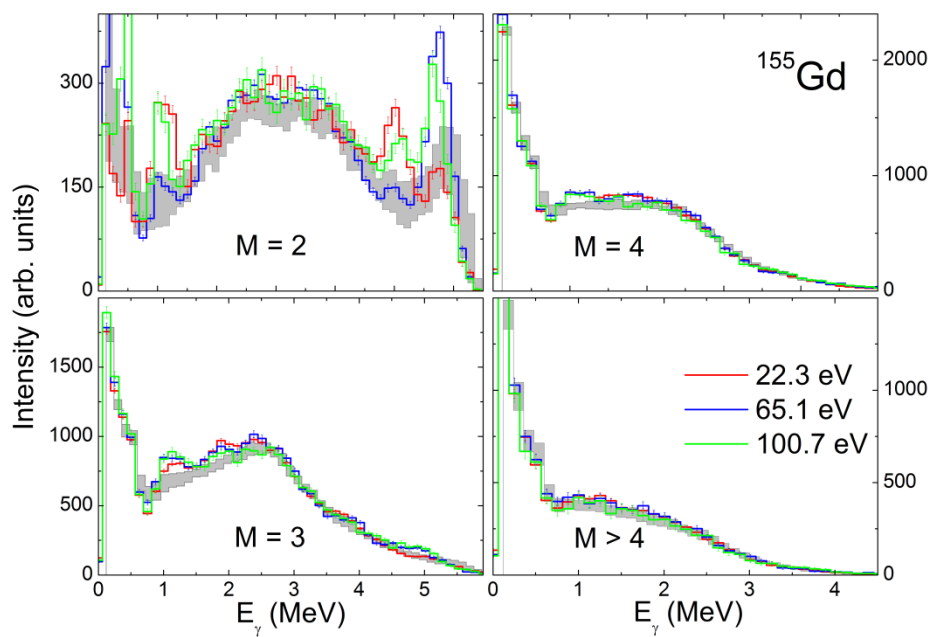
$E_{\text{SM}} = 2.9 \text{ MeV}$ ,  $\Gamma_{\text{SM}} = 1.0 \text{ MeV}$ ,

$\Sigma B(M1, \text{SM}) \approx 2.0 \mu_N^2$

**SM built only on the levels below 2.5 MeV**

# $^{155}\text{Gd}$ results

Comparison of preliminary results obtained for  $^{155}\text{Gd}$



$^{155}\text{Gd}$  simulation assumption:

KMF + **SM** + **SF** + **SP** + SP + BSFG(1)

$E_{\text{SM}} = 2.7 \text{ MeV}$ ,  $\Gamma_{\text{SM}} = 1.0 \text{ MeV}$ ,

$\Sigma B(M1, \text{SM}) \approx 2.0 \mu_N^2$

**SM built on all levels**

$^{155}\text{Gd}$  simulation assumption:

KMF + **SM** + **SF** + **SP** + SP + BSFG(1)

