

A threshold resonance state explains unusual branching ratio and angular distributions

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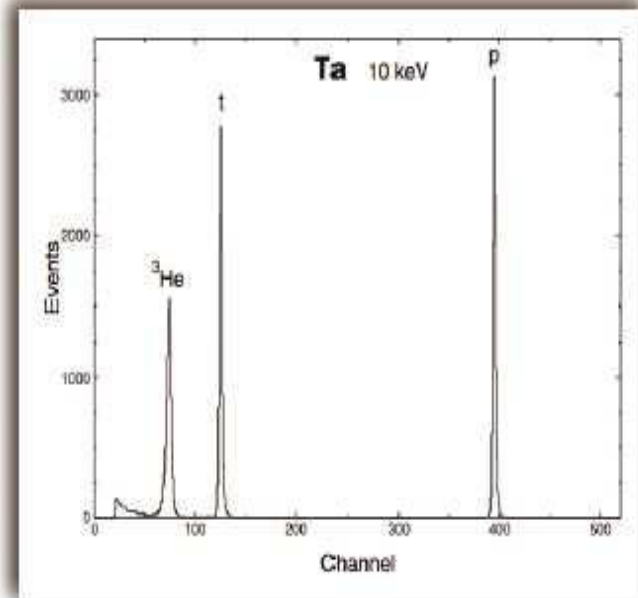
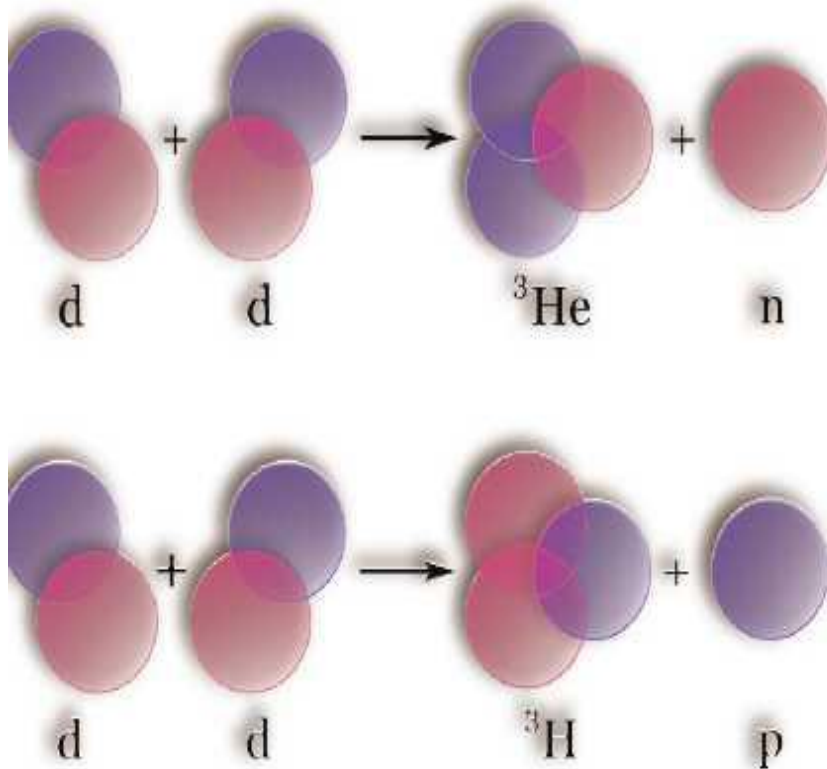
9th Nuclear Physics Workshop "Marie & Pierre Curie" Kazimierz Dolny 2012

Outline

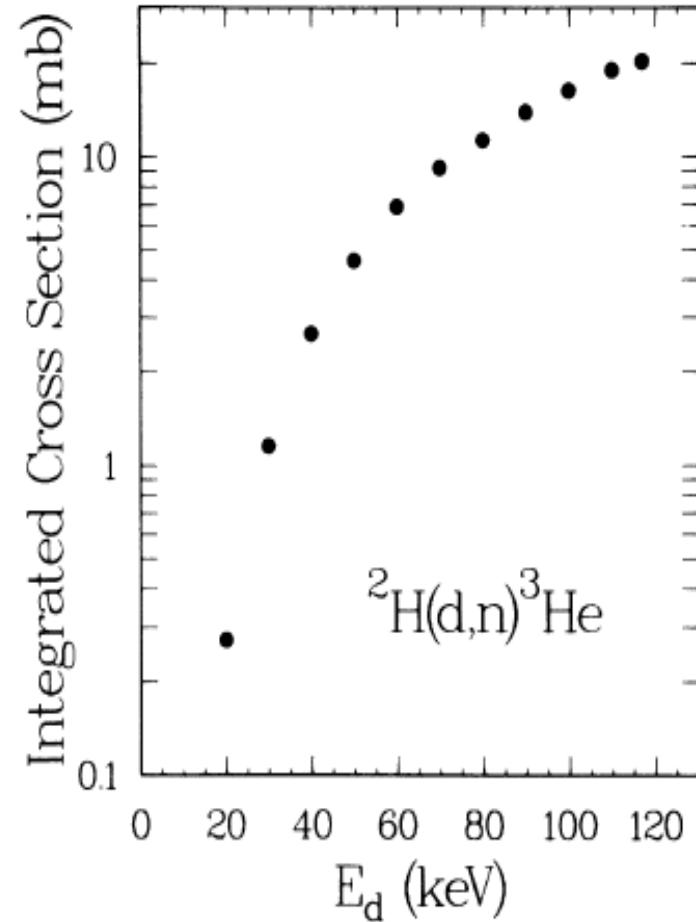
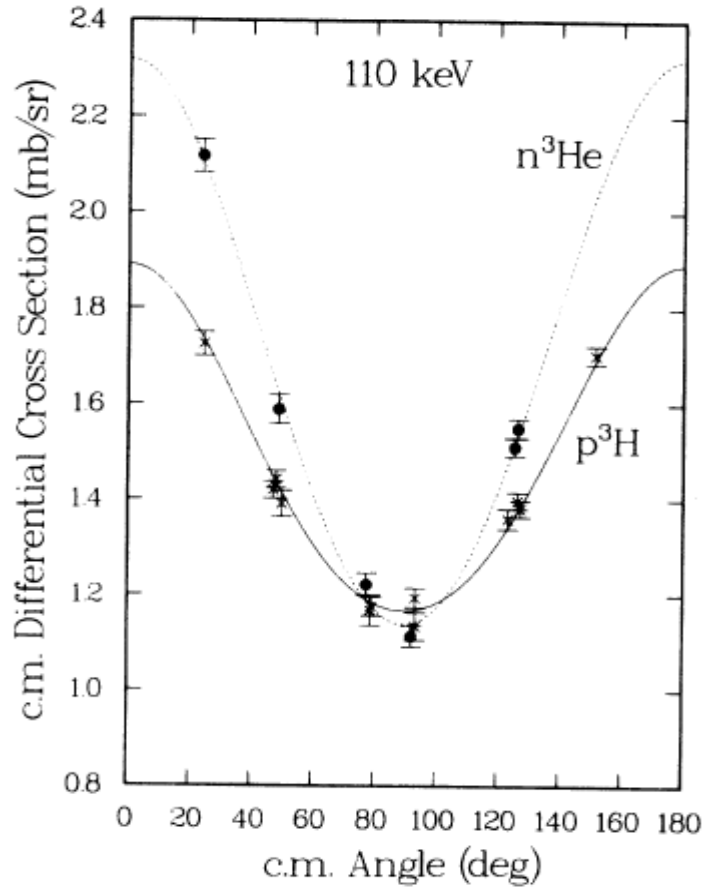
- General view of D+d reactions- motivation for the study
- Branching ratio and angular distributions for The D+d reactions
- Direct reaction and compound nucleus reaction contributions
- Model independent approach
- Experimental results
- 0^+ threshold resonance contribution in He^4 for the D+d reactions

