

# Microscopic description of temperature, pairing and deformation effects in nuclei

**E. Khan**



# Normal to superfluid (phase) transition in nuclei

**Normal phase**

Symmetric

Hot nucleus:  $T > T_c$

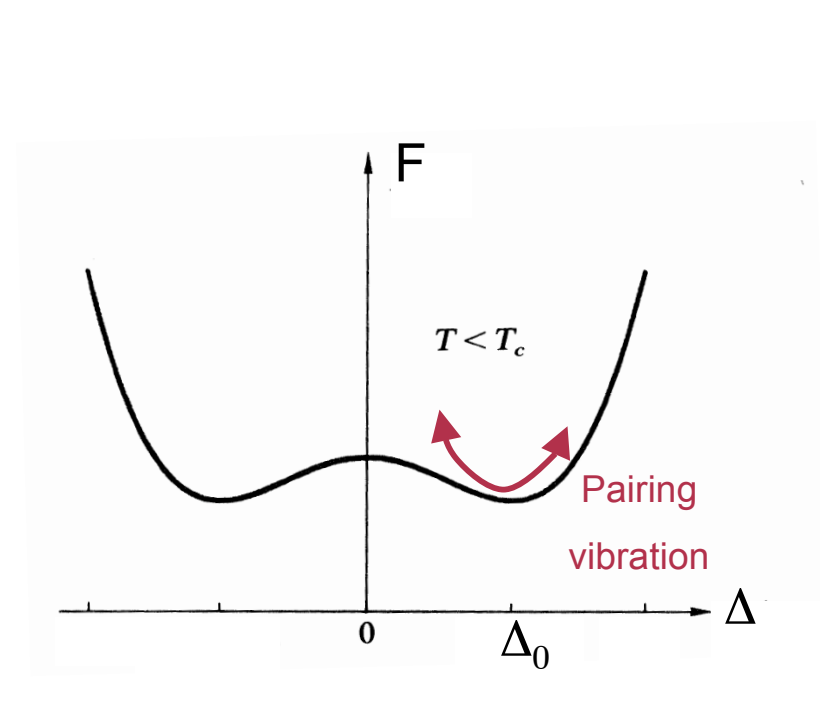
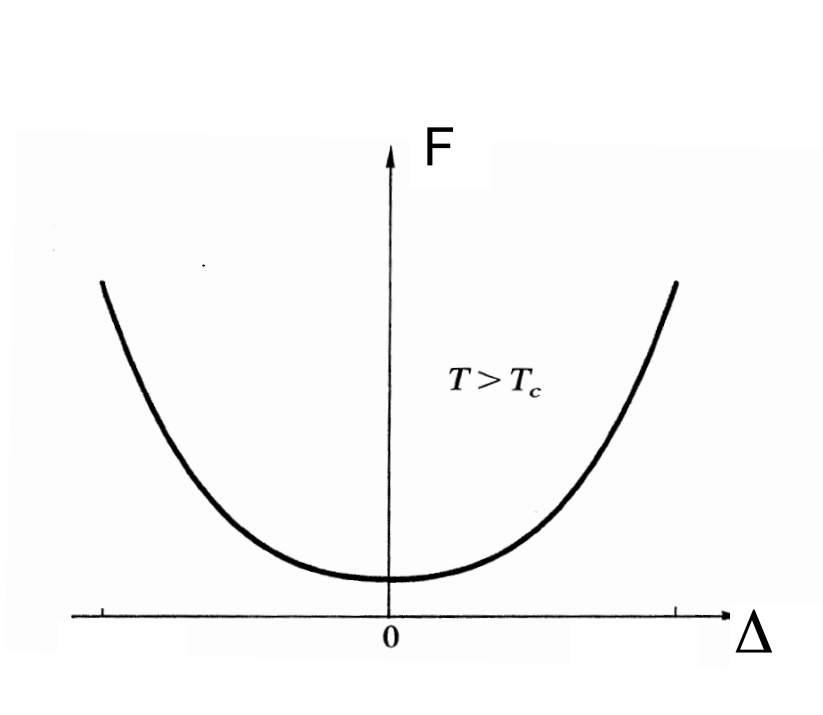
**Superfluid phase**