$E_{\text{SM}} = 2.7 \text{ MeV}$ ,  $\Gamma_{\text{SM}} = 1.0 \text{ MeV}$ ,

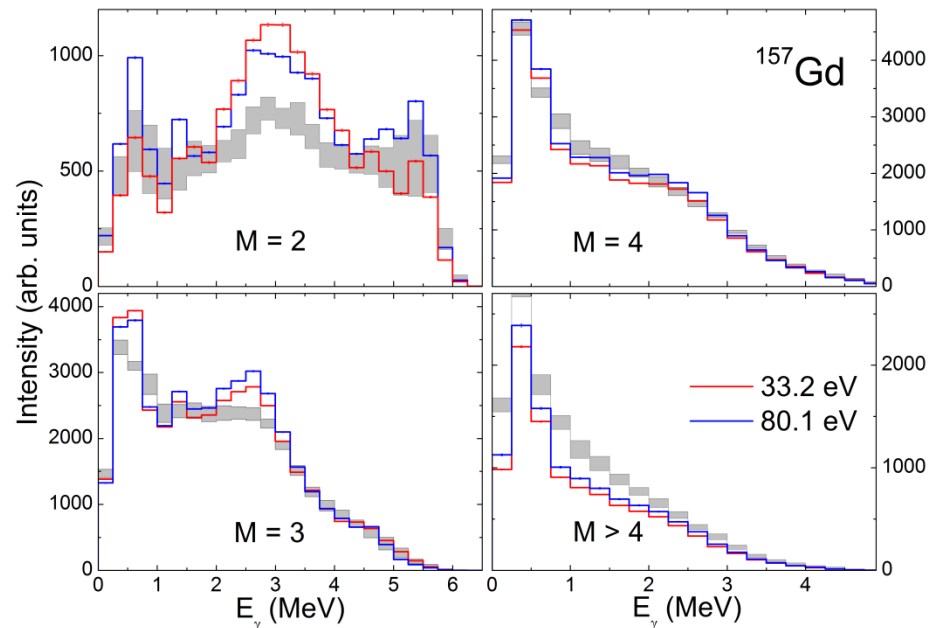
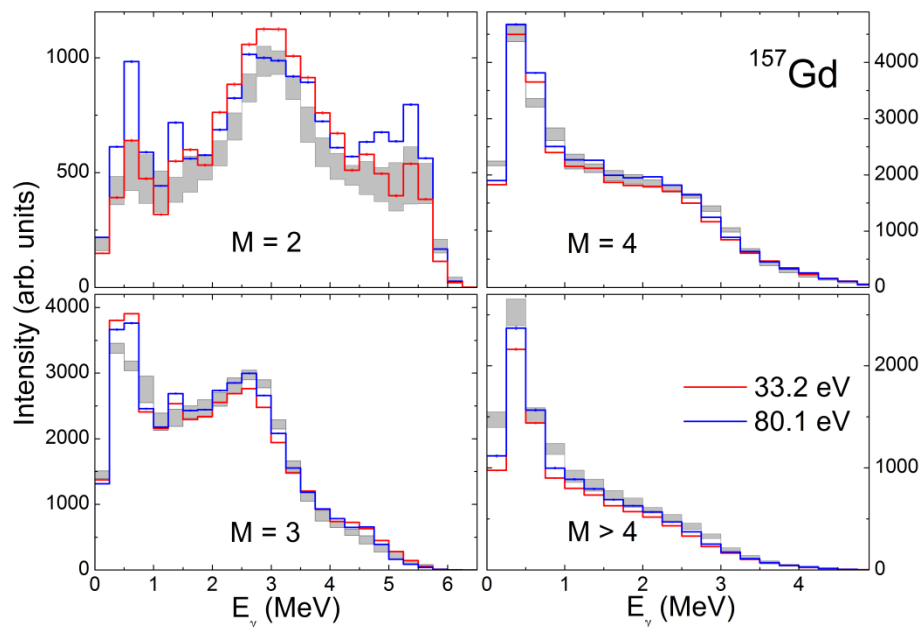
$\Sigma B(M1, \text{SM}) \approx 2.0 \mu_N^2$

**SM built only on the levels below 2.5 MeV**



# $^{157}\text{Gd}$ results

Comparison of preliminary results obtained for  $^{157}\text{Gd}$



$^{157}\text{Gd}$  simulation assumption:

KMF + **SM** + **SF** + **SP** + SP + BSFG(1)

$E_{\text{SM}} = 3.0 \text{ MeV}$ ,  $\Gamma_{\text{SM}} = 1.0 \text{ MeV}$ ,

$\Sigma B(M1, \text{SM}) \approx 6.0 \mu_N^2$

**SM built on all levels**

$^{157}\text{Gd}$  simulation assumption:

KMF + **SM** + **SF** + **SP** + SP + BSFG(1)