Motivation

The ${}^2\text{H}(d,n){}^3\text{He}$ and ${}^2\text{H}(d,p){}^3\text{H}$ reactions



Angular Distribution and Cross section for dd reactions in gas target experiment

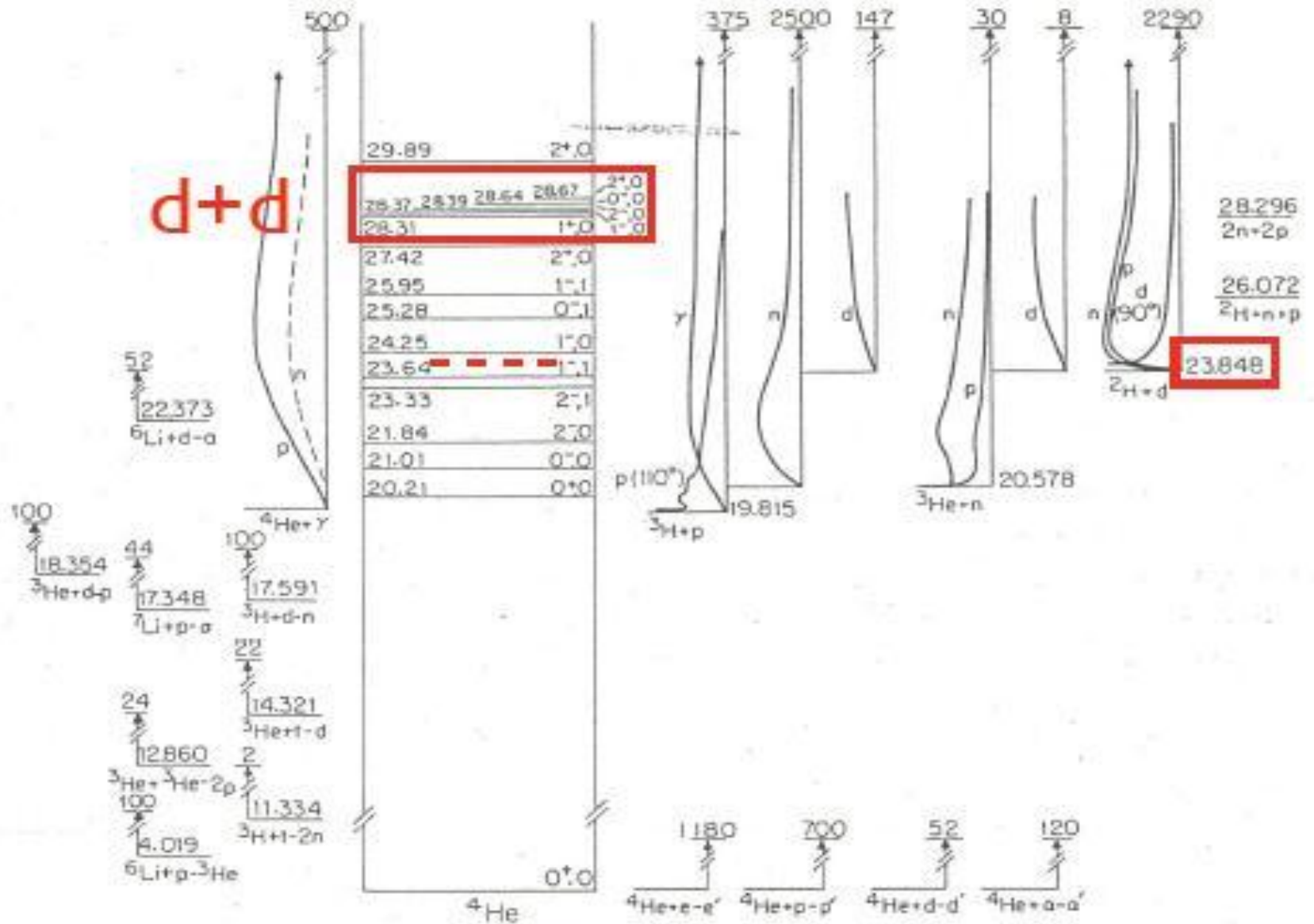


$$\sigma(\theta) = a + b\cos^2\theta + c\cos^4\theta.$$

Level scheme of He4

D.R. Tilley et al. / Energy levels of light nuclei A = 4

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Very small cross sections

$$E \ll E_C \rightarrow 10^{-18} \text{ barn} \leq \sigma(E) \leq 10^{-9} \text{ barn}$$

'Nuclear' contribution:
the S-factor

$$\sigma(E) = S(E) e^{-2\pi\eta(E)} \frac{1}{E}$$

Coulomb contribution (strong
energy dependence):
The Gamow factor

With the Gamow factor: $2\pi\eta(E) = 31.29 Z_1 Z_2 (\mu/E)^{1/2}$

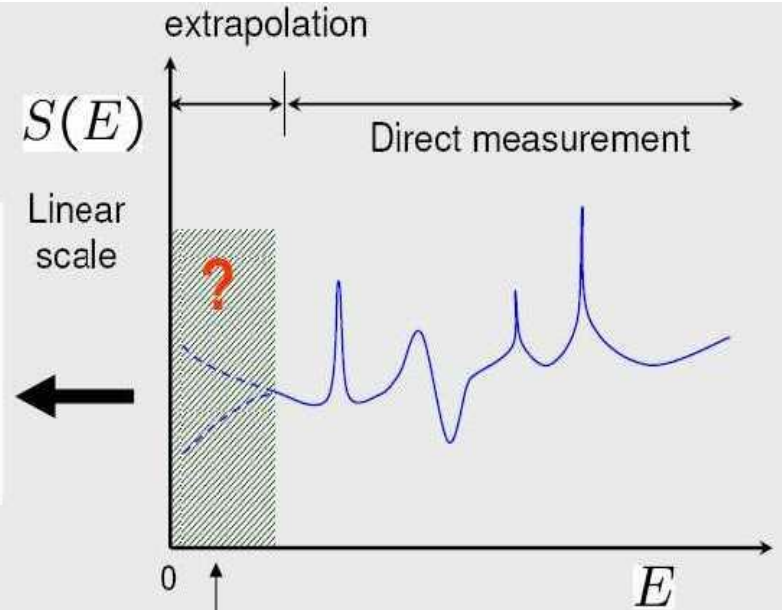
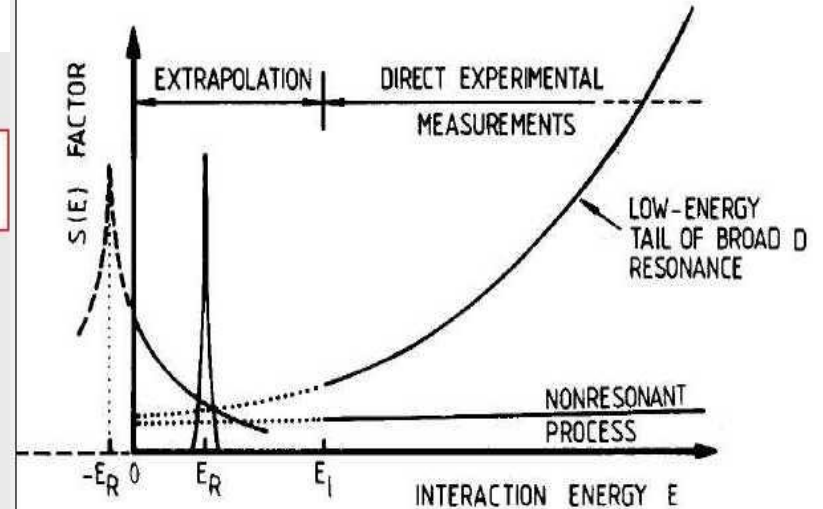
Z_1, Z_2 the charge of the nuclei,
 μ the reduced mass, E in keV