Spontaneous symmetry breaking

Nucleus:  $T < T_c$

2<sup>d</sup> order phase transition

$\Delta$  pairing gap: order parameter



# Finite temperature HFB

- **Goal:** describe the normal to superfluid transition in a self-consistent approach

A.L. Goodman NPA352 (81) 30

- **Method:** Grand canonical ensemble

Density matrix depends on Fermi-Dirac occ.

$$f_i = \frac{1}{1 + e^{\beta E_i}}$$

—————> Same equation than HFB, except for the densities:

$$\rho = U^T f U^* + V^\dagger (1 - f) V$$

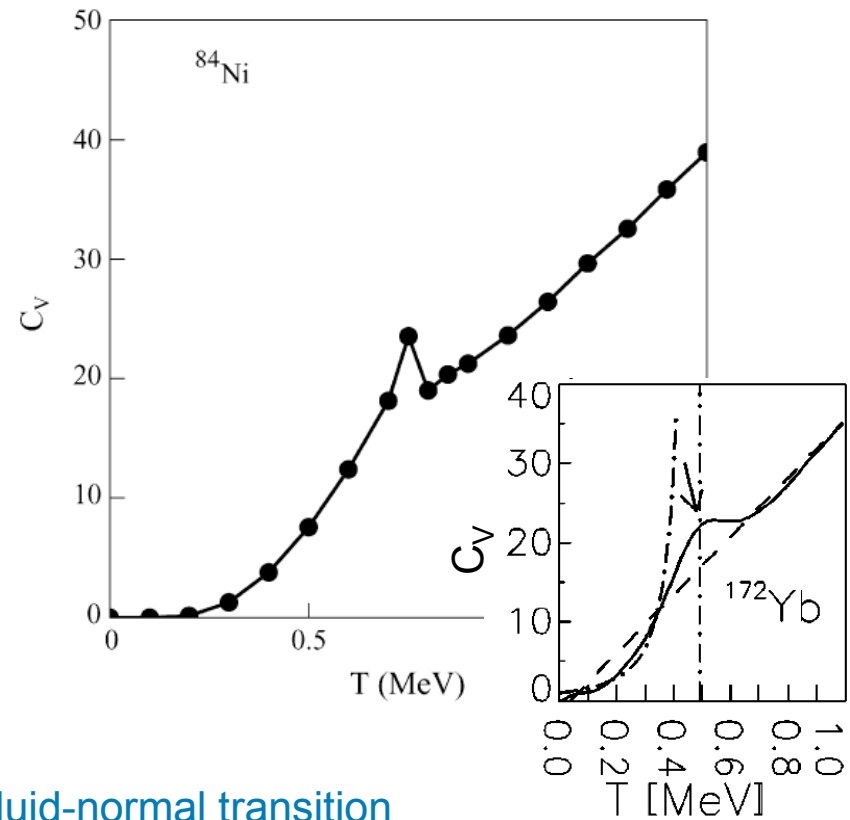
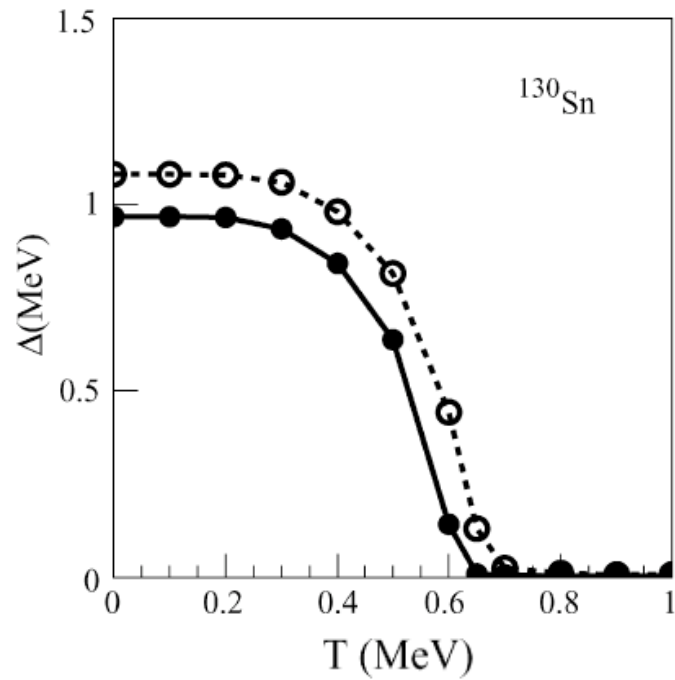
$$\kappa = U^T f V^* + V^\dagger (1 - f) U$$