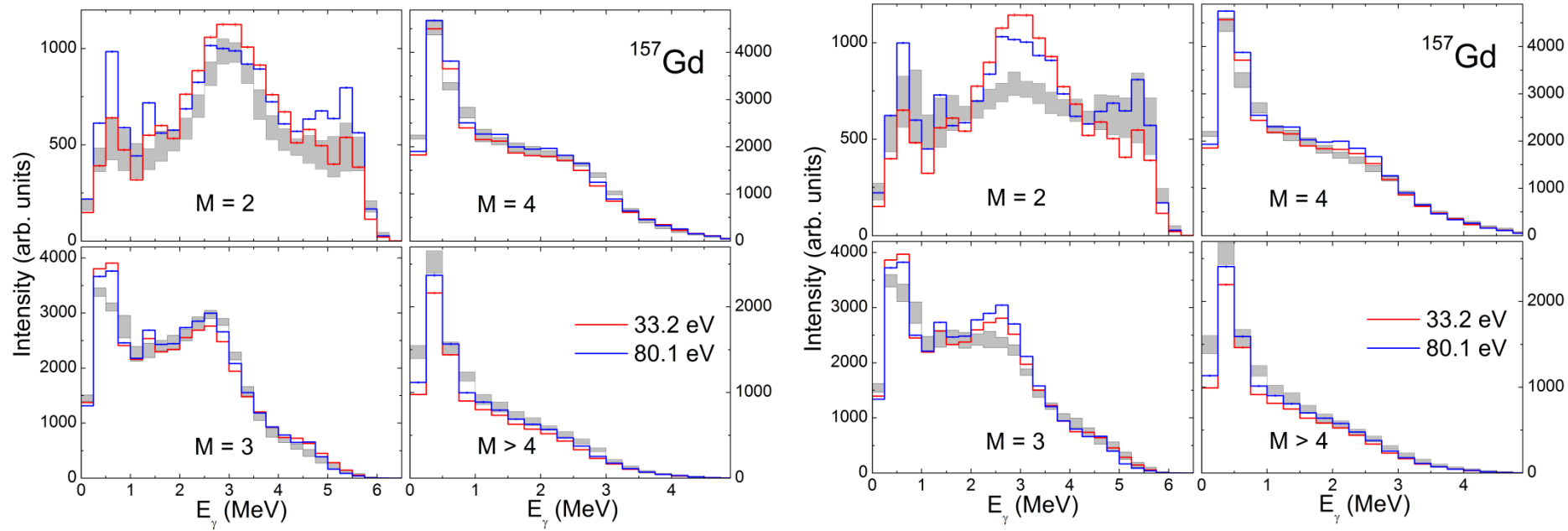
$E_{\text{SM}} = 3.0 \text{ MeV}$ ,  $\Gamma_{\text{SM}} = 1.0 \text{ MeV}$ ,

$\Sigma B(M1, \text{SM}) \approx 2.0 \mu_N^2$

**SM built on all levels**

# $^{157}\text{Gd}$ results

Comparison of preliminary results obtained for  $^{157}\text{Gd}$



$^{157}\text{Gd}$  simulation assumption:

KMF + **SM** + **SF** + **SP** + SP + BSFG(1)

$E_{\text{SM}} = 3.0 \text{ MeV}$ ,  $\Gamma_{\text{SM}} = 1.0 \text{ MeV}$ ,

$\Sigma B(M1, \text{SM}) \approx 6.0 \mu_N^2$

**SM built on all levels**

$^{157}\text{Gd}$  simulation assumption:

KMF + **SM** + **SF** + **SP** + SP + BSFG(1)