Procedure

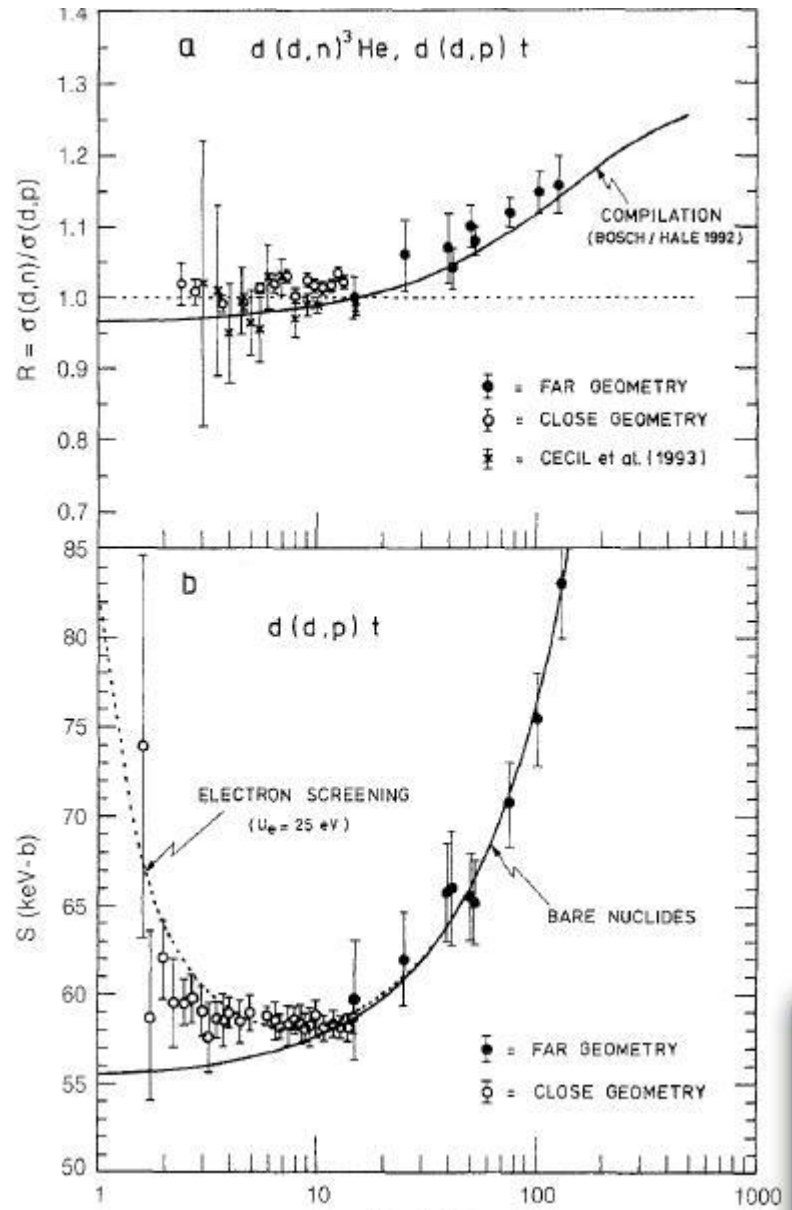
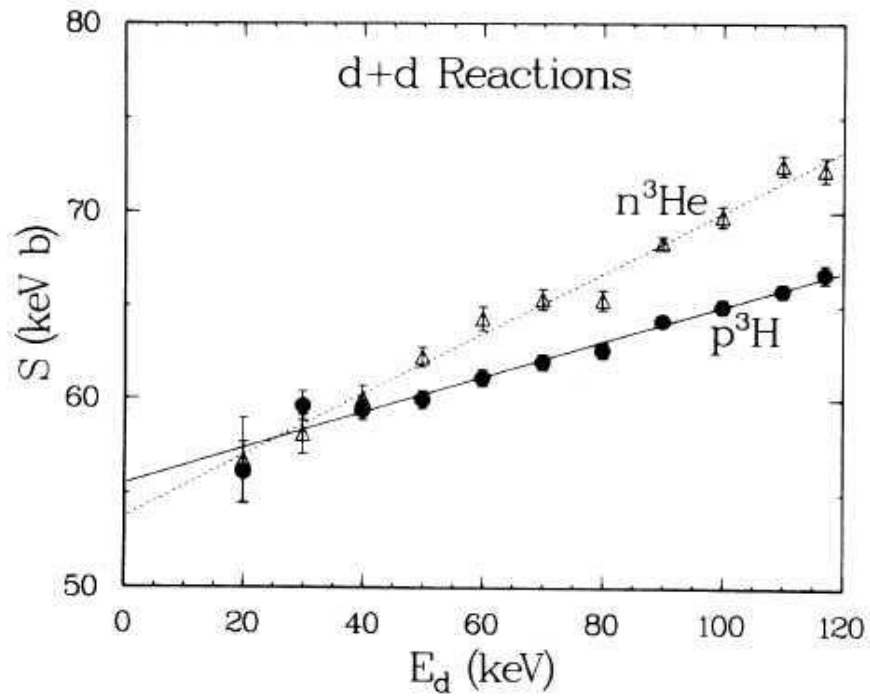
1. measurement of cross sections higher energies
2. extrapolation to astrophysical energies

