

Fusion hindrance and SHE

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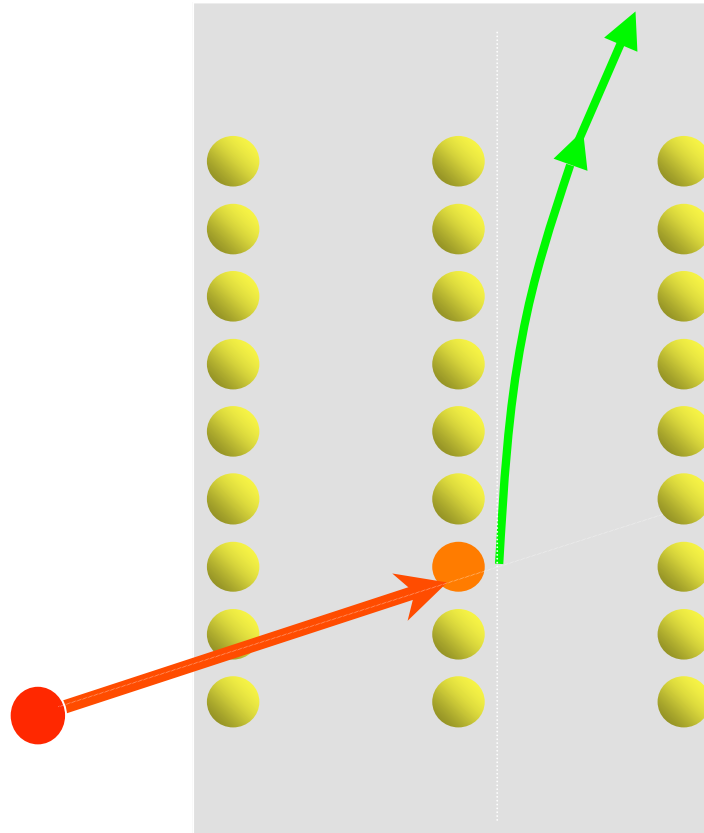
Questions for theoreticians

- Can we guide the experiments ?
- What is the shell correction energy ?

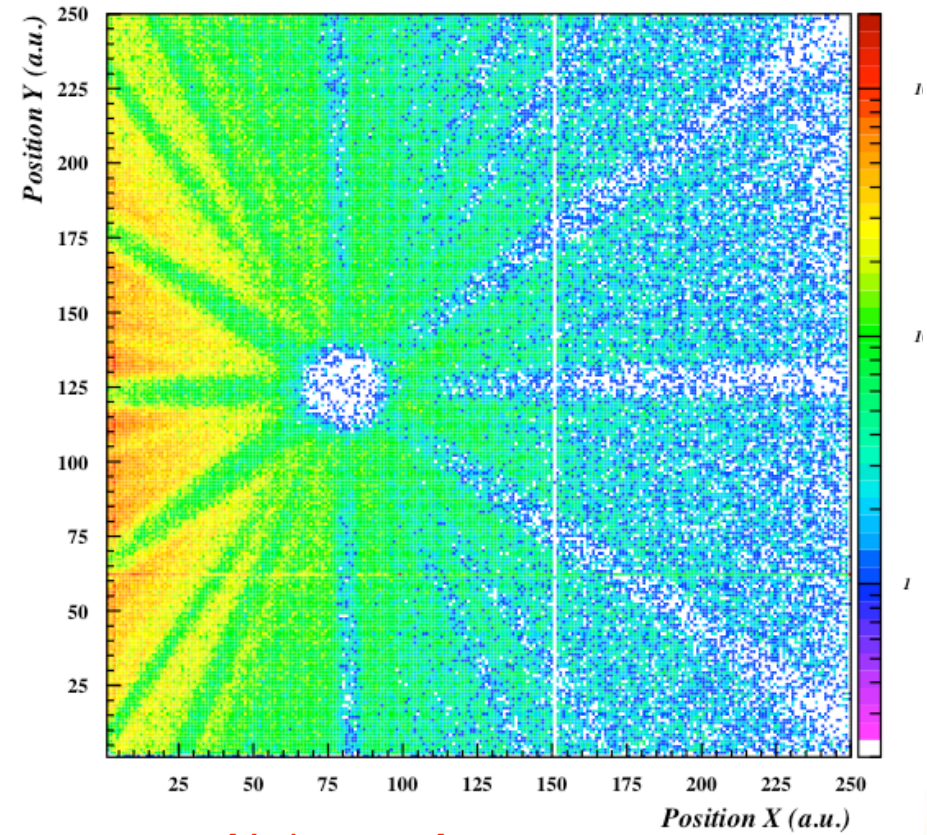
Difficulties

- Models cannot be extrapolated from lighter systems
 - ✦ Fusion hindrance
- Extremely low cross sections
 - ✦ Few data with few information

Blocking technique in crystals



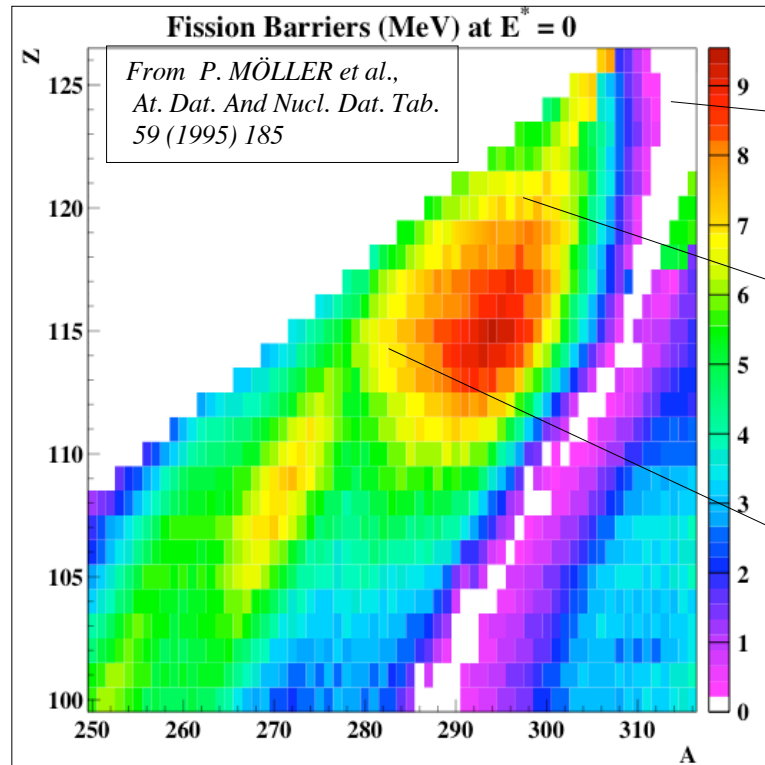
$^{238}\text{U} + ^{28}\text{Si}$ 24 A.MeV
Elastic scattering



F. Goldenbaum et al.,
PRL 82 (1999) 5012

Direct evidence for long fission times

Fission barriers



Mesurements at GANIL by crystal blocking techniques

Z = 124 A = 312

At least 12 % of the capture events with a life time longer than 10^{-18} s

Z = 120 A = 296

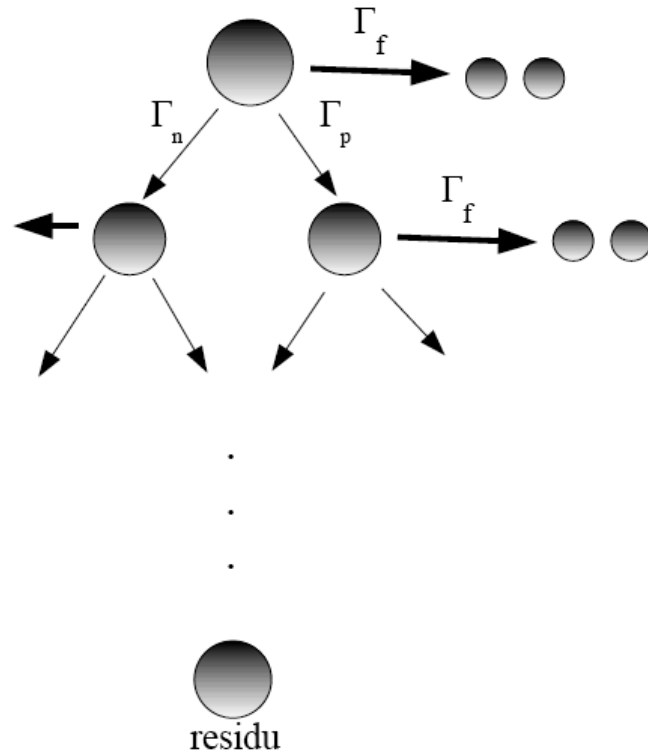
At least 10 % of the capture events with a life time longer than 10^{-18} s