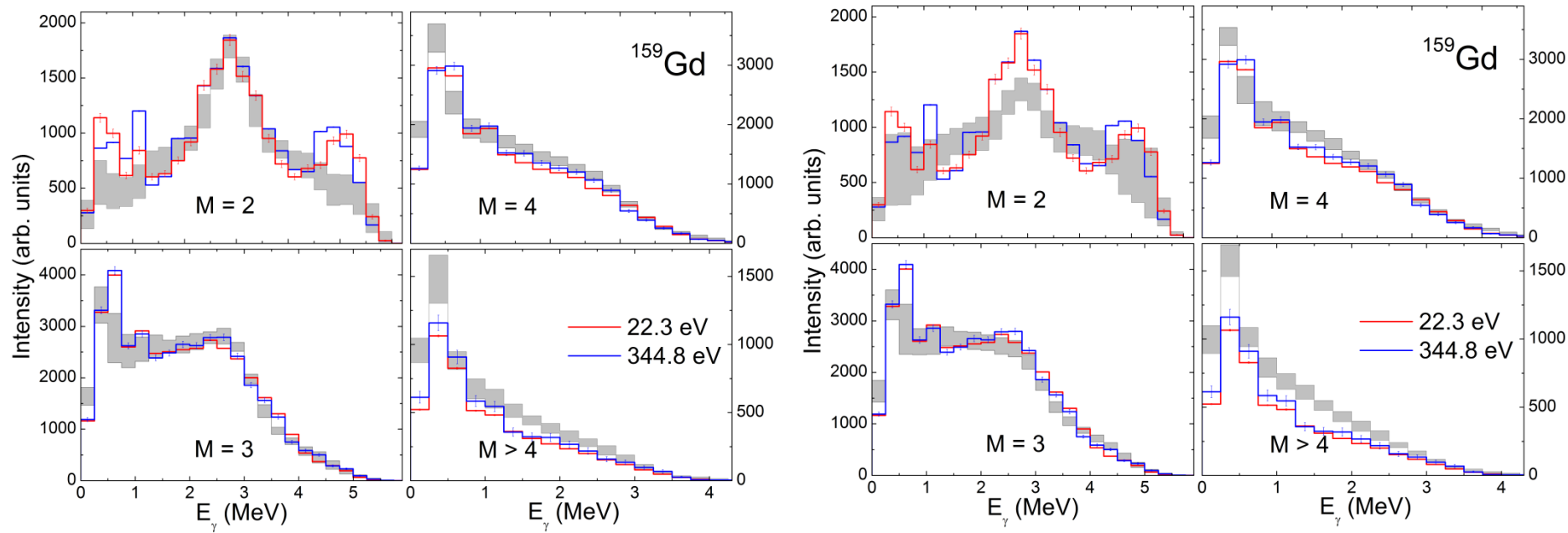
$E_{\text{SM}} = 3.0 \text{ MeV}$ ,  $\Gamma_{\text{SM}} = 1.0 \text{ MeV}$ ,

$\Sigma B(M1, \text{SM}) \approx 6.0 \mu_N^2$

**SM built only on the levels below 2.5 MeV**

# $^{159}\text{Gd}$ results

Comparison of preliminary results obtained for  $^{159}\text{Gd}$



$^{159}\text{Gd}$  simulation assumption:

KMF + **SM** + **SF** + **SP** + SP + BSFG(1)