Need

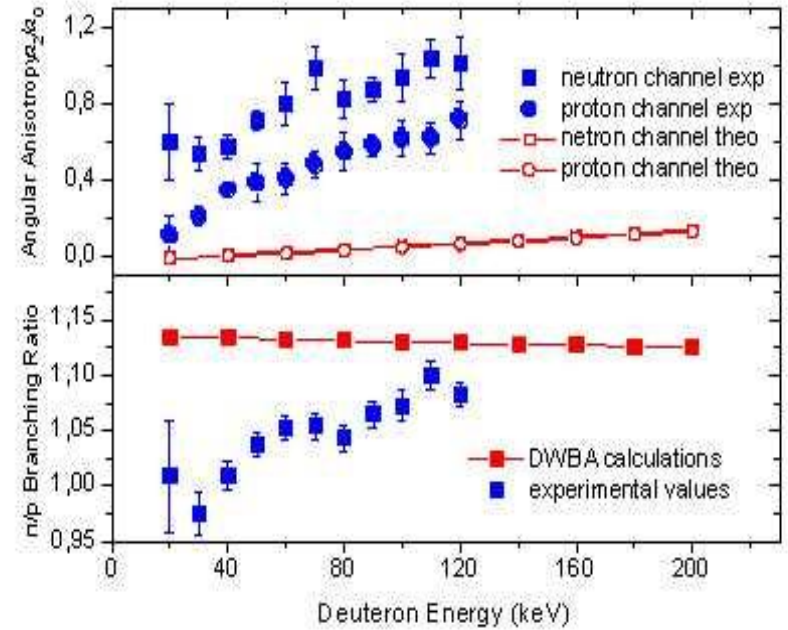
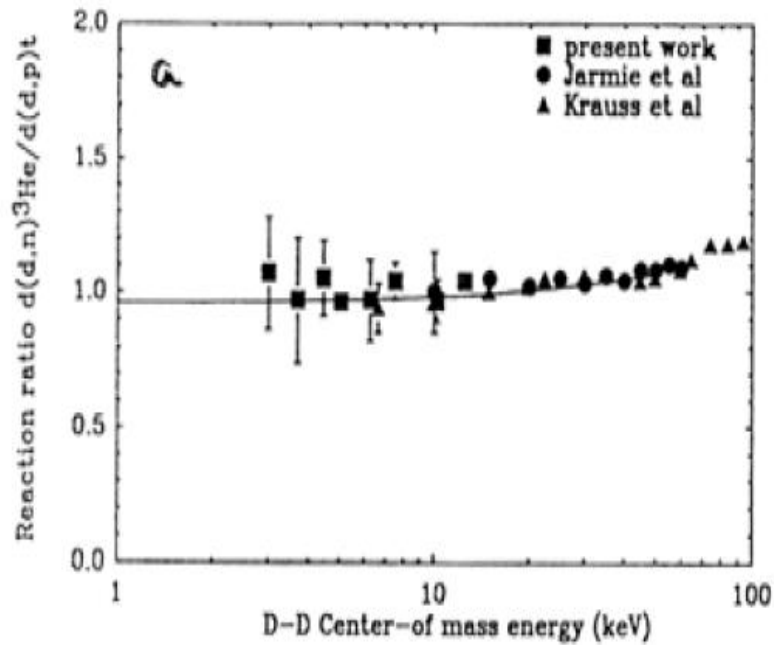
- low energy measurements (but even though....)
- Use of theoretical methods



Astrophysical S-factor for d+d



DWBA calculation versus R - Matrix



Cecil, F.E. and G.M. Hale. Measurement of D-D and D-Li6 Nuclear Reactions at Very Low Energies. in Second Annual Conference on Cold Fusion, "The Science of Cold Fusion". 1991.

A.İ.Kılıç, K. Czernski et al Isospin symmetry breaking and branching ratio in the deuteron reactions at Very low energies . International Journal of Modern Physics E Vol. 20, No. 2 (2011)

Model independent approach

Definition of Transition matrix elements, penetration and penetrabilities for d+d reactions

$$T_{\beta\alpha} = \langle 2S_{\alpha}+1 \ell_{\alpha J} | J^{\pi} | 2S_{\beta}+1 \ell_{\beta J} \rangle$$

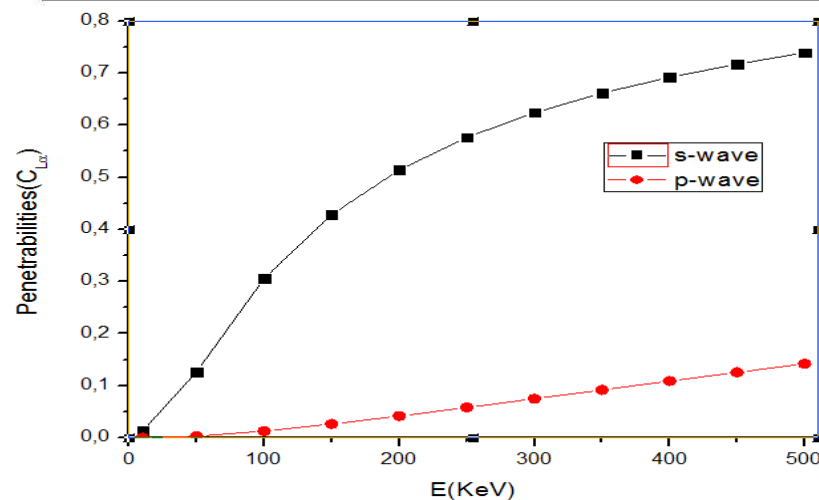
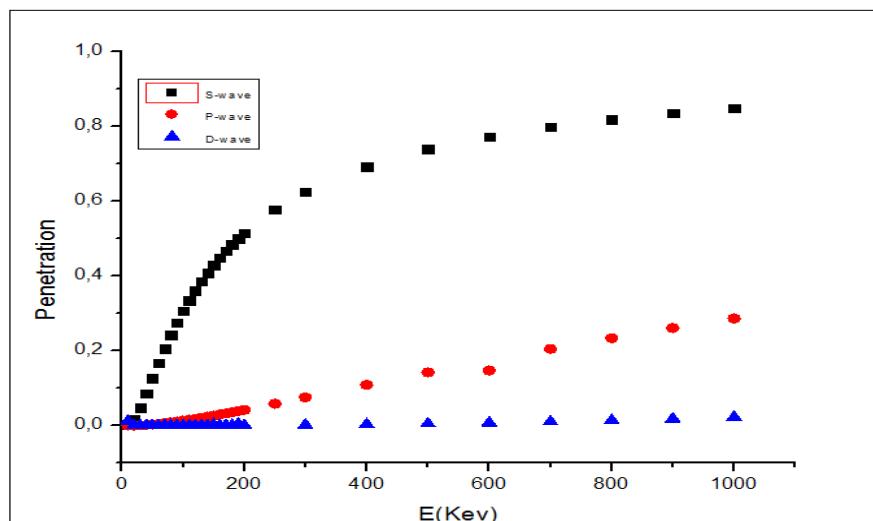
α : entrance channel; β : exit channel.