Z = 114 A = 282

Very low statistic or no events with a life time longer than 10^{-18} s

M. Morjean et al, *Eur. Phys. J. D45* (2007) 27
& *PRL101*, 072701 (2008)

$$\frac{1}{\Gamma_f} \approx 10^{-21} \text{ s}$$



$$\frac{dP_i}{dt} = \Gamma_{i-1}^n P_{i-1}(t) - (\Gamma_i^f + \Gamma_i^n) P_i(t)$$

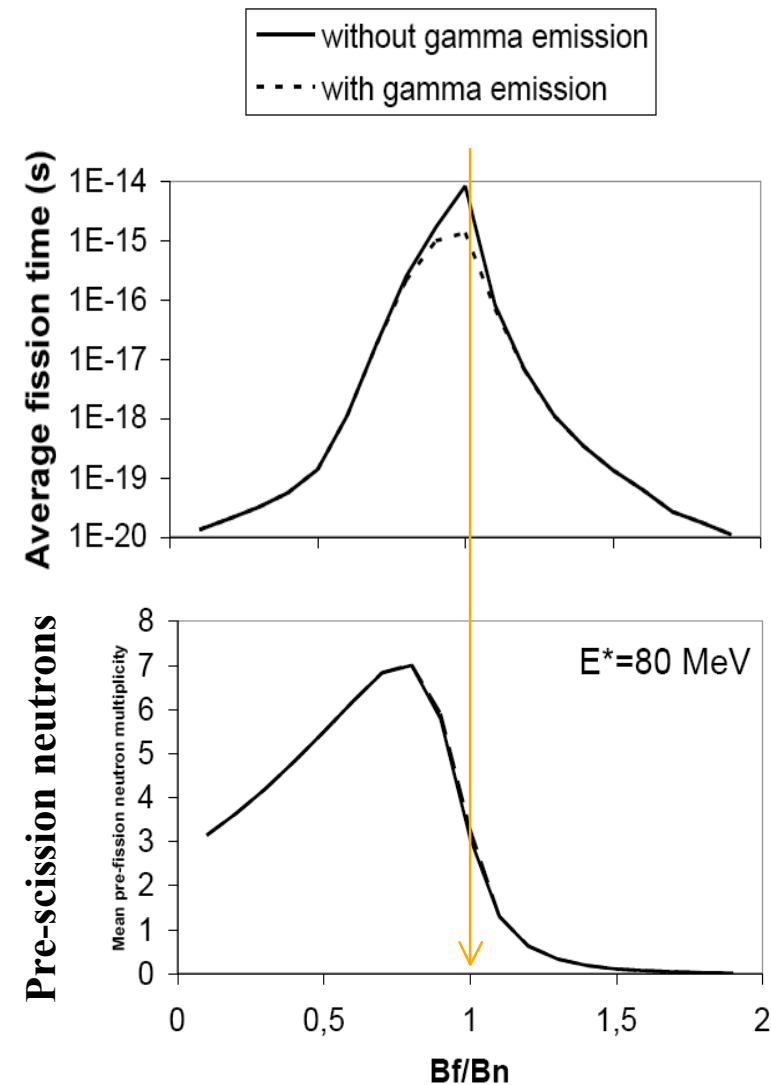
KEWPIE 2

Main ingredients

- Formalism:
 - ◆ Weisskopf or Hauser-Feshbach
 - ◆ Bohr-Wheeler
- Level density:
 - ◆ Bohr-Mottelson with angular dependence
- Level density parameter:
 - ◆ Töke-Swiatecki
 - ◆ Suppression of shell energy corrections according to Ignatyuk
- Collective enhancement included

Simplified model

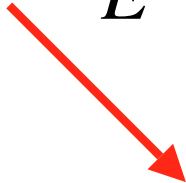
- Fission vs neutron evaporation
- $B_n=6$ MeV & B_f constant along the chain
- Long fission times mean:
 - ◆ $B_f \approx B_n$
 - ◆ Long fission time events occur after evaporation of several neutrons
 - ◆ We cannot extract B_f of each isotope



D.B. et al, IJMP E17 (2008) 1681-1693

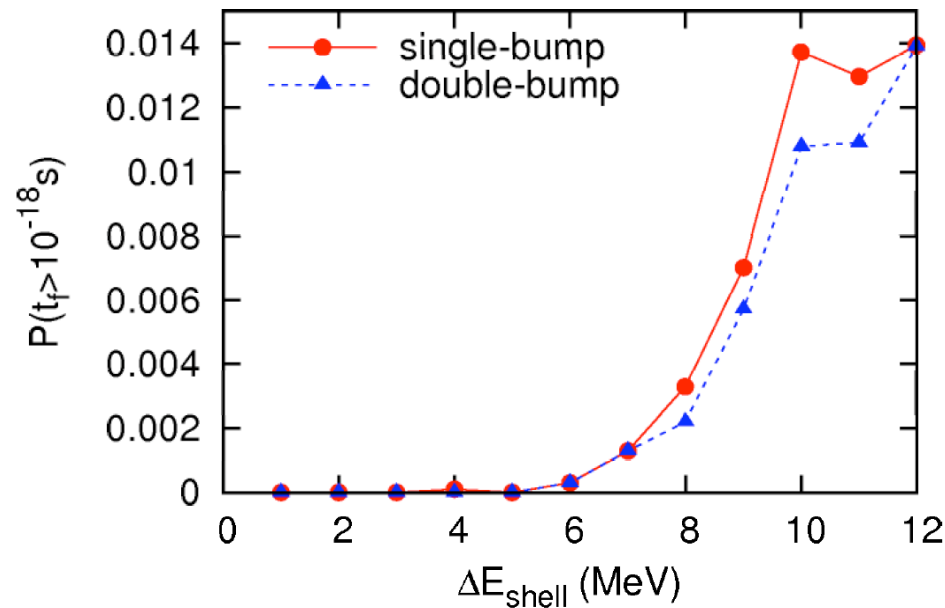
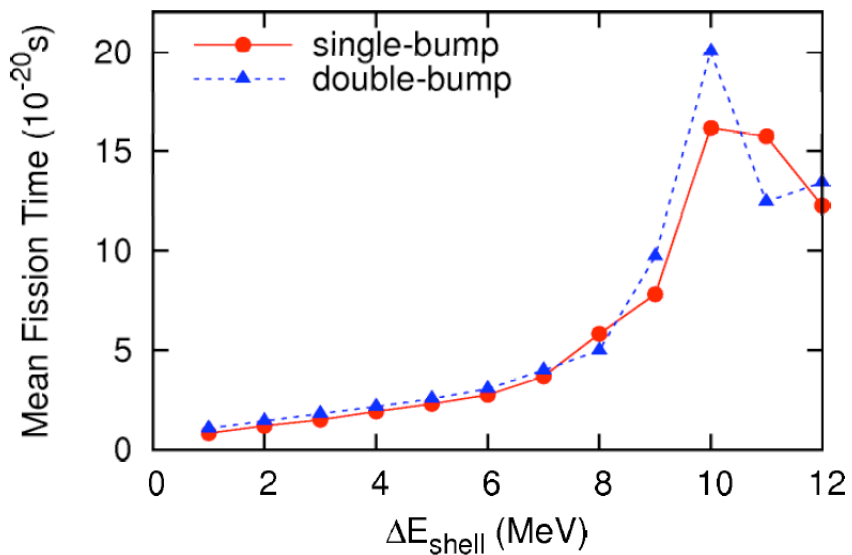
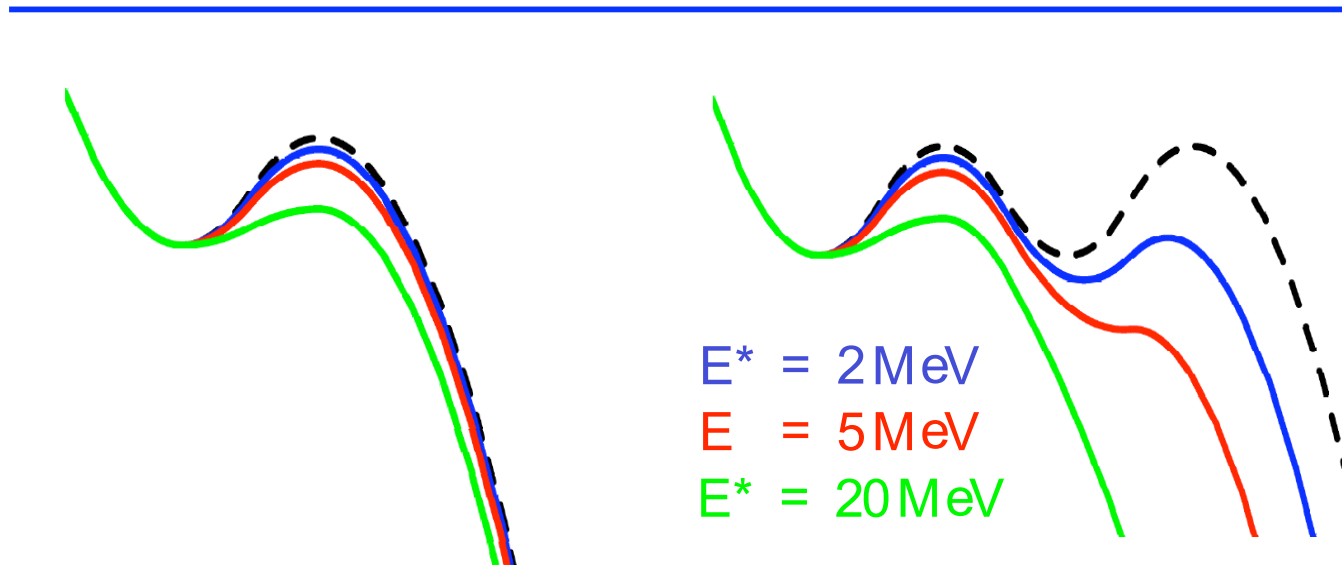
What about ΔE_{shell} ?