$E_{\text{SM}} = 3.0 \text{ MeV}$ ,  $\Gamma_{\text{SM}} = 0.9 \text{ MeV}$ ,

$\Sigma B(M1, \text{SM}) \approx 5.0 \mu_N^2$

**SM built on all levels**

$^{159}\text{Gd}$  simulation assumption:

KMF + **SM** + **SF** + **SP** + SP + BSFG(1)

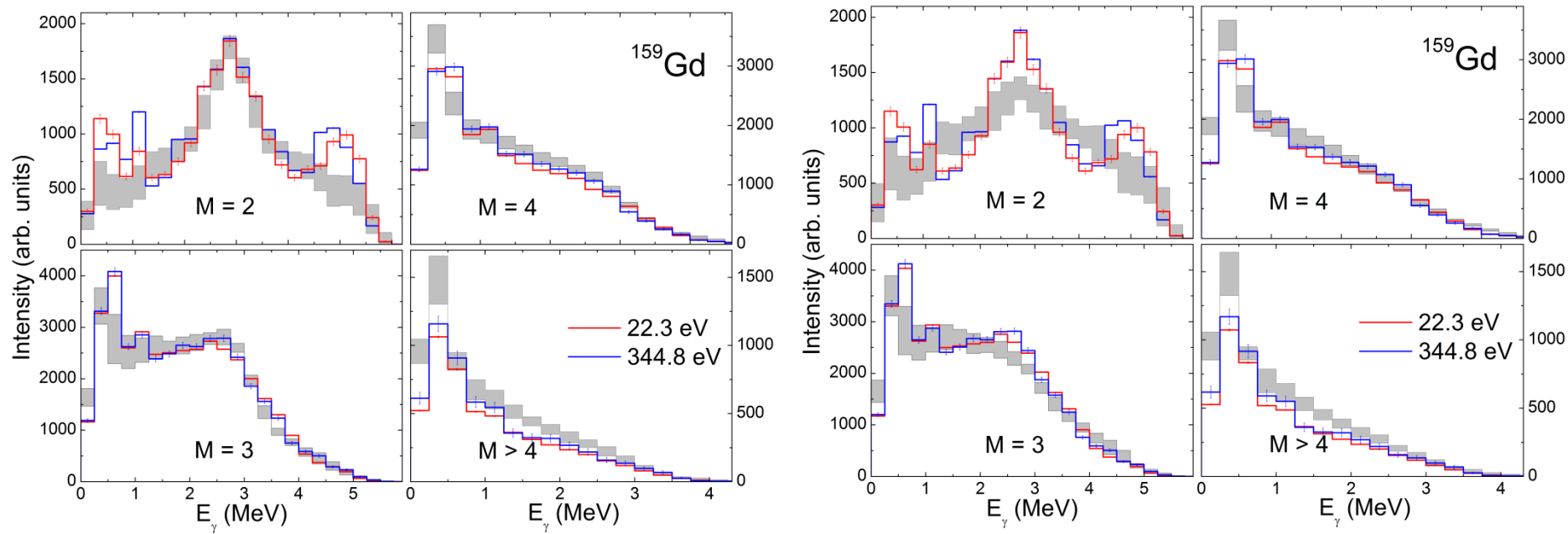
$E_{\text{SM}} = 3.0 \text{ MeV}$ ,  $\Gamma_{\text{SM}} = 1.0 \text{ MeV}$ ,