$$T_{\beta\alpha}(E) = C_{\ell_{\alpha}}(E) \hat{T}_{\beta\alpha}$$

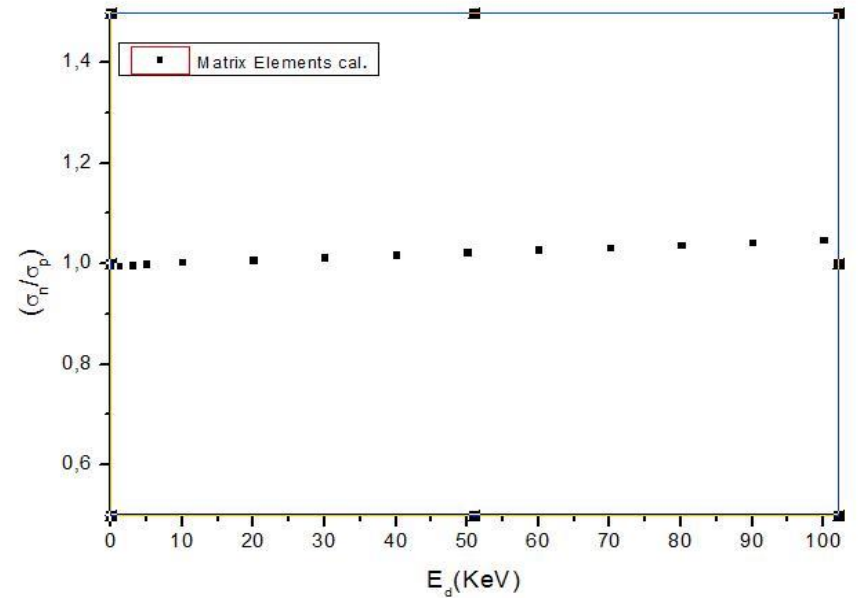
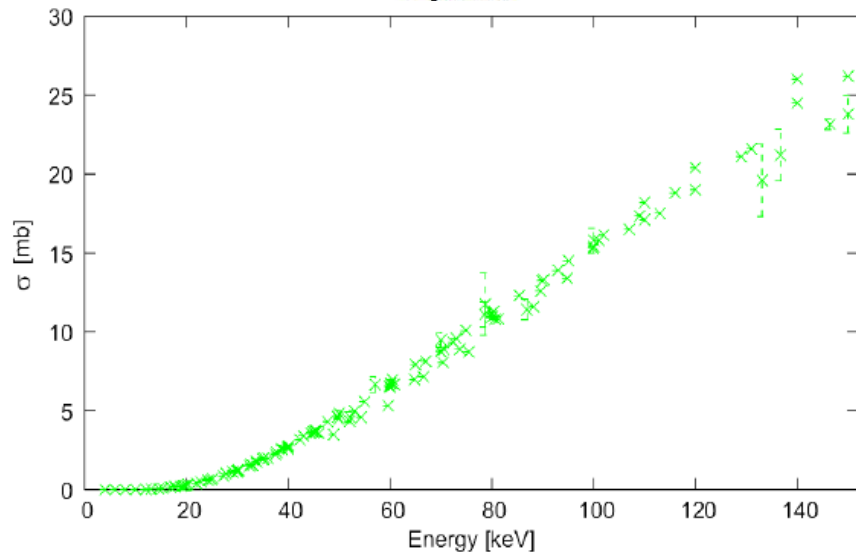
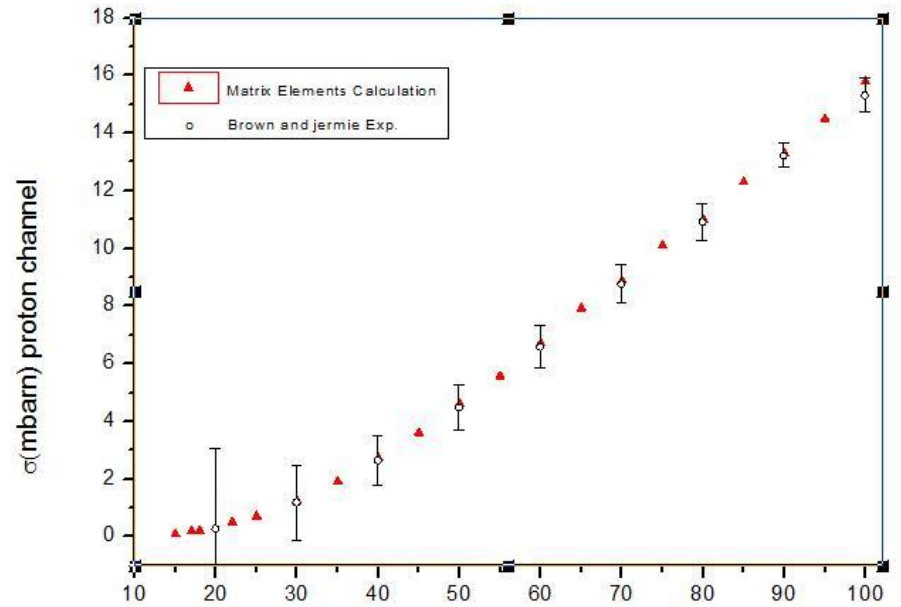
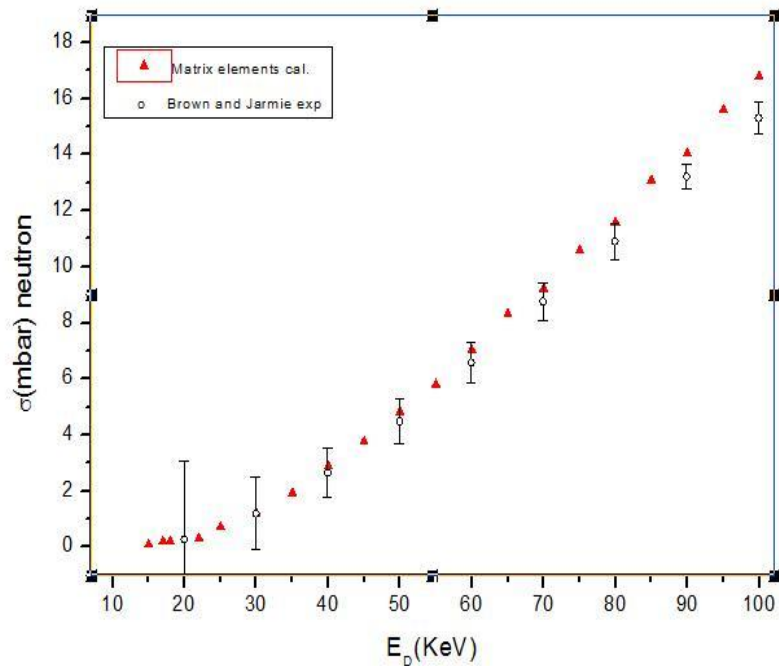
$$C_{\ell_{\alpha}}(E) = \sqrt{P_{\ell_{\alpha}}(E)} \exp[i(\delta_{\ell_{\alpha}} + \varphi_{\ell_{\alpha}})]$$

$$P_{\ell_{\alpha}}(E) = \frac{1}{F_{\ell_{\alpha}}(E)^2 + G_{\ell_{\alpha}}(E)^2}$$