$$a_{ground} = a. \left(1 + \frac{(1 - e^{-E^*/E_d}) \cdot \Delta E_{shell}}{E^*} \right)$$

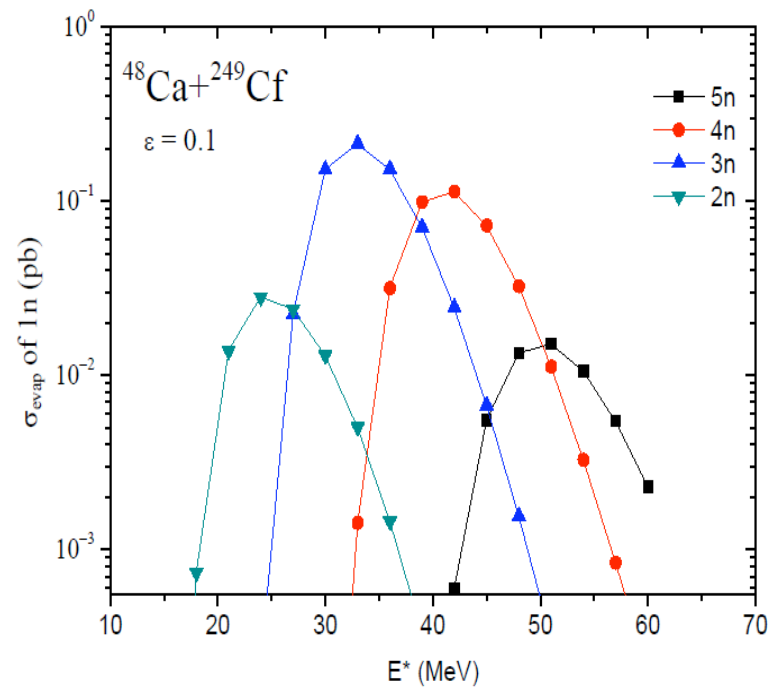

$$B_f \approx e^{-E^*/E_d} \cdot |\Delta E_{shell}|$$

- Experimental results for Z=120 and 124 cannot be reproduced with Möller's table
- Very large ΔE_{shell} for the first isotopes of the evaporation chain
- Potential structure effects ?

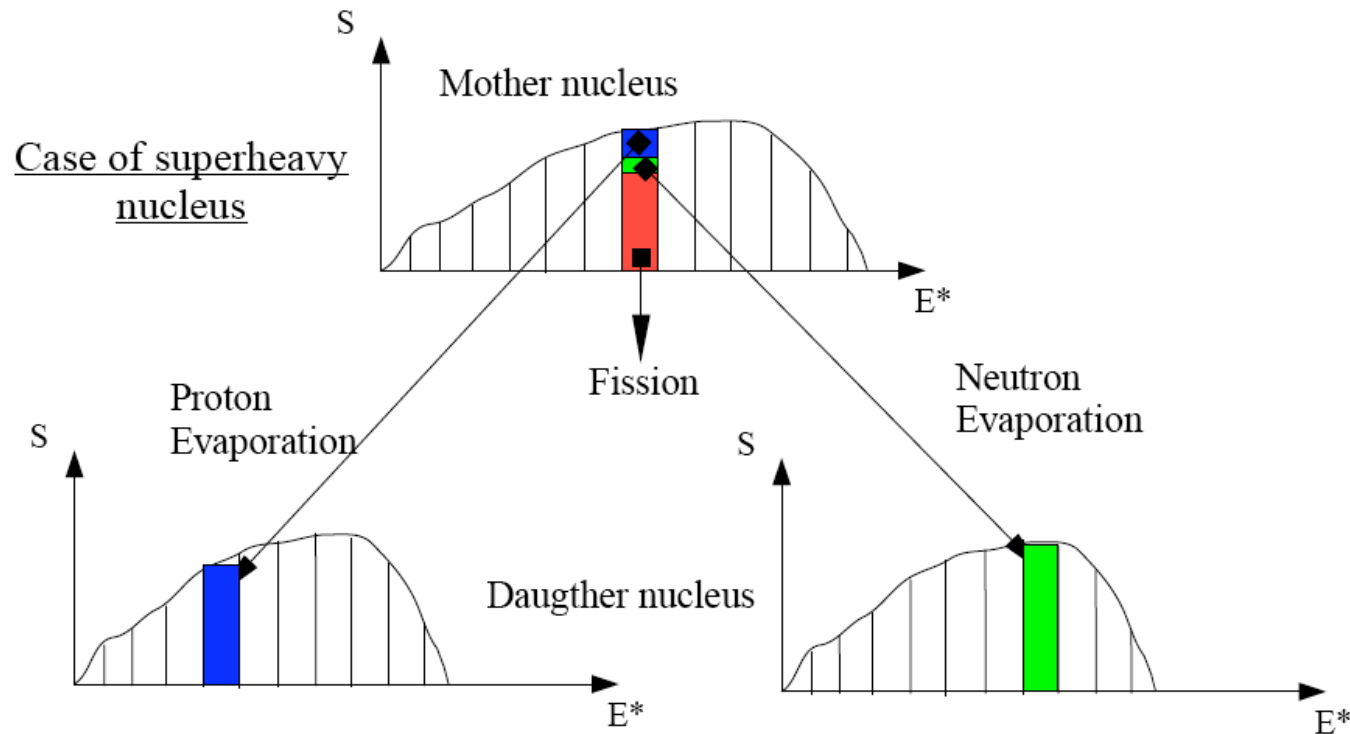
Structure effect 2



Residue cross sections



- It is **not** a Monte-Carlo code to calculate very low probabilities
- It is based on a **discretisation** in bins of the energy spectra:



Residue cross sections

Important parameters of KEWPIE2

- Shell correction energy -> correction factor

$$\Delta E_{shell} = f \cdot \Delta E_{Moller}$$

- Damping Energy E_d

$$a_{ground} = a \cdot \left(1 + \frac{(1 - e^{-E^*/E_d}) \cdot \Delta E_{shell}}{E^*} \right)$$