- Self consistent calculations:

**Gogny:** shape transition J.L. Egido, L.M. Robledo, V. Martin, PRL85 (00) 26

**Skyrme:** superfluid-normal transition E. Khan, N. Van Giai, N. Sandulescu, NPA789 (07) 94

# Skyrme FT-HFB results



- Relevant description of the superfluid-normal transition
- $T_c$  dependence on the volume/surface nature of the pairing interaction

# Finite temperature QRPA

- **Goal:** compare Cv with measurements of excited states (Oslo group)

A. Schiller et al., PRC63 (01) 021306(R)

- **Method:** FT-QRPA coordinate space formalism with Fermi-Dirac terms in the unperturbed Green function.

$$\mathbf{G} = (\mathbf{1} - \mathbf{G}_0 \mathbf{V})^{-1} \mathbf{G}_0 = \mathbf{G}_0 + \mathbf{G}_0 \mathbf{V} \mathbf{G}$$

$$\text{Residual interaction: } \mathbf{V}^{\alpha\beta}(\mathbf{r}\sigma, \mathbf{r}'\sigma') = \frac{\partial^2 \mathcal{E}}{\partial \rho_\beta(\mathbf{r}'\sigma') \partial \rho_\alpha(\mathbf{r}\sigma)}$$

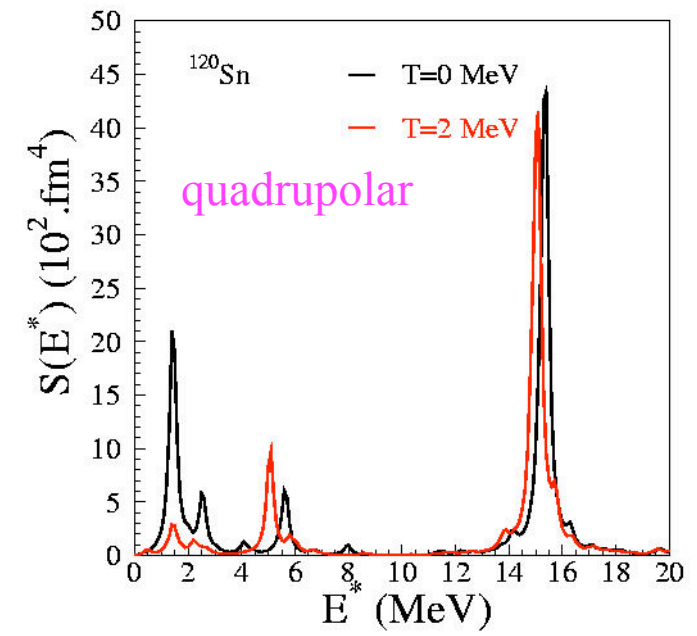
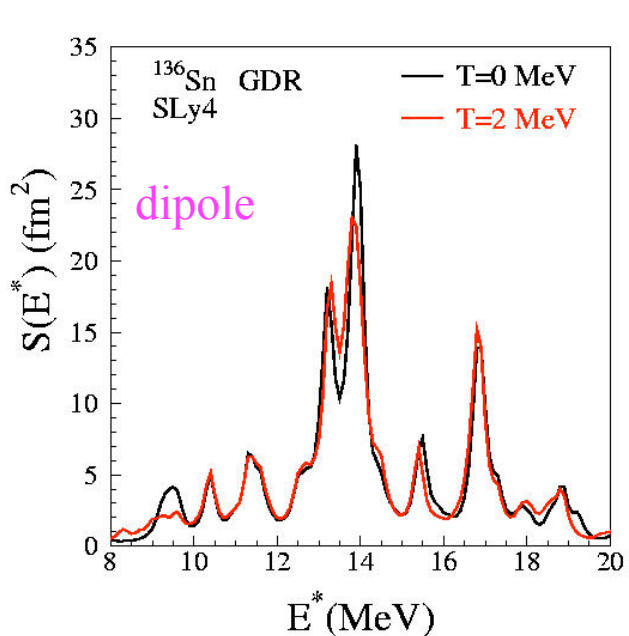
$$G_0^{11}(1, 1'; \omega) = \sum_{ij} \frac{U_i^*(1)U_j(1)U_j^*(1')U_i(1')}{\hbar\omega + i\eta + E_i - E_j} (f_i - f_j) + \frac{U_i^*(1)U_j(1)V_i(1')V_j^*(1')}{\hbar\omega + i\eta + E_i - E_j} (f_j - f_i)$$