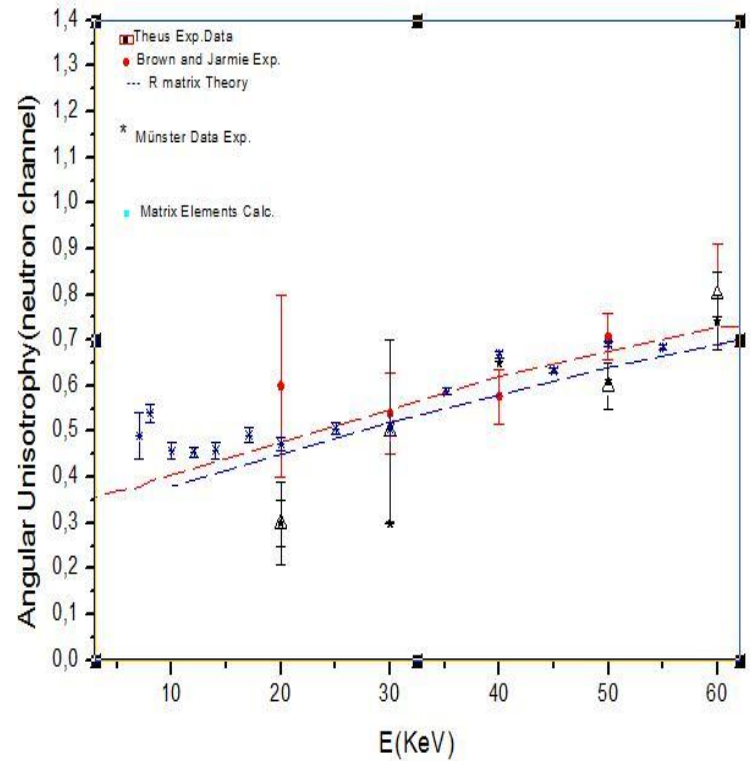
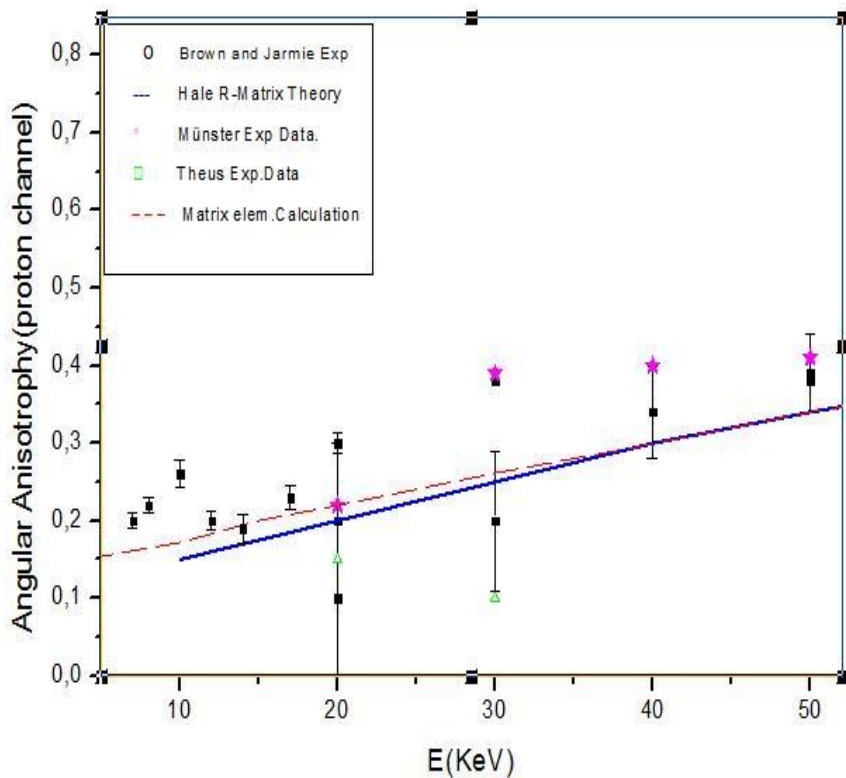
	$S_{\alpha} = 0$ (Singlet)	$S_{\alpha} = 1$ (Triplet)	$S_{\alpha} = 2$ (Quintet)
$\ell_{\alpha} = 0$	$\alpha_0 = \langle {}^1S_0 0^+ {}^1S_0 \rangle$		$\gamma_1 = \langle {}^5S_2 2^+ {}^1D_2 \rangle$ $\delta_1 = \langle {}^5S_2 2^+ {}^3D_2 \rangle$
$\ell_{\alpha} = 1$		$\alpha_{10} = \langle {}^3P_0 0^- {}^3P_0 \rangle$ $\beta_{11} = \langle {}^3P_1 1^- {}^1P_1 \rangle$ $\alpha_{11} = \langle {}^3P_1 1^- {}^3P_1 \rangle$ $\alpha_{12} = \langle {}^3P_2 2^- {}^3P_2 \rangle$ $\alpha_3 = \langle {}^3P_2 2^- {}^3F_2 \rangle$	
$\ell_{\alpha} = 2$	$\alpha_2 = \langle {}^1D_2 2^+ {}^1D_2 \rangle$ $\beta_2 = \langle {}^1D_2 2^+ {}^3D_2 \rangle$		$\gamma_2 = \langle {}^5D_0 0^+ {}^1S_0 \rangle$ $\gamma_3 = \langle {}^5D_2 2^+ {}^1D_2 \rangle$ $\delta_2 = \langle {}^5D_1 1^+ {}^3S_1 \rangle$ $\delta_3 = \langle {}^5D_1 1^+ {}^3D_1 \rangle$ $\delta_4 = \langle {}^5D_3 3^+ {}^3D_3 \rangle$ $\delta_5 = \langle {}^5D_2 2^+ {}^3D_2 \rangle$



Cross sections for d+d reactions



Usual angular distributions for d+d reactions



Electron screening

$$f_{\text{lab}}(E) = \frac{S_{\text{screen}}(E)}{S_{\text{bare}}(E)} \sim \exp(\pi\eta U_e/E)$$

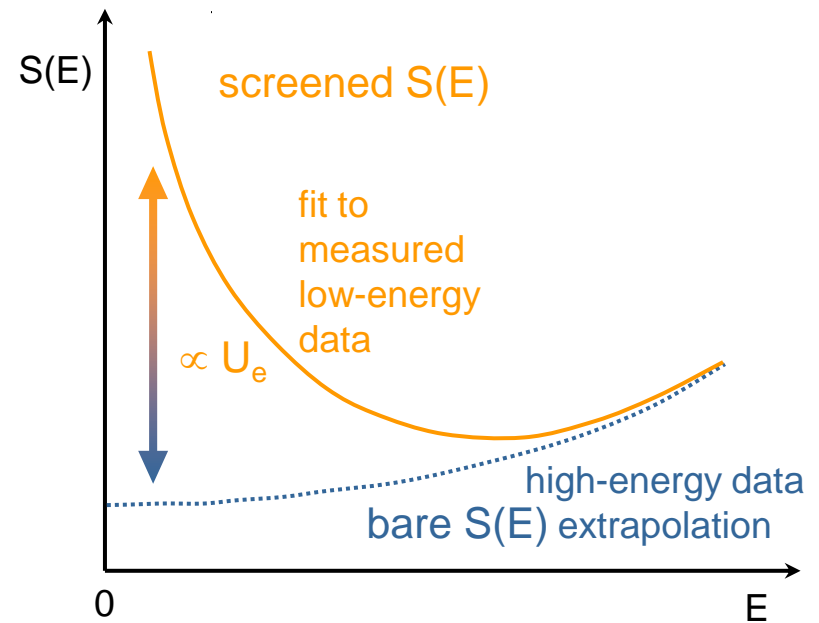
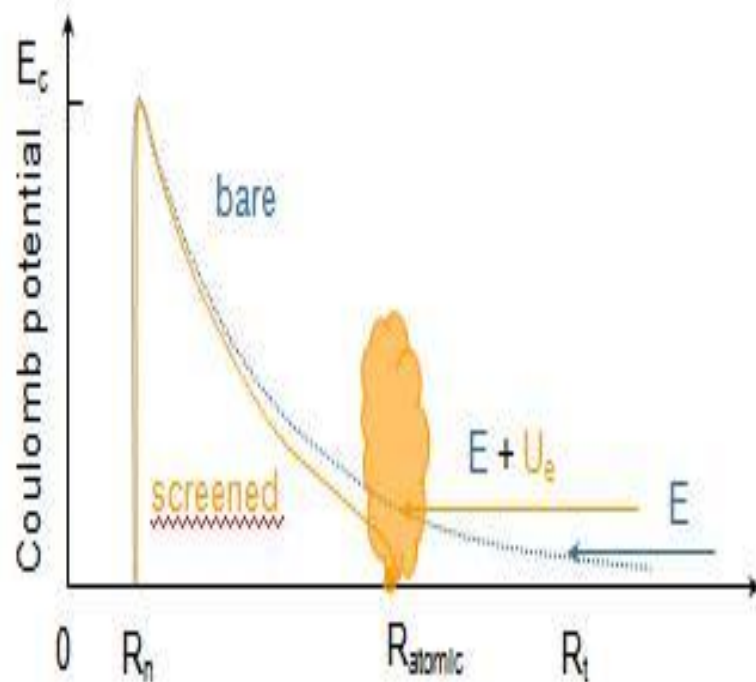
$$V(r) = \frac{Z_1 Z_2 e^2}{r} \phi(r)$$