- ◆ Originally, $E_d = 18.5$ MeV

$$B_f \approx e^{-E^*/E_d} \cdot |\Delta E_{shell}|$$

- Reduced friction

$$\beta = 2 \cdot 10^{21} \text{ s}^{-1}$$

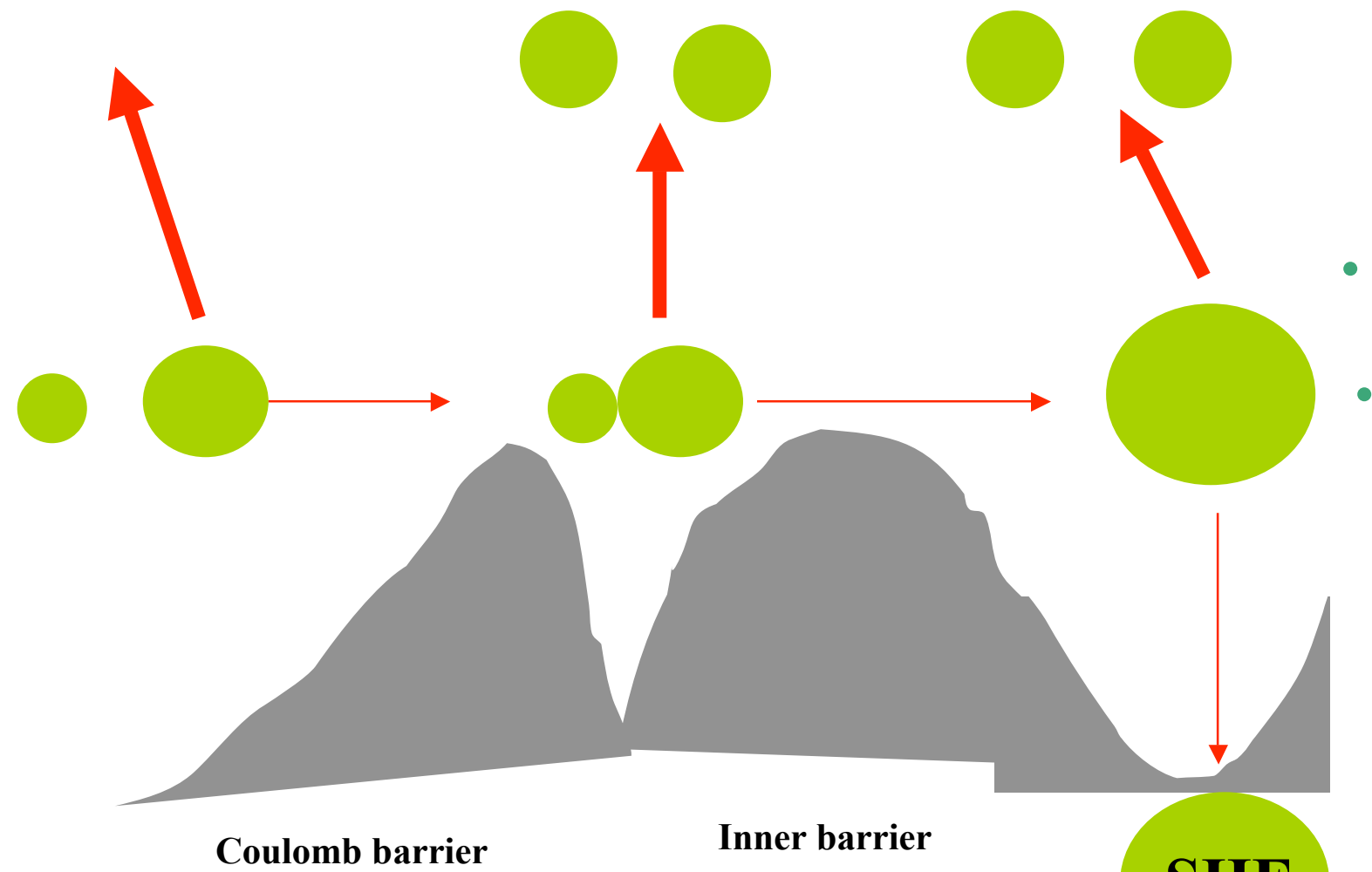
- Fitting the residue cross sections gives very strong constraint on $\Delta E_{\text{shell}} \dots$
 - Precision of 1 MeV
- ... if we know the fusion cross section