$\Sigma B(M1, \text{SM}) \approx 2.0 \mu_N^2$

**SM built on all levels**

# $^{159}\text{Gd}$ results

Comparison of preliminary results obtained for  $^{159}\text{Gd}$



$^{159}\text{Gd}$  simulation assumption:

KMF + **SM** + **SF** + **SP** + SP + BSFG(1)

$E_{\text{SM}} = 3.0 \text{ MeV}$ ,  $\Gamma_{\text{SM}} = 0.9 \text{ MeV}$ ,

$\Sigma B(M1, \text{SM}) \approx 5.0 \mu_N^2$

**SM built on all levels**

$^{159}\text{Gd}$  simulation assumption:

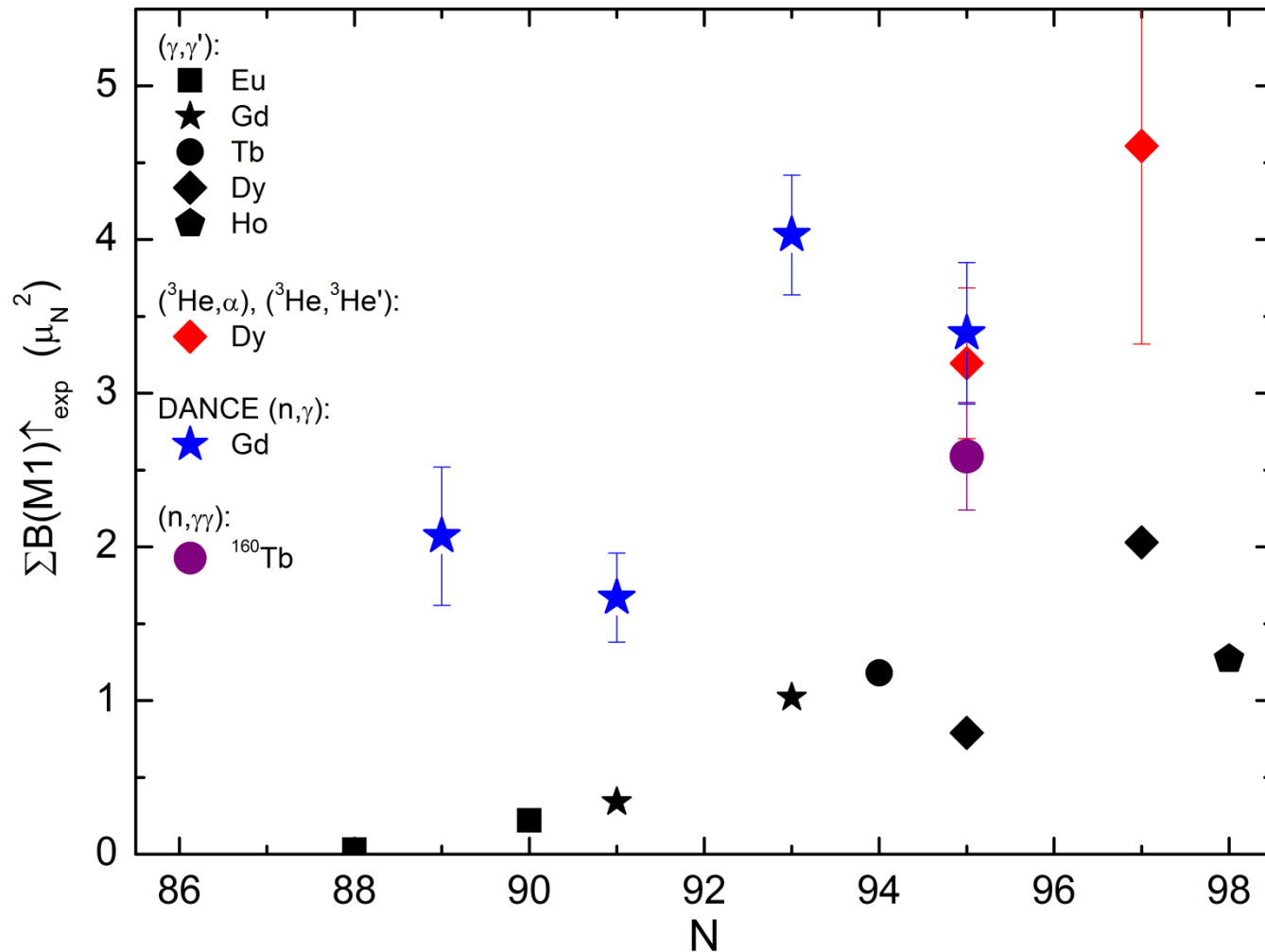
KMF + **SM** + **SF** + **SP** + SP + BSFG(1)