$$\phi(r) = e^{-\frac{r}{a}}$$

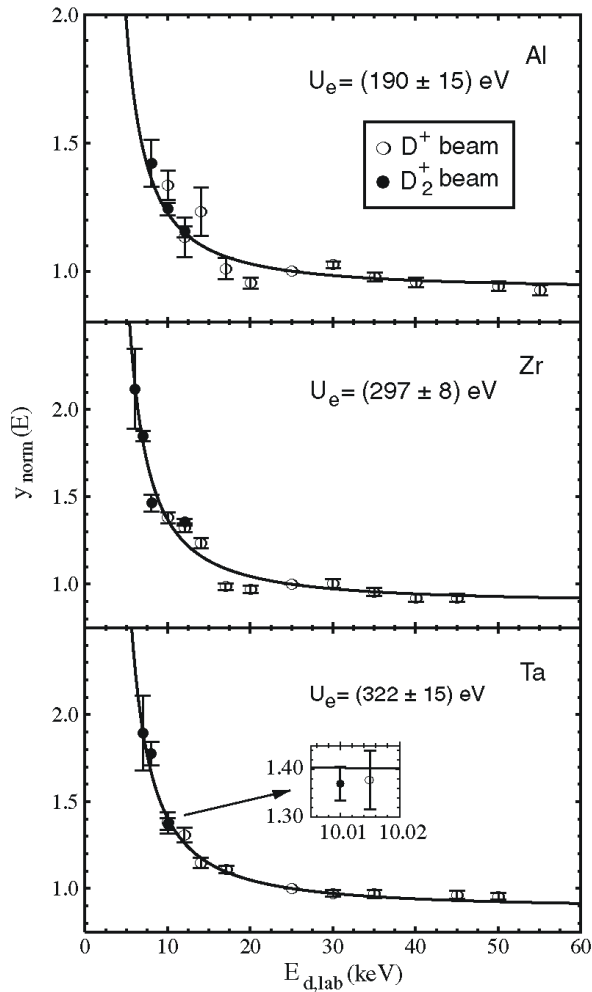
$$V(r) = \frac{Z_1 Z_2 e^2}{r} \left(1 - \frac{r}{a}\right) =$$

$$= \frac{Z_1 Z_2 e^2}{r} - \underbrace{\frac{Z_1 Z_2 e^2}{a}}_{U_e}$$

$$E_{\text{eff}} = E + U_e$$



Experimental screening



metal target

NIC 1998, p. 152

Europhys. Lett. 54 (2001) 449

Similar results:

J. Kasagi et al.

LUNA Collaboration

$U_e = 25 \pm 5 \text{ eV}$

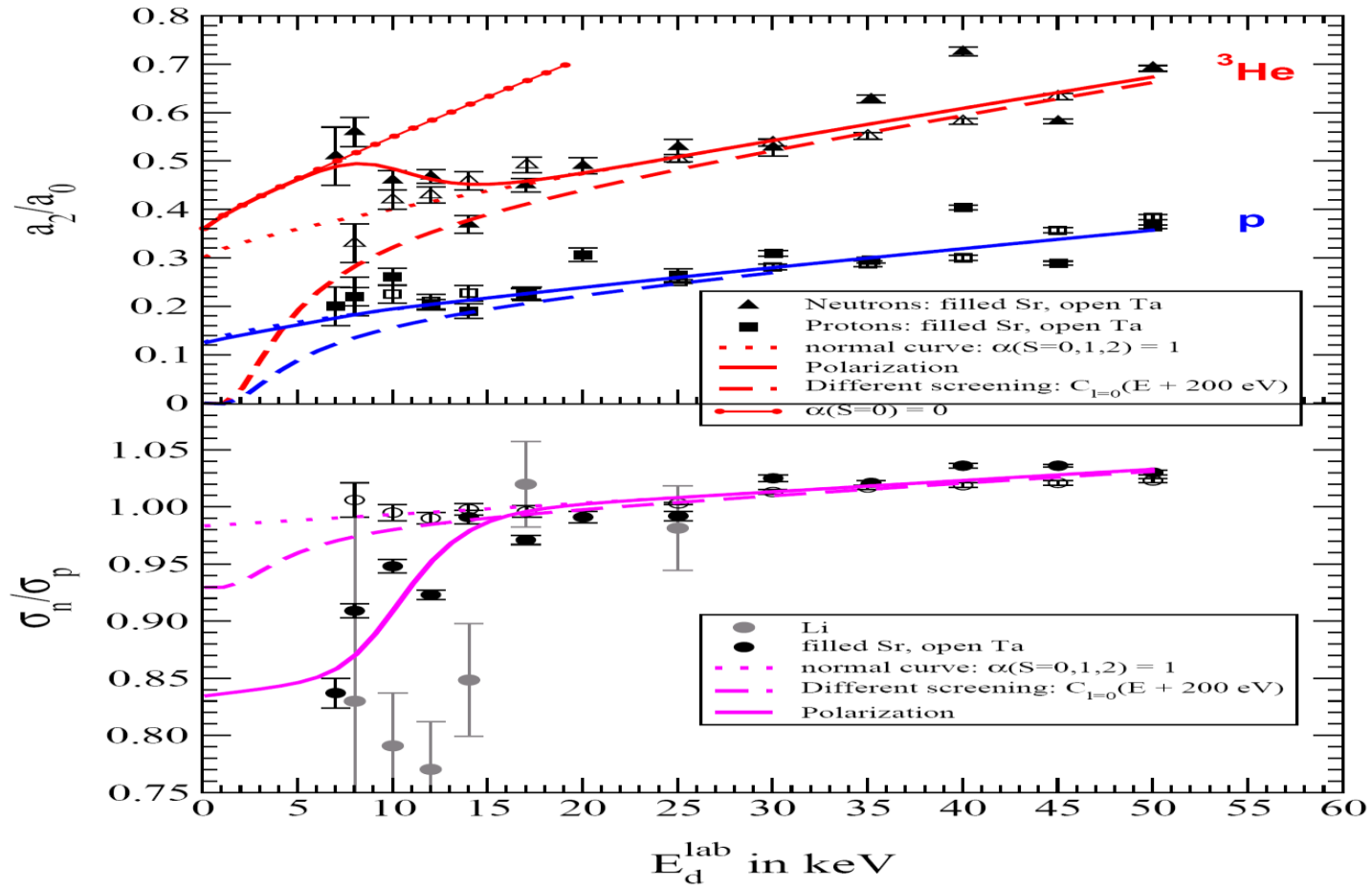
U.Greife et al., Z.Phys. A351 (1995)