**T ≠ 0**

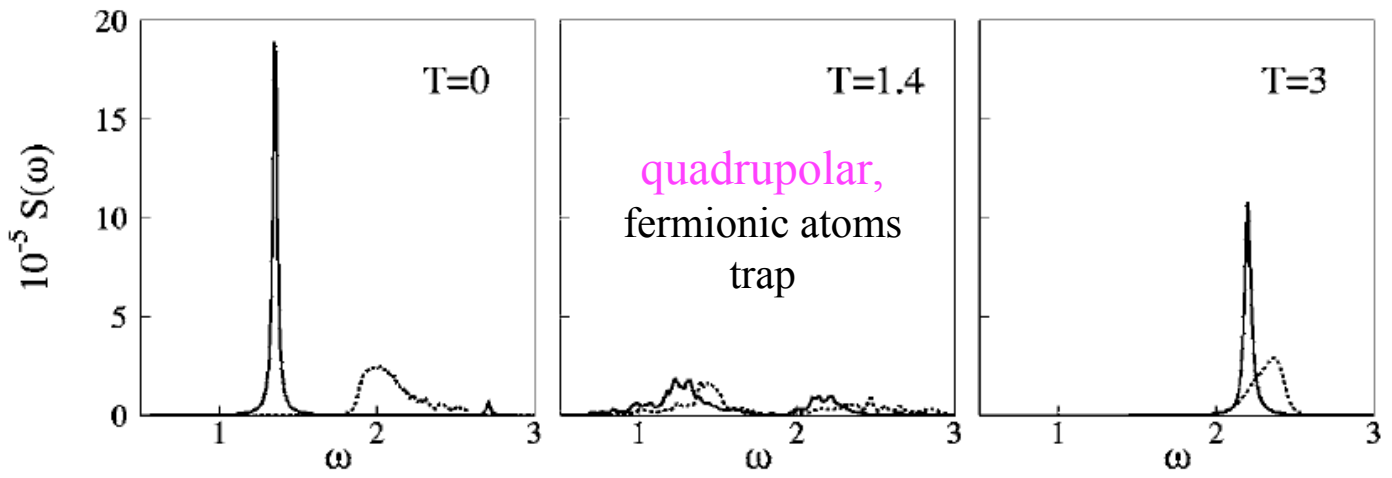
$$+ \frac{V_i(1)V_j^*(1)V_j(1')V_i^*(1')}{\hbar\omega + i\eta - E_i + E_j} (f_j - f_i) + \frac{V_i(1)V_j^*(1)U_j^*(1')U_i(1')}{\hbar\omega + i\eta - E_i + E_j} (f_i - f_j)$$

$$+ \frac{V_i(1)U_j(1) [U_j^*(1')V_i^*(1')]}{\hbar\omega + i\eta - E_i - E_j} (1 - f_i - f_j) + \frac{U_i^*(1)V_j^*(1) [V_j(1')U_i^*(1')]}{\hbar\omega + i\eta + E_i + E_j} (f_i + f_j - 1)$$