$E_{\text{SM}} = 3.0 \text{ MeV}$ ,  $\Gamma_{\text{SM}} = 0.9 \text{ MeV}$ ,

$\Sigma B(M1, \text{SM}) \approx 5.0 \mu_N^2$

**SM built only on the levels below 2.5 MeV**

# $\Sigma B(M1, 2.7-3.7) \uparrow$ in odd nuclei



NRF data [black] A. Nord et al., *PRC* **67**, 034307 (2003).

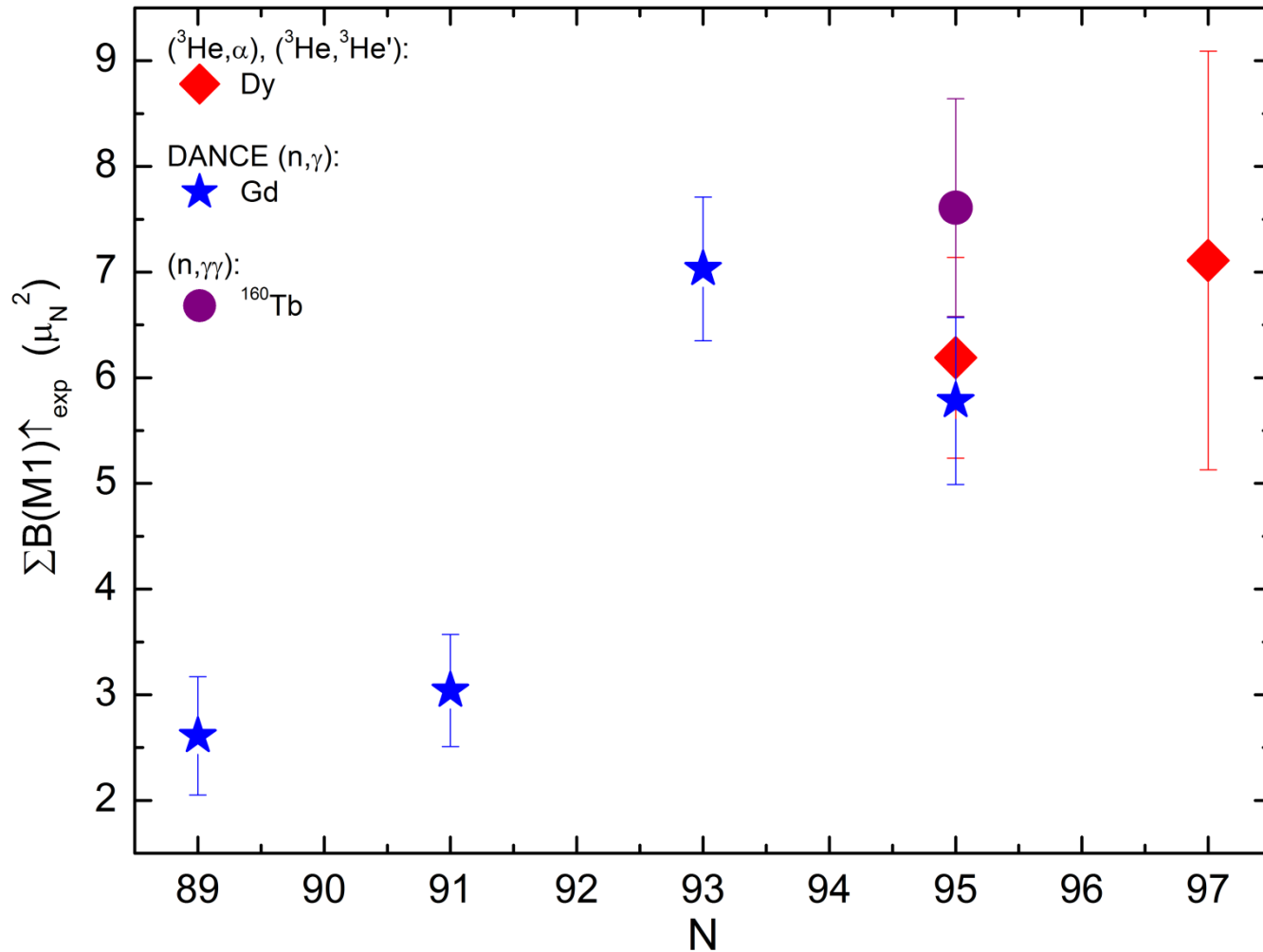
$^{161}\text{Dy}$  [red] M. Guttormsen et al., *PRC* **68**, 064306 (2003).

$^{163}\text{Dy}$  [red] H.T. Nyhus et al., *PRC* **81**, 024325 (2010).

$^{153,155,157,159}\text{Gd}$  [blue] Preliminary results

$^{160}\text{Tb}$  [purple] J. Kroll et al., *Int. Jour. of Mod. Physics E*, Vol. **20**, No. 2 (2011) 526– 531.