Reaction

Reseparation

Quasi-fission

Fission



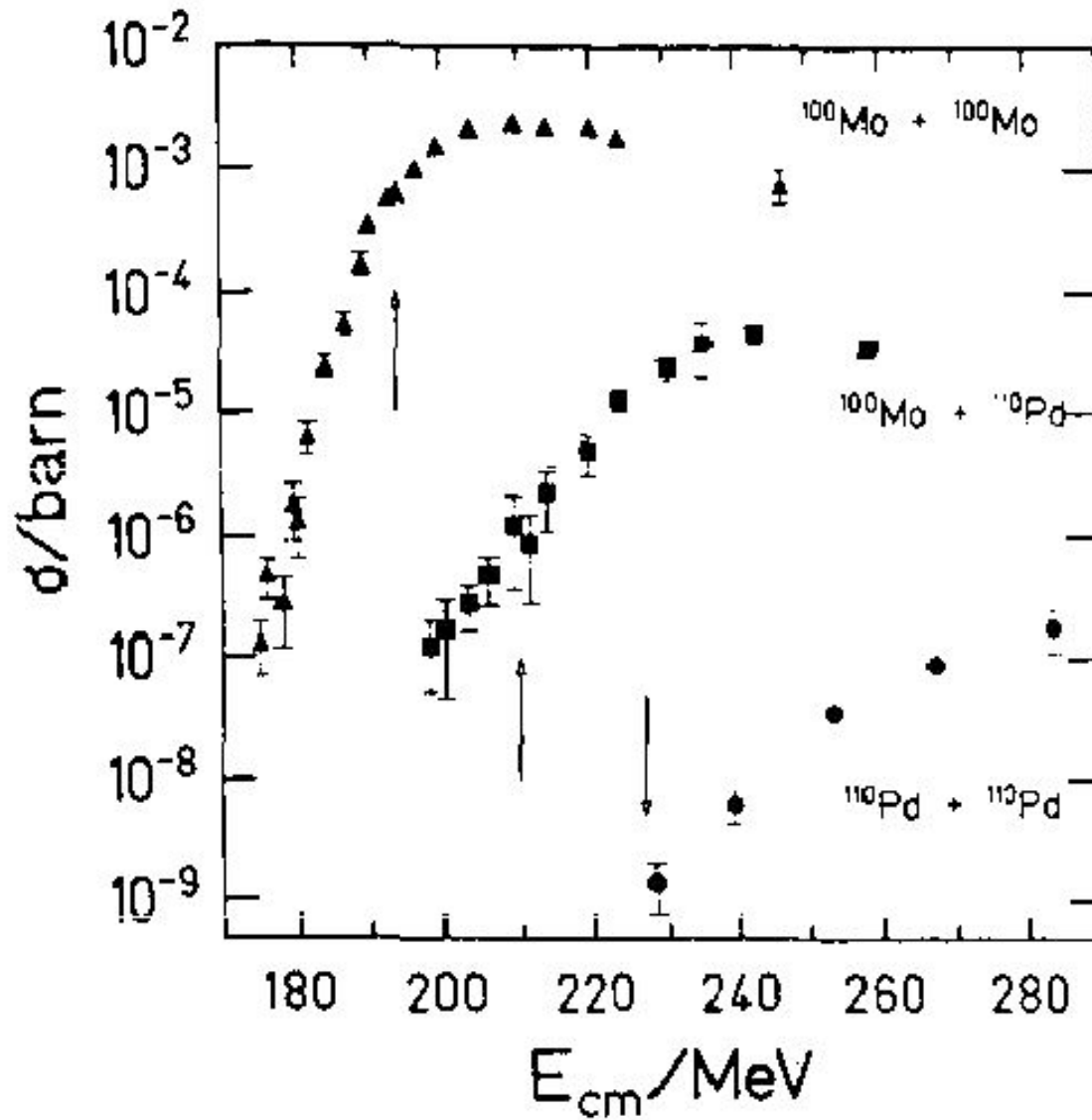
Coulomb barrier

Inner barrier

SHE

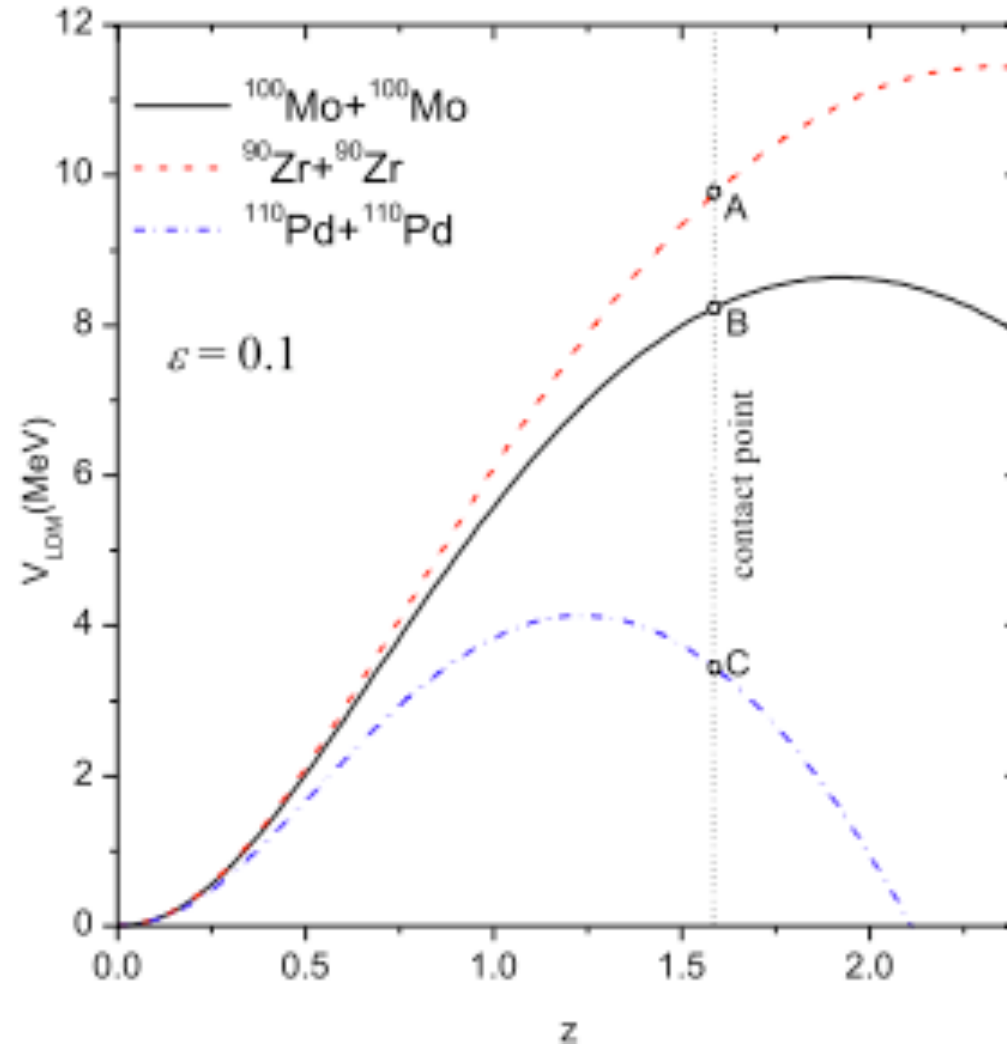
How to assess the fusion model?

Experimental fusion hindrance



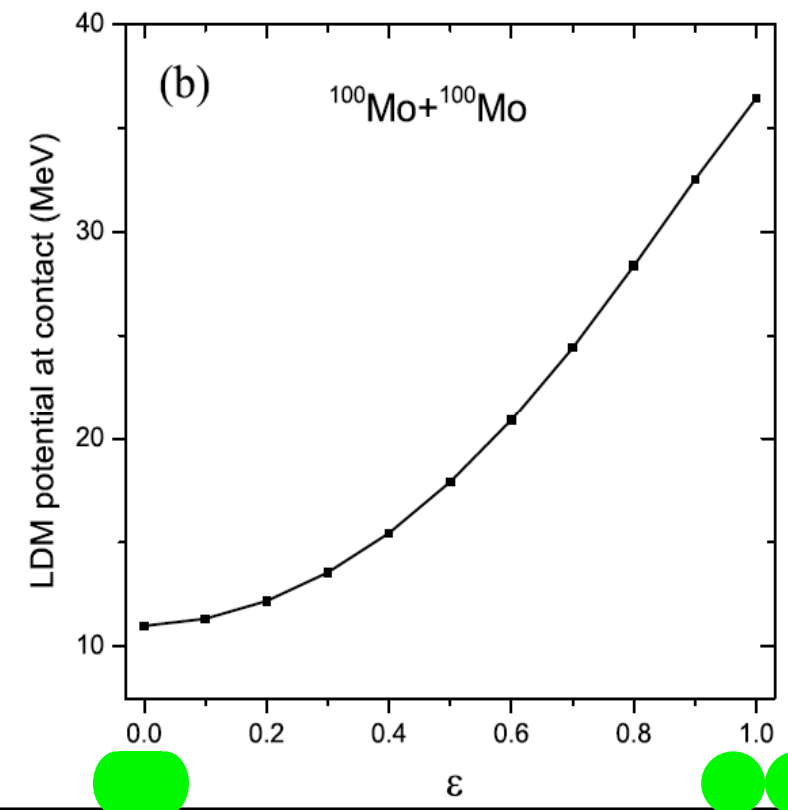
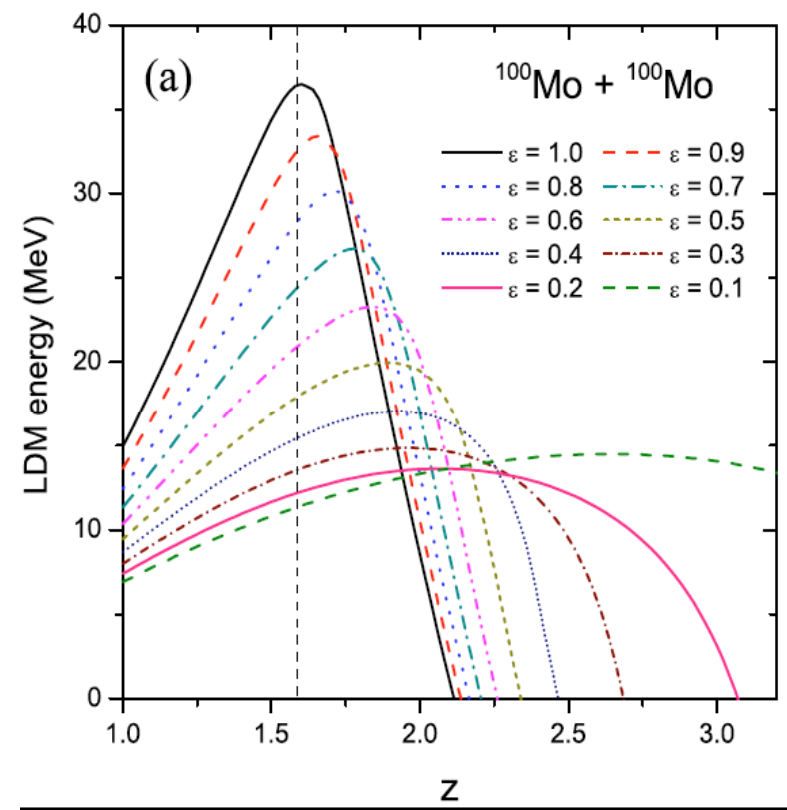
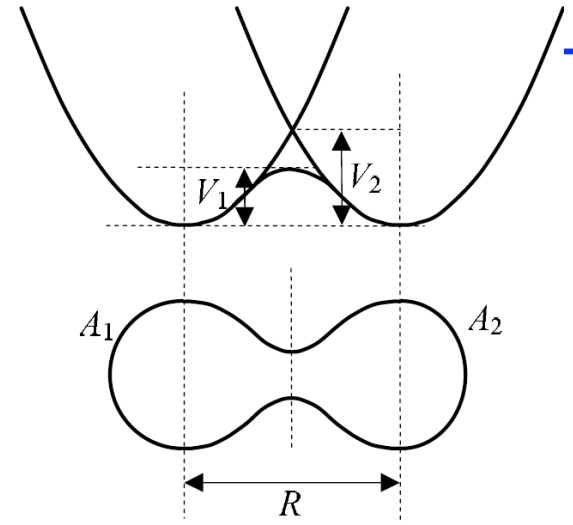
K.-H. Schmidt & W. Morawek *Rep. Prog. Phys.* **54** (1991) 949