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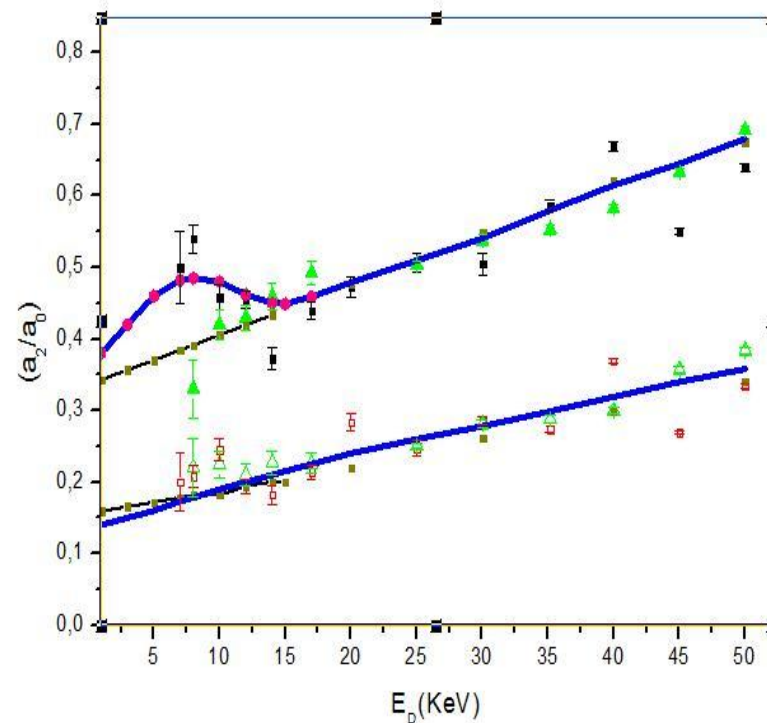
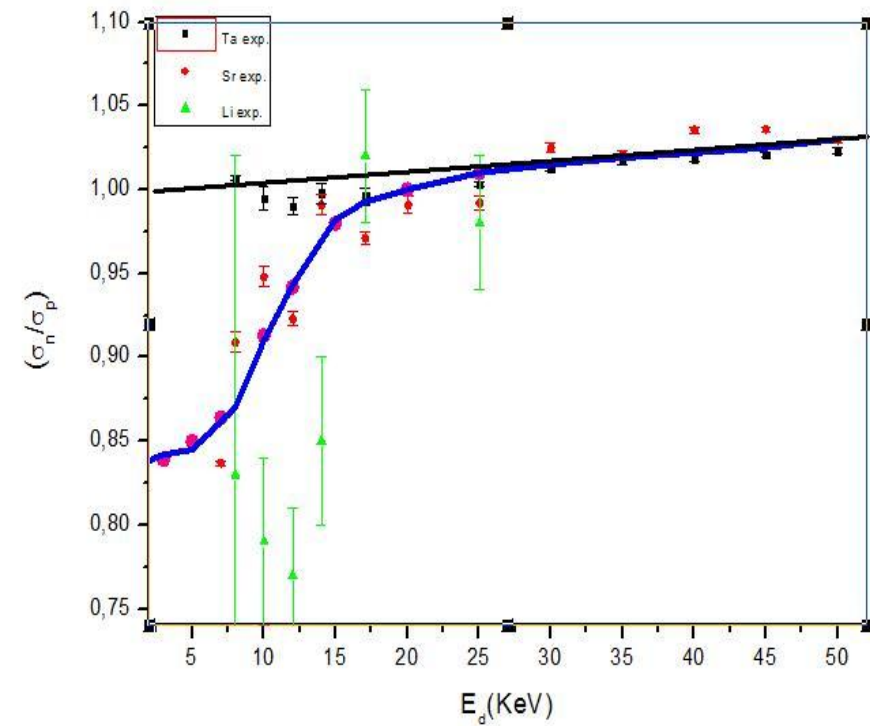
UHV experiments

J.Phys. G, 2008

Experimental results of measurements in metals



Theoretical results for unusual branching ratio and angular distributions



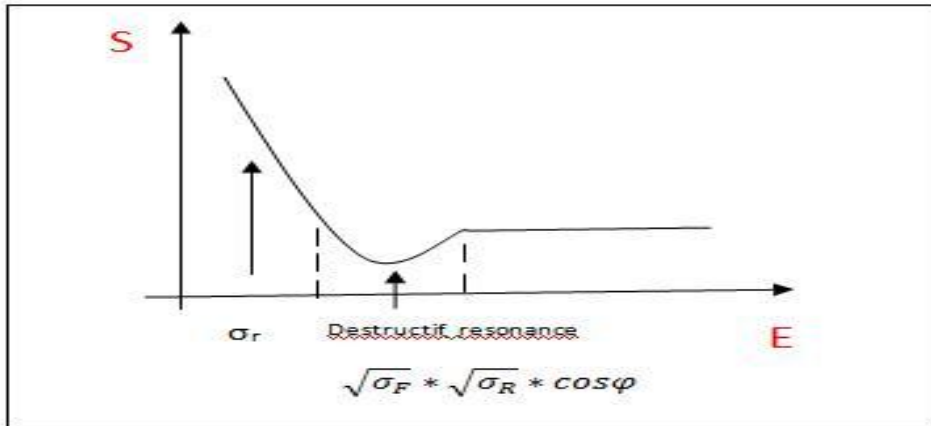
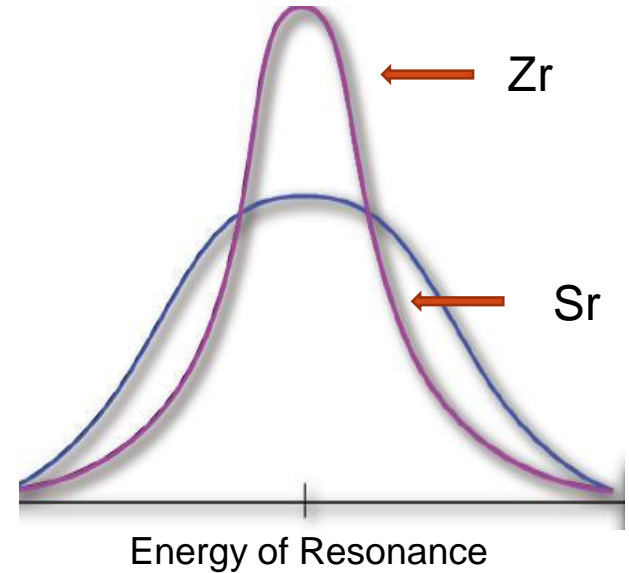
Single particle threshold resonance

$$\sigma = (\sqrt{\sigma_F} + \sqrt{\sigma_R})^2 = \sigma_F + \sigma_R + 2\sqrt{\sigma_F}\sqrt{\sigma_R}\cos\varphi$$

$$\sigma_R \sim \pi\lambda^2 \omega \frac{\Gamma_a * \Gamma_b}{(E - E_R) + \frac{\Gamma^2}{4}} \quad Tg\varphi = \frac{\Gamma}{2(E - E_0)}$$

$$\Gamma_D \gg \Gamma_P \approx \Gamma_n \quad E \gg E_0 \quad E \gg \Gamma$$

new resonance at He⁴ $\sigma = \sigma_F + c\left(1 - \frac{a}{E^2}\right)$



Conclusions

- Simple physical theory, interplay between the electron screening and the resonance excitation, based on known effects, to verify in accelerator experiments, can explain the branching ratio and the angular distributions of the D+d reactions
- The resonance contribution can explain the enhanced electron screening effect observed in metallic environments
- Experiments with atomically clean target are needed