# $\Sigma B(M1)\uparrow$ in odd nuclei



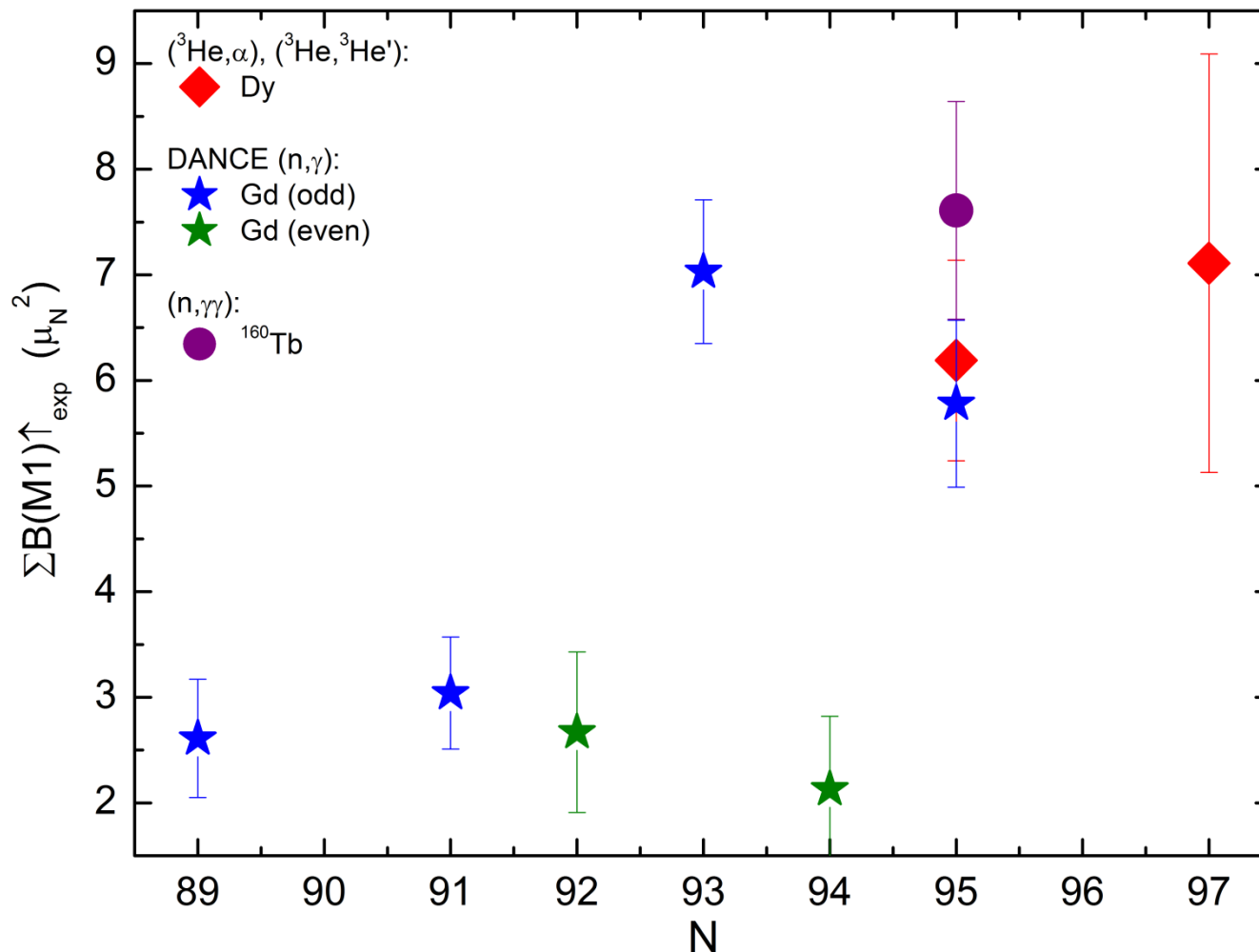
$^{161}\text{Dy}$  [red] M. Guttormsen et al., *PRC* **68**, 064306 (2003).

$^{163}\text{Dy}$  [red] H.T. Nyhus et al., *PRC* **81**, 024325 (2010).

$^{153,155,157,159}\text{Gd}$  [blue] Preliminary results

$^{160}\text{Tb}$  [purple] J. Kroll et al., *Int. Jour. of Mod. Physics E*, Vol. **20**, No. 2 (2011) 526– 531.

# $\Sigma B(M1, SM) \uparrow$ in odd nuclei



$^{161}\text{Dy}$  [red] M. Guttormsen et al., *PRC* **68**, 064306 (2003).

$^{163}\text{Dy}$  [red] H.T. Nyhus et al., *PRC* **81**, 024325 (2010).

$^{153,155,157,159}\text{Gd}$  [blue] Preliminary results

$^{158}\text{Gd}$  [green] A. Chyzh et al., *PRC* **84**, 014306 (2011).

$^{156}\text{Gd}$  [green] B. Baramsai et al., submitted to *PRC*.

$^{160}\text{Tb}$  [purple] J. Kroll et al., *Int. Jour. of Mod. Physics E*, Vol. **20**, No. 2 (2011) 526–531.

# Conclusions

- $M1$  SM plays an important role in gamma deexcitation of studied Gd isotopes.
- Values of  $\Sigma B(M1, 2.7-3.7)\uparrow$  obtained for  $^{156,158}\text{Gd}$  are slightly below the results of  $(\gamma, \gamma')$  experiments. Significant part of the observed strength corresponds to the non-resonant structure present in  $M1$  PSF.
- We have received new results for  $\Sigma B(M1)$  present in odd rare-earth isotopes  $^{153,155,157,159}\text{Gd}$ .
- SM resonances are built not only on the GS but also on excited levels in all studied Gd isotopes.
- Difference between  $\Sigma B(M1)$  in  $^{156,158}\text{Gd}$  and  $^{157,159}\text{Gd}$ .



# DANCE collaboration

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