Position of the inner barrier

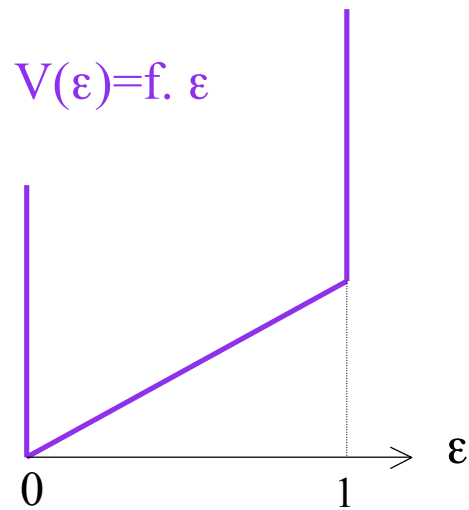


Importance of the neck

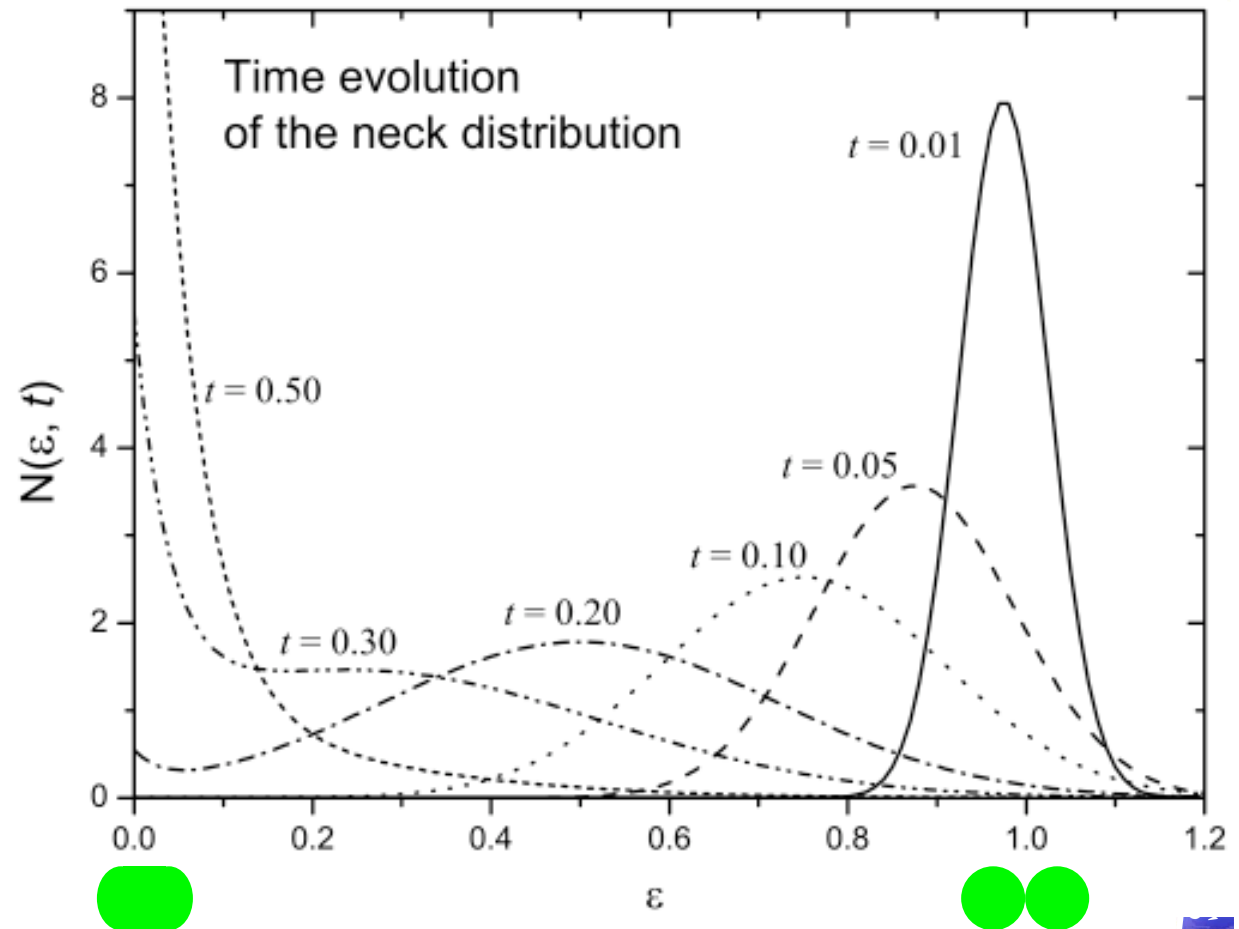
The value of the neck parameter differs from authors