# FT-QRPA results



E. Khan, Nguyen Van Giai, M. Grasso, NPA731 (04) 311

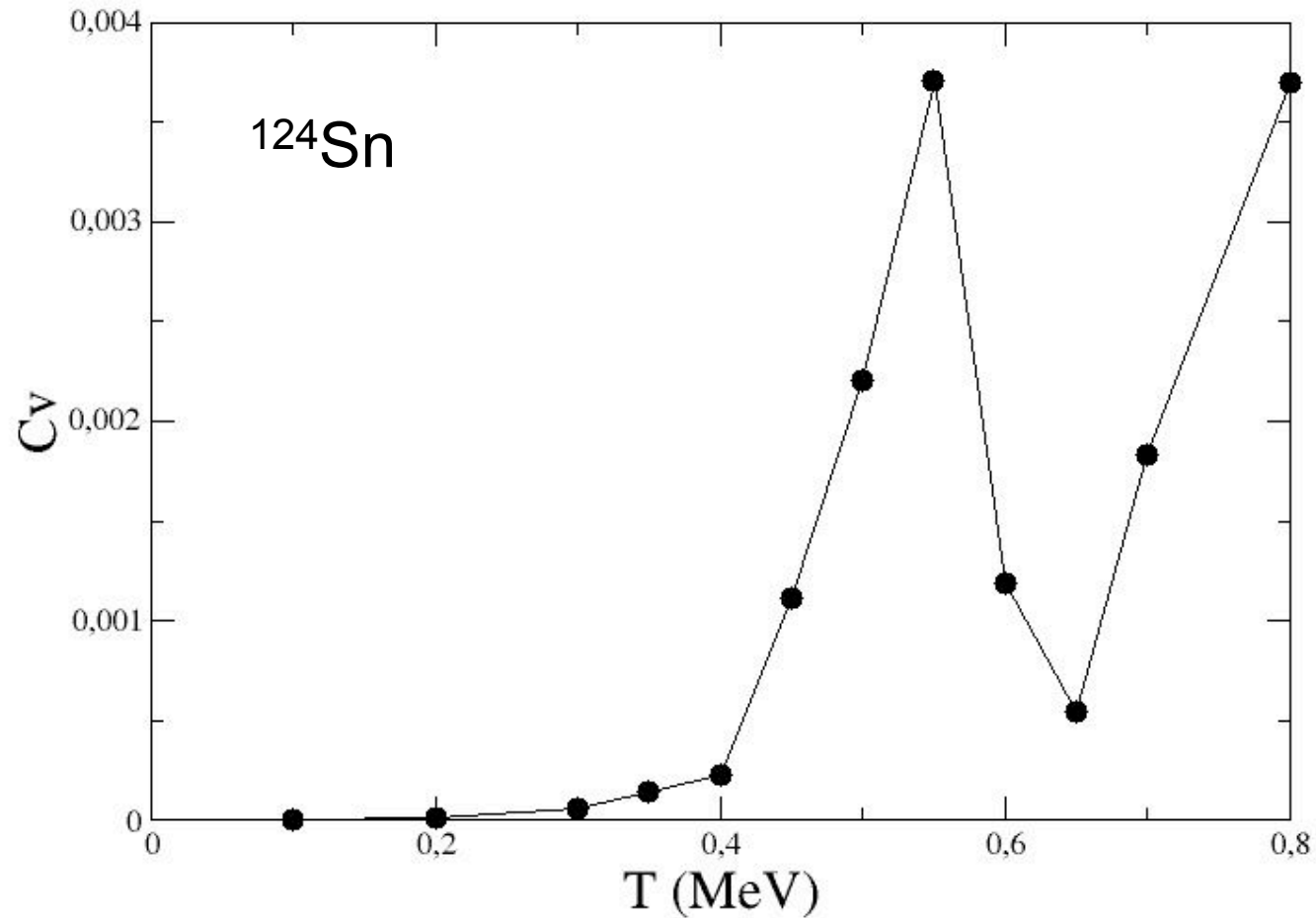


M. Grasso, E. Khan, M. Urban, PRA72 (05) 043617

## Cv calculations

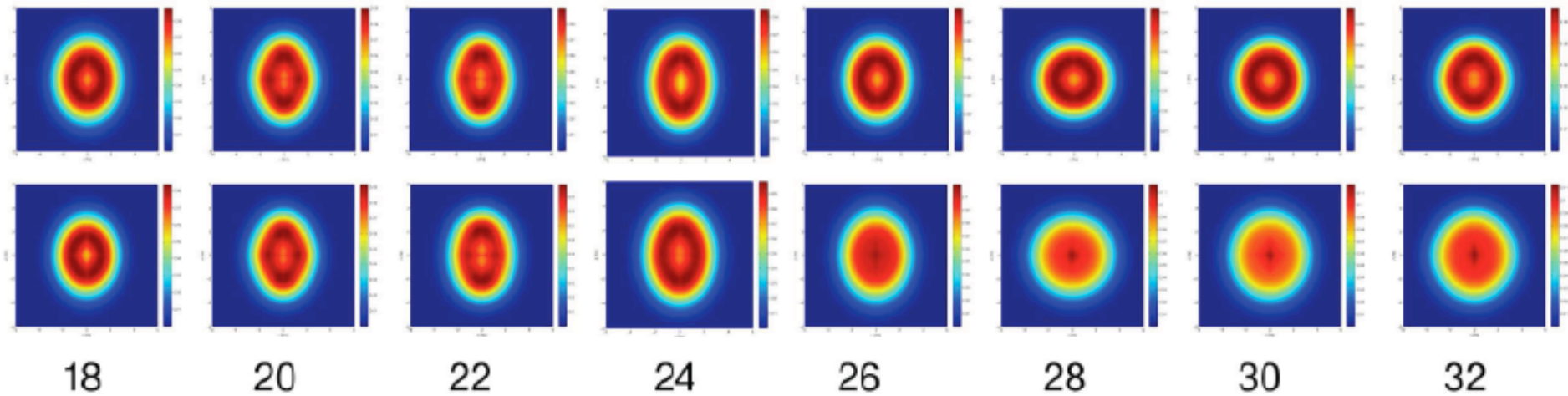
- **Method:** calculate all possible  $J^\pi$  QRPA responses below 5 MeV:  $0^+$  to  $10^+$

- **Cv from S:** 
$$S = - \sum_i (2j_i + 1) (f_i \ln f_i + (1 - f_i) \ln(1 - f_i))$$

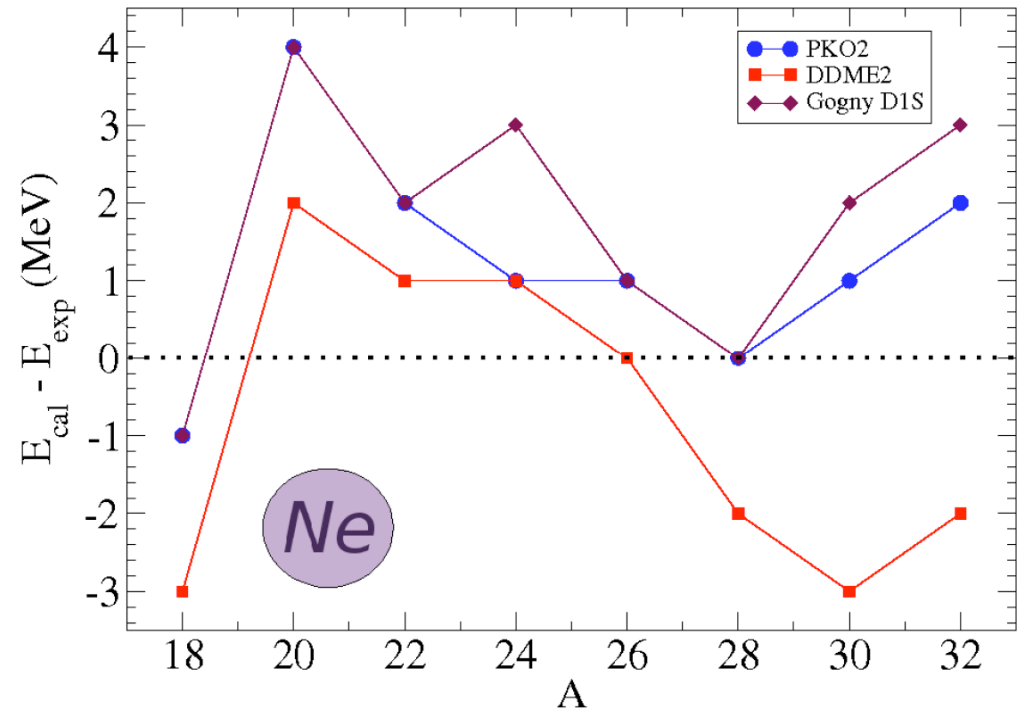


Ne isotope

# Relativistic deformed HFB



- Axially symmetric RHFB model
- Fock term included
- DD coupling constants



Jean-Paul Ebran, PhD (Orsay, 2010)



# Conclusion

- FT-HFB is an appropriate tool to describe superfluid-normal transition
- EDF only parameter, allows to probe the surface/volume nature of the pairing force
- Specific heat of nuclei (compare with exp data): FT QRPA calculations provides the excited energy spectrum
  
- Relativistic HFB in axial symmetry available