Neck dynamics



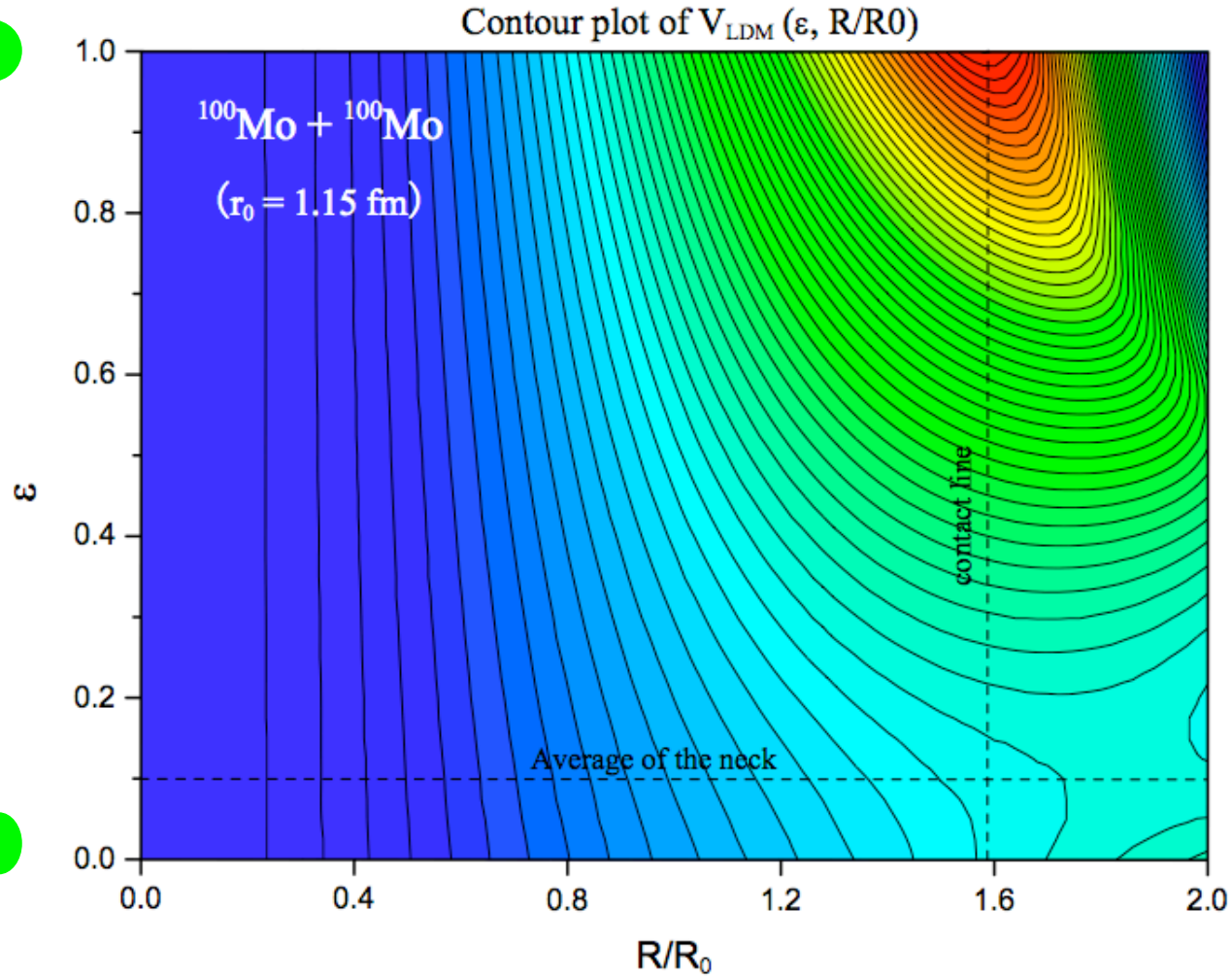
We solved the
Smoluchowski equation



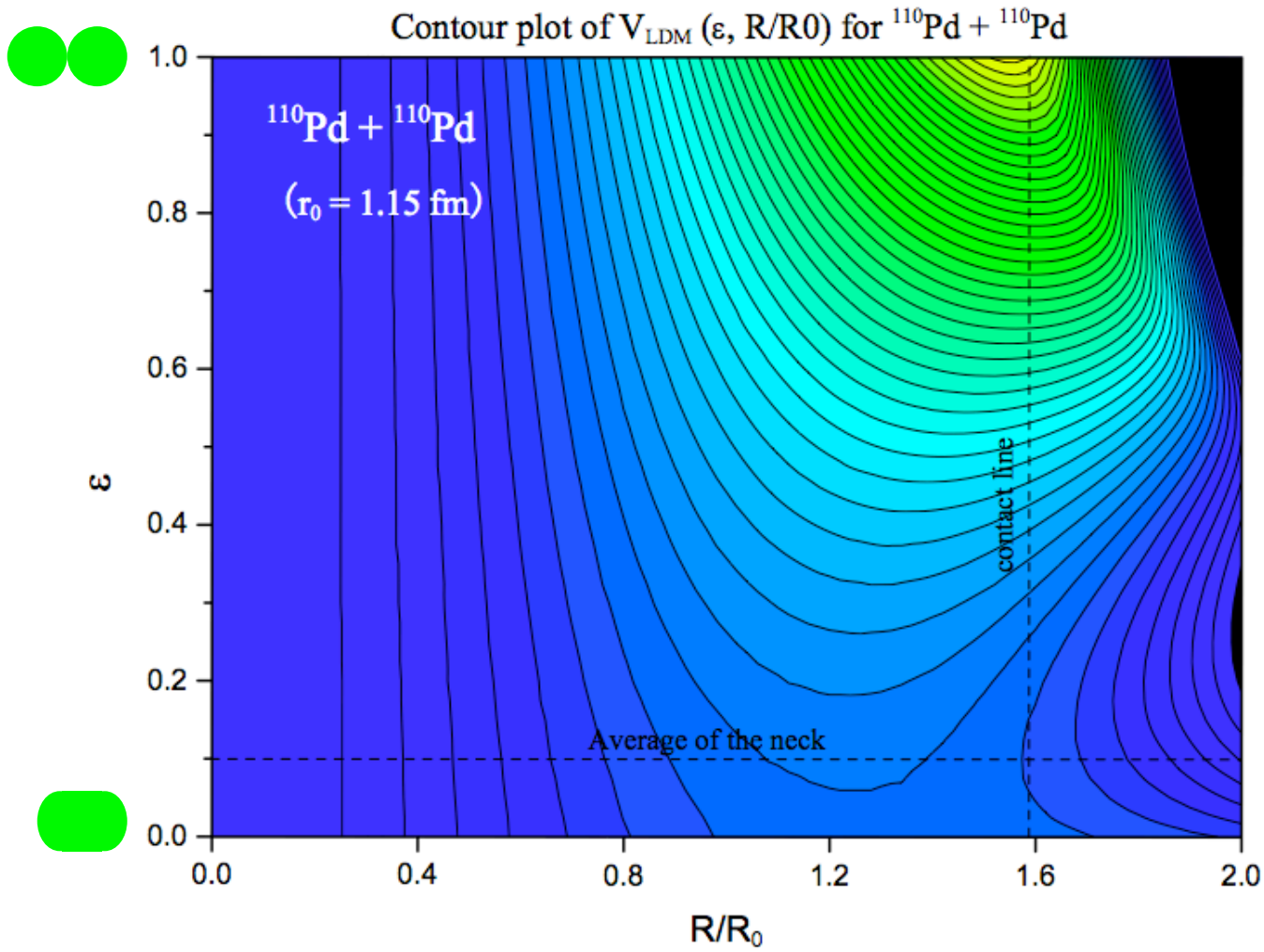
➔ Neck equilibrates very quickly

➔ $\langle \epsilon \rangle \approx 0.1$

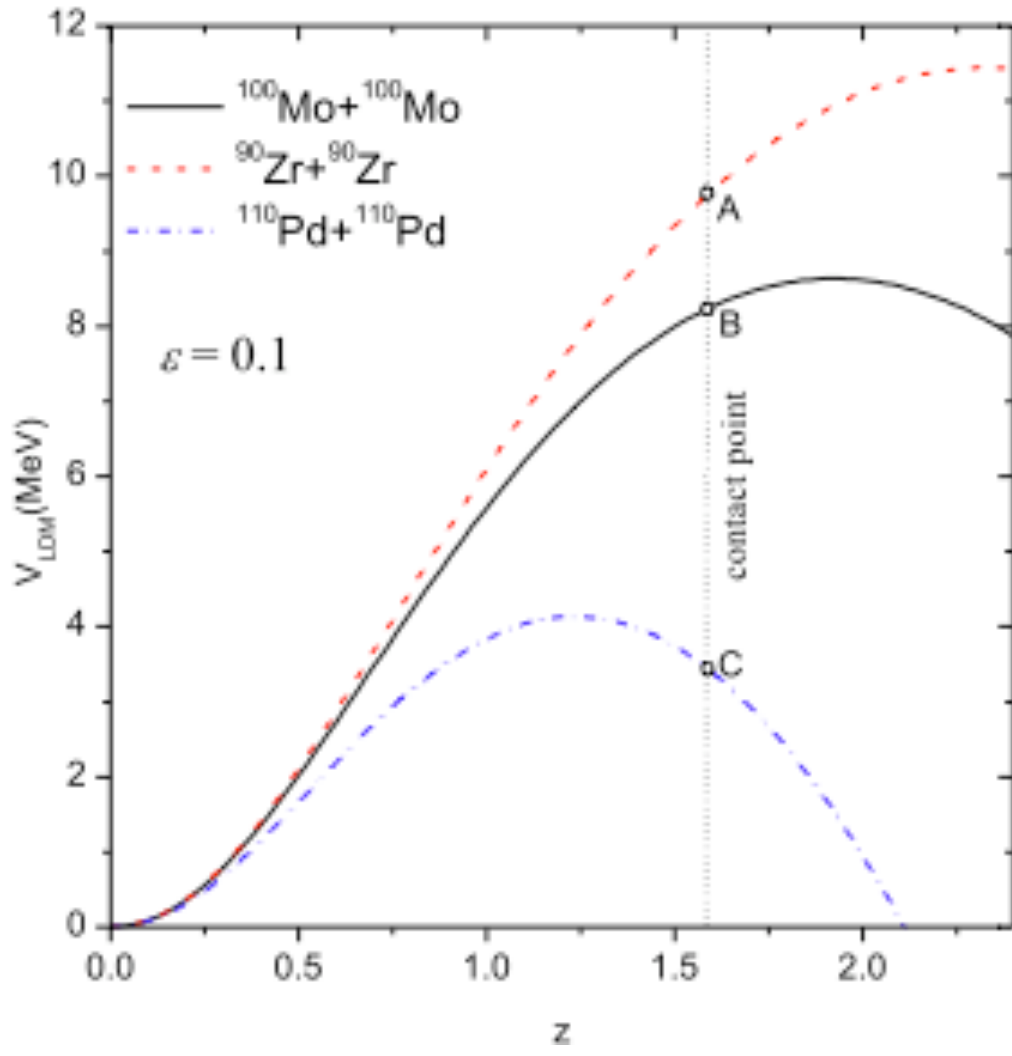
Fusion hindrance for symmetric reactions



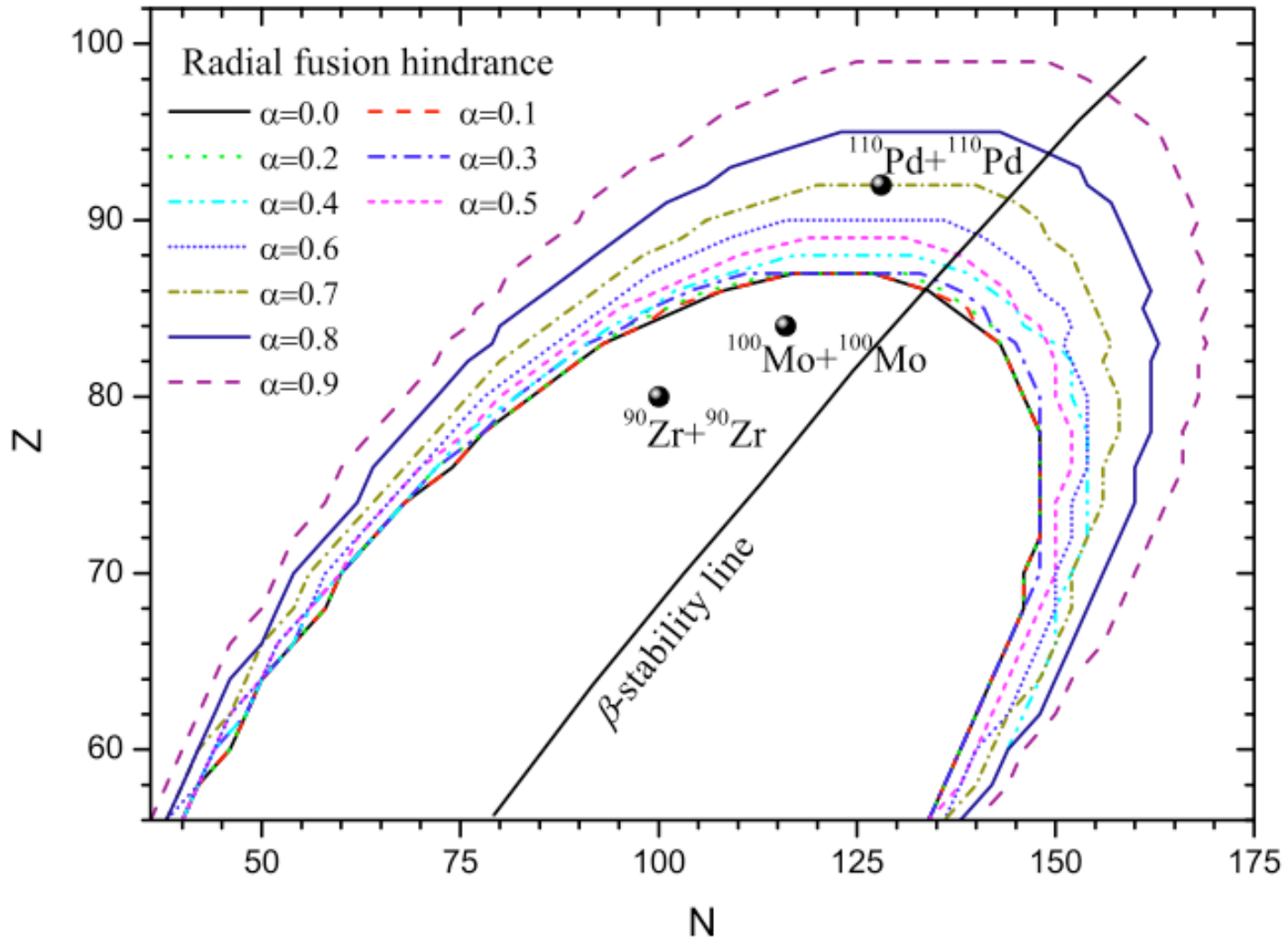
Fusion hindrance for symmetric reactions

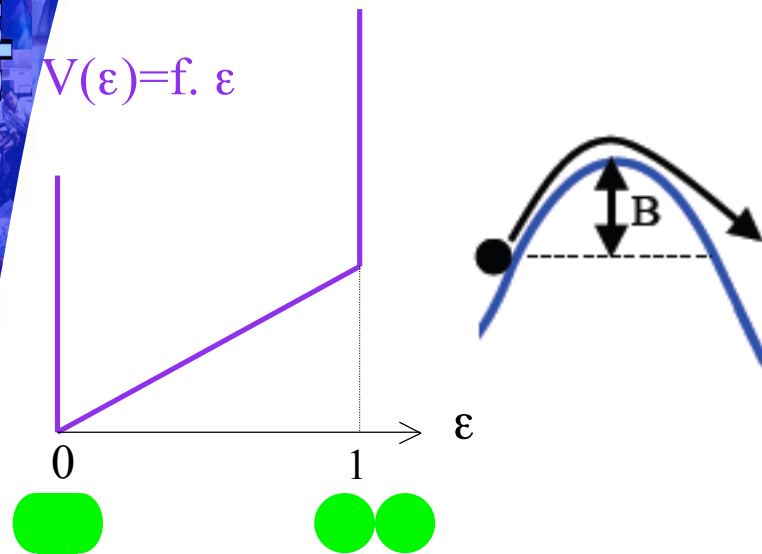


Influence of the shift



Borderline between hindered and non hindered reactions





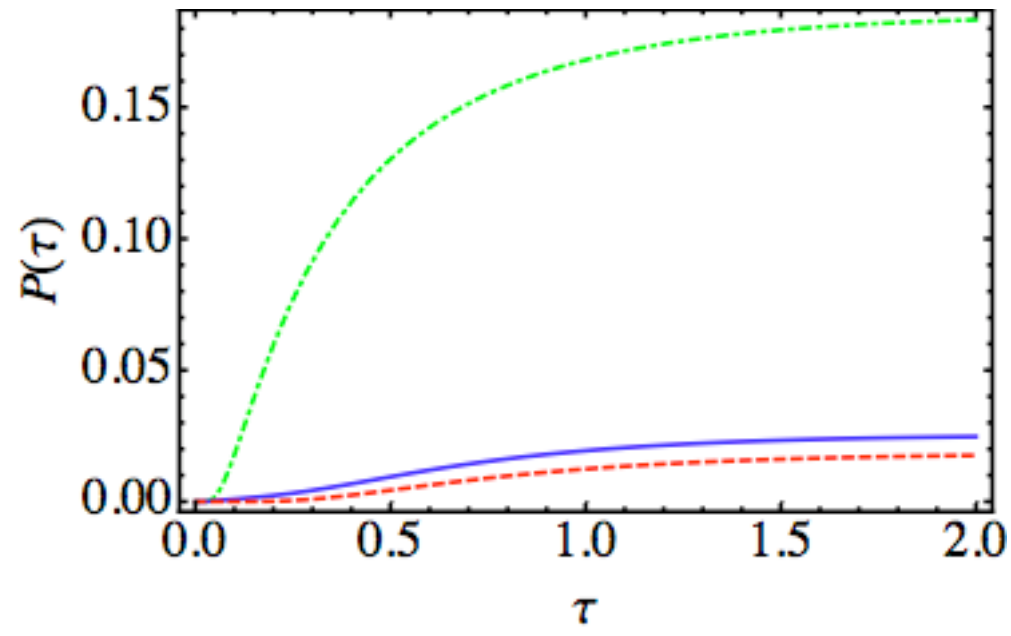
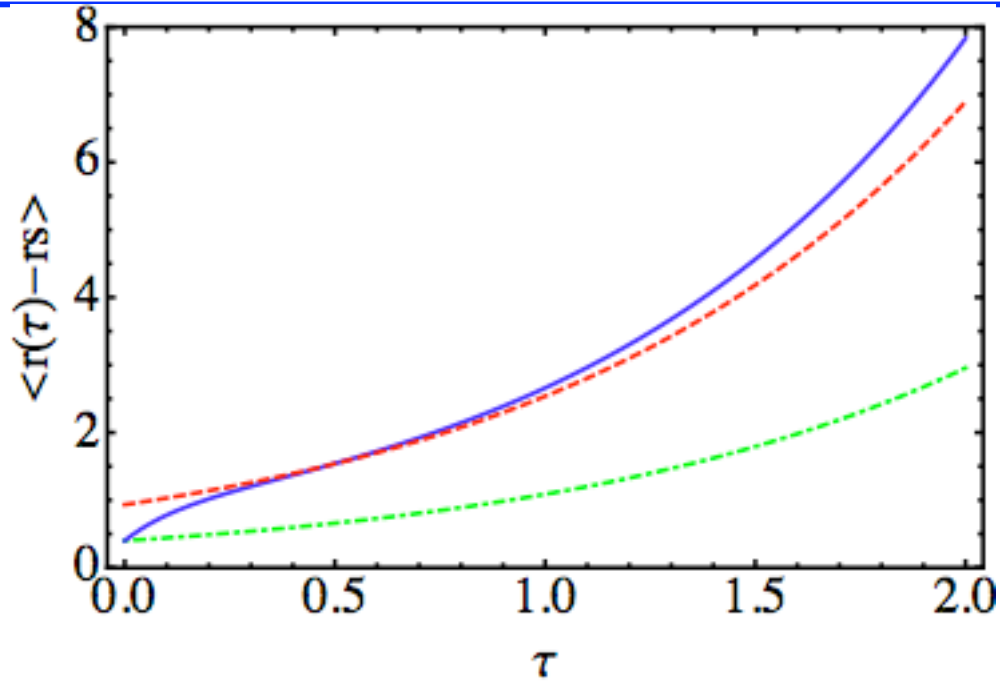
- Fast degree of freedom (neck) vs slow degree of freedom (r)
- Tensor coupling
- Shift of the initial condition in r
- Larger hindrance due to dynamical coupling!

$$[\gamma] \begin{bmatrix} \dot{\varepsilon} \\ \dot{r} \end{bmatrix} = - \begin{bmatrix} \partial V / \partial \varepsilon \\ \partial V / \partial r \end{bmatrix} + \begin{bmatrix} \rho_1(t) \\ \rho_2(t) \end{bmatrix},$$

$$\Delta r \simeq - \frac{\gamma_{r\varepsilon}}{\gamma_{rr}} \Delta \varepsilon.$$

Test on a simple case

**Exact
solution for a
saddle made
with 2
parabolas**



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